

Ingenious COCKER! (Non to Ret thru Tt Go Noe Art can show thee fully but thine own The ware Arithmetick alone can show The wast Sums of Thanks whe for the Luba



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Cocker's

ARITHMETICK

BEING

A plain and familiar Method, fuitable to the meanest Capacity for the full understanding of that Incomparable Art, as it is now taught by the ablest School Masters in City and Country.

COMPOSED

By Edward Ocker, late Practitioner in the Arts of VVriring, Arithmetide, and Pagraving. Being that fo long time promised to the World.

PERUSED and PUBLISHED

By John Hanking Writing-Mafter near St. Georges Church in Southwark, by the Authon correct Coppy, and commended to the World by many eminent Mathematicians and Writing-Mafters in and near London.

This impression is corrected and amended, with many Additions abroughout the Whole.

Licenie J. Sepr. 3. 1677. Rager L'Eftrange.

LONDON

Printed by 7. A. for Even Thacen at the These Bibles of the These Bridge. 1607.

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By Edward Countries to the house of the countries of the countries and the countries to the countries of the countries to the

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TO his much Honoured Friends, Manwaring Davies of the Inner Temple, Esquire; and Mr. Humpbry Davies of St. Mary Newington Buts' in the County of Surry.

John Hawkins, As an Acknowledgment of unmerited Favours, humbly Didicateth this Manael of

Arithmetick.

A 3

To

To the R EAD ER.

Courteous Reader.

Having the Happiness of an Intimate Acquaintance with Mr. Cocker in his Life-time often folicited him to remember his Promise to the World, of Publishing his Arithmetick, but (for Reasons best known to himself) he refuted it; and (after his Death) the Copy falling accidentally into my hands. I thought it not convenient to importier a work of io confiderable a moment, not questioning but it night be as kindly accepted, as if it had been presented by his own hand. The Method is familiar and easie, discovering as well the Thewick as the Practick of that Necessary Art of Vulgar Arithmetick: And in this new Edition there are many remarkable Alterations for the benefit of the Teacher or Learner, which I hope will be very acceptable to the World : I have also performed my promise in Publishing the Decimal Arithmerick, which finds encouragement to my Expectation, and the Bookfellers too, I am

Thine to fer ve thee,

John Hawkins.

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Mr. Edward Cocker's

PROEME or PREFACE.

B I the sacred Inflhence of Divine Providence, I have been Instrumental to the benefit of many; by vertue of those useful Arts, Writing and Engraving: And do now with the same wonted alacrity cast this my Arithmetical Mite into the Publick Treasury, beseeching the Almighty to grant the like blessing to these as to my former Labours.

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Seven Sciences supremely excellent,
Are the chief Stars in Wisdoms Firmament:
Whereof Arithmetick is one. whose worth
Twe Beams of Prosit and Delight spines forth;
This crowns the rest; this makes man's mind complete;
This treats of Numbers, and of this we treat.

I have been often desired by my intimate Friends to publish something on this subject; who in apleasing Freedom have signified to me that they expected it would be extraordinary. How far I have answered their Expectation, I know not; but this I know, that I have designed his work not extraordinary abstruct or prosound.

The Proeme or Preface.

profound, but have by all means possible within the Circumference of my Capacity, endeavoured to render it extraordinary afeful to all those, whose Occasions shall induce them to make use of Numbers. If it be objected that the Books already published, treating of Numbers are innumerable, I answer that's but a small wonder, since the Art is infinite. But that there should be fo many excellent Trasts of Practical Arithmetick extant, and so little practised, is to me a greater wonder; knowing that as Merchandile is the Life of the Weal-Publica; fo Practical Arithmetick is the Soul of Marchan. dise. Therefore I do ingenuously profess, that in the beginning of this undertaking, the unmerous Concerns of the honoured Merchants first possessed my Consideration: And how far I have accommodated this Composure for his most worthy Service, let his own profitable experience be judge.

Secondly, For your Service, most excellent Professors, whose understandings soar to the sublimity of the Theory and Practice of this Noble Science, was this Arithmetical Tractate composed; which you may please so imploy as a Monitor to instruct your young Tyores, and thereby take occasion to reserve your pressons moments, which might be exhausted that way, for your more important Assairs.

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The Brocme or Prefacel

Thirdly, for you, the ingentions off spring of happy Parents, who will willingly pay the full Price of Industry and Evercise for those Arts and choice Accomplishments which may contribute to the Felicity of your suture State. For you, I say, (ingenious Practitioners) was this Work composed, which may prove the Pleasure of your Youth, and the Glory of your Age.

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Lastly, For you the pretended Numerists of this vapouring Age, who are more disingeniously witty to propound unnecessary Questions, than ingeniously judicious to resolve such as are necessary. For you was this Book composed and published, if you will deny your selves so much as to invert the streams of your ingenuity, and by studiously conferring with the Notes, Names, Orders, Progress, Species, Properties, Proprieties, Proportions, Powers, Affections and Applications of Numbers delivered herein, become such Artists indeed, as you now only seem to be. This Arithmetick ingeniously observed, and diligently practifed, will turn to good account to all that shall be concerned in Accompts. All whose Rules are grounded on verity and delivered with Sincerity. The Examples are built up gradually from the smallest consideration to the greatest. All the Problems or Propositions are well weighed, pertinent, and clear, and not one of them

The Process or Preface.

them throughous the Trait taken upon strift;

Zoilu and Monus lie you down and dye; For these Inventions your whole force defye.

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Edward Coeker.

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Courteous

Courteons Reader.

D. Bing well Acquainted with the deceafed Anthor, and finding him knowing and fin dious in the Myflexics of Numbers and Algerra, of which he had fome choice Manufcripts, and agreat Collection of Printed Authors in Several Languages. I doubt not but be bath were bis Brithmetick suitable to his own Preface, and warthy agceptation, which I thought to certifie on a request to that purpose made to him that wisheth thy Welfare, and the Progress of Arts.

John Collens

November 27th. 1677.

This Manual of Arithmetick is recommended to she World by Us whose Names are sub-Scribed viz.

Mr. John Collens)

Mr. James Atkinfon

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And generally Approved by all Ingenious Artifis.

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Likefice it will be convenient to examine from whence Number hath its its or beginning; Molt Applies maintain that that its be Beginning of Number, and it felt no nauther further beginning on the Principles and Descriptions in the first radiments of Geometry, we first find, that the compilers of a boat is no way convendent? Chap coites that it is a Arithmetic of and another one, or that much be so

Arithmetick and Geometry, the winch we do intended to treat of in order; applying the Principles of the order of the Definitions of the Orders of the Principles of the order; applying the Principles of the order, applying the Principles of the order of Greatness is the subject of Geometry, the Multitude of Number is the subject of Geometry, the Multitude of Number is the subject of Geometry, the Multitude of Number is the subject of Geometry, the Multitude of Number is the subject of Geometry, the Multitude of Number is the subject of Geometry, the Multitude of Number is the subject of Arithmeticks and it for their field Principles and chief Fundamentals, and have like Definitions; or at least, a Semblable Congruency.

2. Number, is that by which the Quantity of any hing is Exprelled or Numberd, as the limit is the number by which the quantity of one thing is exprelled a faid to be one, and two by which it is named two, and a half by which it is named or called half, and the cost of 3, by which it is called the Root of 3, the like f any other.

3. Hence it is that Unit is bumber, for the part is the fame matter that is his whole, the Units is art of the Multitude of Units, therefore the Unit is at the fame matter, that is the Multitude of Units as number, it the matter of the Multitude of Units is number, berefore the matter of Unit is number; for cife if om a given number, no number be fublicated, the imbergiven remaineth, let three be the number given, from which number subtract or take away one

nich as fome conecive is no numbers therefore the

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number given remaineth, that is to say, there remaineth three, which is abfurd.

4. Hence it will be convenient to examine from whence Number hath its Rife or Beginning: Most Authors maintain that Unit is the Beginning of Number, and it felf no number; but looking opon the Principles and Definitions in the first rudiments of Geometry, we shall find, that the definition of a Point is in no way congrueds with the Definition of an Unit in Arithmetick; and therefore one, or Unit must be in the bounds or limits of Number, and confequently multiper one of the percent to make mainber and magni-tude conferent in Principles, and like in Definitions, we make and configure is Oppher to be the beginning of mimber, or father the medium between encrealing and decreating numbers, commonly called absolute or whole Numbers, and negative or fractional numbers between Which nothing can be imagined more agreed ble to the nation of a point in Geometry? Why a point is an adjunct of a life, and it left no line! 64 (c) Sypher an adjunct of number and it left no number. ber: And as a point in Geometry cannot be divided o increased into parts; to likewise (6) cannot be divided of increased into parts; for as many points thought phers, though in minute; in the control of the phers, though in minute; in the control of the co the number D'be increased by the grant of the first state of the first ber 6, but if it be granted that the point of that A be extended by brotoped to the point of that A c be that same nave of the point of, the half a continued line, then A B B in a doubt most a continued line, then A B B in a doubt most a continued line, created by the addition of the point C, in like his

Chapter of Number

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ner if we grant D 6 be prolonged to E (c) to that D E (60) be a continued number making 60, then 6 is a grant mented by the aid of (c) as to the conditinting the number (60) fixty; and furthermore that one of pair is material and a number and fint (c) as the beginning of number is proved by all Authors althorization indirectly, for the Tables of Sines and Tangents prove one degree to be a number, because the Sine of I degree is 174524 (the Radius being 10000000) and the beginning of that Table is (c) and to it answereth cooper.

Hence it is that number is not quantity discon-timed, for all their which is but one quantity. Is not quantity disjunct; (60) fixty as it is a number, is one quantity viz one number (60) lixty; therefore as it is number, it is not quantity disjunct for number, is some fact thing in Magnitude, as humidity in Water; for as humidity extends it self through all and every part of Water, to number related to Me Allo as to continued Water doth answer continued humidity, fo to a continued Magnitude doth answer a humidity, to to a continued the midity of continued humidity of continued humber. As the continued humidity of any inture vater fuffered the limiting and but into humber fuffered the dame Davillon, and but inture that his Magnitude dotte. From all which continues that his Magnitude dotte. tions we might enlarge a further Dignession ing Number and Magnitude, by comparing tions of the one with the Trinciples of the naying found a point in Magnitude, we may very tion to a point in Magnitude, we may very clude that number may be congruent to a line the Figurative Number to be equipment in Dennition with a Superficies, and sold of the Conference of t

remetrical remainates some not composed it radiated to the characters of Notes by which a numbers are instituted or by which a Numbers for the collowing (u.g.) a Cypher of nothing 3 Ones 1 world inter-the policy of the characters of the collowing of the characters of the collowing of the characters of the collowing of the cypher, which though of the collowing of the collowing of the cypher, which though of the collowing of the cypher, which though of the cypher of the cyphe

Notation Chap. Jo

felf fignifieth nothing viz.) expresseth not any ce rtain or known quantity, but is the Beginning, Radix, or Root. of Number, and the other Nine Figures or Characters are called fignificant Figures or Digits.

7. In Numbers of any fort, two things are to be confidered, (viz.) Notation and Numeration.

8. Notation teacheth how to describe any Number by certain Notes and Characters, and to declare the value thereof being to described, and that is by De-

grees and Periods.

grees and Periods.

9. A degree confifts of three figures, viz, of three places comprehending Units, Tens and thandreds, for you is a degree, and the first figure (2) on the right hand, stands simply for its own value, being Units or so many ones (viz.) five; the second in order from the right, signifies as many times ten, as there are unites contained in it, (viz.) fixty; the third in the same order signifies so many hundreds as it contains Units, so will the expression of the Number be, three hundred sixty five; also 789, is seven hundred eighty mine. mine. dec.

to. A Period is when a Number confilts of more than three figures, or places, and whose proper order the right hand, and so on to the left, so the Number \$24.52 being given, it will be diffriguished thus, \$2.52 and expressed thus, fixty three chouland four hundred fifty two, likewish 4.58.236.782, being diffriguished, as you see will be expressed thus, sour thousand five lumined seventy eight Millions, two lumined therey fix thousand, seven hundred eighty two. is to prick or diffinguish every third Place b

Number & efficie Absolute or Negative.

An Absolute of indire whole, increasing Number is that widely by annexing of another Figure of Cypher it becomes fon times as much as it flood for before a and if two Figures of Cyphers be annexed, it makes it a thindred times more than it stood for before, (see as if you annex to the Figure & a Cypher dien if will become (60) fixty. So if two Cyphers be annexed,

Chap. 1.

annexed, then it will be(600) fix hundred, and if you do annex to it a (4) four, then it will be (64) fixty four; and if you annex (78) seventy eight, it will be then (678) fix hundred seventy eight, and so on: By annexing more Figures or Cyphers, it will engrease in

a decuple proportion ad Inhutum.
12. A Negative, or Broken, Fractional, Decrealing Number, is that which by prefixing a Point or Prick towards the left hand its value is decreased from so many Units, to so many tenth parts of any thing; and if a point and (o) cypher, or a digit be prefixed, it will be then to many hundred parts, and if a Point and two Cyphers or digits be prefixed, its Value is decreafed to be fo many thousand parts; as if you would prefix before the Figure 3 a point (.) or prick thus (.2) it is then decreased from a Units or Integers, to (2) three tenth parts of an Unit or Integer; and if you prefix a point and cypher thus (.3) it is decreased from a Integers to a hundreth parts of an Integer, and by this means 31. Absolute by prefixing of a point will be decreased to 51. Negative which is five tenth parts of a Pound, equal in value to ten thillings, and to by prefixing of more Cyphers or Digits, its value is decreased in a decuple proportion ad Infinitum. the following Scheme, or rather order of Numbers, we have placed (o) Cypher in its due place and order, as it is both the beginning and medium of Numbers for going from (o) towards the left hand you deal with Intire, Absolute, Whole increating Numbers.

Decreasing Mumbers. Increasing Numbers. 29 376 543 256 2 1 0 1 2 345 678 976 3 CX UXC

But going from (o) the place of Units towards the right hand, you meet with broken, Negative is the national and Decreasing Numbers. And hence it follows that

Multiplication encreaseth the product in Absolute Num-bers, but decreaseth the product in Negative Numbers; Also Division necreaseth the Quotient in whole Numbers, and increaseth it in Negative or Fractional Numbers.

14? An Abidute, Indire, Whole, Increating with ber, hath always a point annexed towards the right

hand, and therefore,

15. A Negative, Broken, Decimal, Decreafing number, hath always a point prefixed before it towards the left halid. When we express Integers or whole num-bers, as a pounds, a feet, 26 men, we usually annex a

point or prick after the Number thus, 5. 5. 26. 347. Bit when we express Decimals, or Numbers that are denved to be intire as decreafing Numbers, we do commonly prefix a point or prick before the faid Decimal or decreafing mumber, thus (.2) that is a tenths, or a primes . 63, that is a hundredths, or, a feconds.

16. A whole or absolute number is an Unit or a compofed Multitude of Units, and it is either a prime, or

cife a compounded number

17. Prime numbers amongst themselves are those which have no multitude of Units for a common meafurer as 8 and 7 or 10 and 13, because not any multi-tude of Units can equally measure or divide them without a Remainder.

18. Compound numbers amongst themselves are those which have a multitude of Units for a common measurer, as 9 and 12, because 3 measures them ex-

actly, and abbreviates them to 3 and 4.

10. A Broken number commonly called a Fraction, is a part or parts of a whole number, viz. a part of an Integer, as a one third is one third part of an Unit.

20. A Broken number or Fraction confins of a parts,

viz. the Numerator and the Denominator.

21. The Numerator and Denominator of a Fraction. are fet one over the other, with a line between them; and the Numerator is fet above the line, and exprelleth the parts therein contained. gereating Numbers,

ChaperD of Aunibers.

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bin 2 2. The Denominator of a Fraction is the Interior number placed below the line, and expredicts the number of parts into which the linit or integer is divided; as let a be the Fraction given to thalk a bothe number and doth expression, for a sa Faction composed on Houttles or Quarters, and the Figure 3 in numbering theirs us that in that Fraction there are 3 of those tourth parts or quarters; also in the same Fraction 4, a is the denominator and doth express the Quality of the first tion, wir, that the whole, or integer, is here divided into 4 equal parts, and a second viscolar divided viscolar divided viscolar divided viscolar divided viscolar divided viscolar divided viscolar divid

equal to the denominator; thus I is an improper Fraction but are in-

ftion, the Reason is given in the Definition. The ac and

pounds view Simple, when it hath one Denomination, and Compound when it confifteth of diverse Denominations of their figures funds Fractions because they are either but of one numerator and one denominator; but if 1 of 2 of 2 of a pound steeling were given, we say that it is a compound broken number, or fraction, because the expression and representation confistent of more denominations than one; and such by some are called bradions of Fractions and they have always this Particle (of) between them.

25. When a fingle broken Number or Fradion, hath for his denominator a number conflicting of a Unit in the first place towards the left hand, and nothing but Cyphers from the Unit towards the right hand, it is then the more aptly and rightly called a decimal Fraction, under this head are all our decreating numbers placed, and in our 13th definition called Negative, and by that order there prescribed, we order them to be Decimals by signing a point or prick before them, or the numerator rejecting the denominator: Therefore ac-

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cording

cording to our last Rule, 12 75 725 are said to be Decimals; and a Decimal Fraction may be expressed without its denominator (as before) by prefixing a point or prick before the numerator of the said Fraction, and then shall the former Fraction 75 and 725 shand thus 9 and 22.

But oftentimes as in the fecond and fourth fractions \(\frac{1}{2} \) and \(\frac{1}{2} \) a prick or point will not do without the help of a Cypher or Cyphers prefixed before the figurificant figures of the numerator, and therefore when the numerator of a decimal fraction, confifieth not of so many places, as the denominator hath Cyphers, fill ap the void places of the numerator with prefixing Cyphers before the significant figures of the numerator, and then figu it for a decimal, so shall \(\frac{1}{2} \) be so and \(\frac{1}{2} \) will be \(\cdot \frac{1}{2} \

26. A Decimal Number or Fraction, is that which is expressed by Primes, Seconds, Thirds, Fourths, &c. and is Number decreasing. Here instead of Natural and Common Fractions, as \(\frac{1}{2} \) of a thing, we order the thing or Integer into Primes, Seconds, Thirds, Fourths, Fifths, &c. that our expression may be consonant to our

former order.

27. In Decimal Arithmetick, we always imagin (and it would be very commodious if it were really so) that all intire Units, Integers, and things are divided sirft into ten equal parts, and these parts so divided we call Primes; and secondly, we divide also each of the former Primes into other ten equal parts, and every of these divisions we call seconds; and thirdly, we divide each of the said Seconds into ten other equal parts, and those so divided we call Thirds and so by decimating the former and sub-decimating these latter, we run on ad infinitum.

28. Let a pound sterling, Troy weight, Averdu-

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pois weight, Liquid Measure, Dry measure, Long meafure, time, dozen or any other thing, or integer ven to be decimally divided; in this notion premiled we ought to let the first Division be Primes, the next division Seconds, the next Toirds, acc. So one pound Sterling being 20 shillings, which divided into ten equal parts, the value of each part will be two thilling therefore one Prime of a Pound fierling will fland thus (.1) which is in value 2 fhillings, Three Primes will fland thus (3) and that is in value of failings. Again a Prime or .1 being divided into ten equal parts, each of those parts will be one Second, and is thus expressed, (.01) and its Value will be found to be ad. farthing and of a farthing; and fo will de fin nific one shilling, or five Seconds. And if of be divided into ten other equal Parts, each of those parts so divided will be Thirds, and will stand thus our and its Value will be found to be 96 of a Farthing, or of a Farthing; and .oog Thirds will be ad. and .o. of a Farthing, or 154 of a farthing, Gc, So that 1375 to will be found to represent 7s. and 6d. for the are 6 fhillings, and the 7 Seconds are as ad and 49 of a penny, and the five Thirds are t penny and penny, both which added together make 752 6d.

29. If you put any bulk or body, representing an . Integer if it be decimally divided; then the parts in the first decimation are Primes, the next Seconds, and the pext decimation is Thirds, the next Fourths, &ce. 48. let there be given a Ballet of Lead, or fuch like, whole weight let be 501. Troy, this eall an Unit, Integer, or thing, then with the like weight and matter, make to other, the which together will be could to be ind will weigh each of them | h a piece, fi matter, and equal to 1. make 10 more, then each of those will weigh 6 ounces a piece; also if a take 6 ounces and thereof make to other final bullets : each of them will weigh 12 permy weight Troy 1 and thus have you made Primes, Seconds, and Toires, in respect of the Integer containing so l. The weight. So that Primes is equal to the half mass, and 2 Primes and & Seconds is a quarter of the mass ; and therefore I

Chap. Notation of the first division, 2 of the second division, and 6 of the third division, will be equal in weight to 1 a quarter of the mats, and contain a Land 3 ounces 30. When a decimal bradion followeth a whole mber you are to leparate or part the decimal from the poole number, by 4 point or prick; so if .75 followed the phole number 32, let them thus 32.75. You will find that divers Authors have divers ways in expressing mixt numbers, as thus, 32/25 or 32-75 or 32-75 but you will find that \$2.75 thus placed and expre icdis fittell for Calculation of 1 10 smire a dies A Har mixt Number hath a parts the whole and the brokens the whole is that which is composed of integers, and the broken is a braction annexed thereunto. So the mixt Number 35 to being given, we fay that 36 the whole Number, which is composed of integers, and he is its the broken number appeared, which sheweth that one of the former integers (of that 46) being diwilled into 12 parts, this of doth express 8 of those ic parts more belonging to the faid 36 integers in Denominative Number and of one, or of many, and those are of divers forts and kinds, viz Singular called Unit as 1 ; and Plural called multitude ; as 213; 4, 5, Single of one kind only called digits, as 1, 2, 2, to furthe 8, 9, and Compounds of many, 25 10, 1, 1, 12, lateger if it be decimally divided : C15-112213611 (05) Proportional, as Single, Multiple, Double, Triple, Quadruple, Or Denominate as Pounds, Shillings, Petre : Undenominate as it, 2 131 Gre Perfect is 164 28, 4964 81 28, 1308 16, 2006 128, Ge. Whole parts are equal to the numbers imperfedt, unequal and more in the lum, Mala to 1, 2; 3: 4; 6; imperied; unequal and left than the fumique & tont, 2,14 i Numbers Chin menfurable and facommenfurable, aspezirandin are Commenterable because three measures them both! 10 and And Arare Incommensurable because no cone common Number or measure can measure them; Linear

 Chap. 2. Of Money, Weights,

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number cubical or folid in form of a Cube. These two latter are otherwise called figurative numbers: There are also other numbers called Tabular, as Signs, Tangents, Secants, Gra. Others that he called Logarithmetick or borrowed numbers, fitted to proportion for easie and speedy Calculation of all manner of Questions.

and likewise that below that, one penny is equal in

the Designation of Shillings, subreby to the noted

the state of the s

in all the following Tables of Weight, Bleaface, Tame Of the Natural Division of Integers, and the several Denominations of the Parts.

1. D Efore we come to Calculation or the ordering of Numbers to operate any Arithmetical Question proposed, we will lay down Tables of the Denomination of several Integers; and after that having mentroned the feveral Species of kinds of Arithmetick we shall immediately handle the Species of Numeration, which are the main Pillars upon which the whole Fabrick of this Art is built. as Artificial Grans

ab d'emy weigh Money, Weights, &c.

2. The least Denomination or Fraction of Money used in England is a Farthing, from whence is produced the following Tables, called the Table of Coyne, (viz.)

4	45,000	Section 1	And therefore,
1	Farth.	CI Farthing	J. s. d. grs.
4	Farth.	ke I Penny	1-20-12-4
	Pence C	St Shilling	1-20 -240 - 960
20	Shill.	CI Pound	1-12-48

The first of these Eables, wix, that on the left band b plain and calle to be understood, and therefore wants

Art dwight fervern only to weigh breast, gold hiver,

1,2

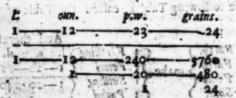
no directions. In the second Table above the line you have 1 l. 20 s. 12 d, 4 qrs. whereby is meant that a pound is equal to 20 stillings, and one shilling is equal to 12 pence, and one penny is equal to 4 Farthings, under the line is 1 l. 20 s. 240 d. 960 qrs. which signifies one pound to contain 20 shillings, or 240 pence, or 960 Farthings; in the second line below that is 1 s. 12 d. 48 qrs. the first standing under the Denomination of Shillings, whereby is to be noted that one shilling is equal to 12 pence, or 48 Farthings, and likewise that below that, one penny is equal in value to four Farthings; understand the like reason in all the following Tables of Weight, Measure, Time, Motion and Dozen.

Of Troy Weight ..

3. The least Fraction or Denomination of weight used in England, is a grain of Wheat gathered out of the middle of the Ear, and well dryed; from whence are produced these following Tables of Weight, called Troy weight.

24 Artificial Grains | 24 Artificial grains | 24 Artificial Grains | 20 Penny weight | 1 Ounce | 1 Pound Troy weight

And therefore,



Troyweight serveth only to weigh bread, gold, filver, and Electuaries; it also regulateth and preseribeth a Form how to keep the Money of England at a certain than the control of the server of the s

flandard, The Goldsmiths have divided the Ounce Try weight into other parts, which they generally cally Mark weight is the denominative parts thereof are as followeth, six, A Mark (being at some Troy) is divided into 24 equal parts, called Carolls and each Carrett into 4 grains, fo that in a Mark are of Grains; by this weight they diffinguish the different finencis of their Gold, for if to the finest of Gold be put a Greets of Alloy (which is of Silver, Copper, or other baser) Metal, with which they use to mix their gold or filver to abate the finencis thereof) both making which cold but an Ounce, or 24 Carefts, then this Gold is faid to be 22 Carefts fine, for if it come to be Refined the 2 Carefts of Alloy will fly away and leave only 22 Carefts of pure Gold, the like to be confidered of a greater or leffer quantity; and as the fineness of Gold is estimated by Carects, to the fineness of Silver is distinguished by ounces; for if a pound of it be pure, and loofeth no-thing in the Refining, such filver is faid to be twelve ounces fine, but if it leseth anything, it is said to contain so much finences as the loss wanteth of 12 ounces, as if it lose an ounce it is faid to be II Ounces fine. and if it lose one ounce 14 penny weight, then it is Gid to be roounces 6 penny weight fine, and that which loseth 2 ounces 4 penny weight 16 grains is said to be of a greater or letter quantity.

Of Apothecaries Weights.

4. The Apothecaries have their Weights deduced from Troy Weight, a pound Tro, being the greatest Integer, a Table of whose division and fub-division followeth, wiz.

I Asund 12 onner and And therefore 1 ounce (2) 8 drams) oun dram forup. 20 grains 12-96-288-5760

E Triver 18 18 18 - 480

adone 14 - 20

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	-12 2 6½ 2 2 7				
1-	12	- las	hide	2004	Tens
		24-136			
•	-	2-6-13	- 26-	52-	364
	Seas-	7-12-6		26-	-180

Note that in some Countreys the Wey is 256 l. Averdupoise as is the Suffolk Wes, but in Effen there is 336 allo a mit and flut a list wife taken fregul eni bnuoq

6. The least Denominative part of Liquid measure is a pint, which was formerly taken from Troy weight, (a pound of Wheat Troy weight making r pint of liquid measure) but in regard of the difference between the Brewers and the Partners of his Majerty's Excise concerning the gauging of Veffels occasioned by the different Opinions of Artifts concerning the folid Inches in a Gallon; it was lately decided by Act of Parliament. the Statute making 282 folid Inches in a Beer-Gallon. and 231 in a Wine Gallon, and confequently the Pint Beer-Measure to contain 35 1 solid Inches, and the Pint Wine-measure to contain 28 2 cubical or folid Inches, from whence is drawn the following Table.

The Table of Liquid Meafure. 351 cubical Inch 1 I pint beer measure 282 cubical Inch I pint wine measure therafore 2 pints I quart last wee are stated in 2 pattles-I gallon 8 gallons & I firk of ale foap or berr. 640 and lange of I fire of beer -- 1 10 galt, and a half ool T fire of Satmon or Eels 2 firkingo -T Kitderkin 2 kilderbins T barrel 42 gallons I Tierce of wine 63 gallons -I boz (bead 2-hogfbends I pipe or butt a Apes or butts

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barley corns of Digral dillad a sum which is to barley corns of Digral dillad

And therefore.

I furlong

1 English mile

40 poles or perches

8 furlongs

mile furl. poles yards feet inches barleoras

1-8-40-51-3-12-3

1-8-320-1760-5280-63360-190080

1-0-220-660-7920-23760

1-161-198-594

1-3-36-108

1-12-36

And note that the yard as also the ell, is usually divided into 4 quarters, and each quarter into 4 Nails. Note also that a Geometrical Pace is 5 feet; and here are 1056 such Paces in an English mile.

2. The parts of the Superficial measures of land are ich as are mentioned in the following Table, vg:

or first the Table of Lund Minute or where

or Perches make { 1 Rood or quarter 16 A 4 Roods }

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By the foregoing Table of long Mcainte, you are informed what a pole, or (which is all one) perch is; and by this that the fourte perches are a Roof of Now a square perch is a Superficies very aptly resembled by a fquare Tresibles, ever fide thereof being a Perch or 5 Yards and a half in length, 40 of them is a Rood, and 4 Roods an Aere. So that a Superficient latis 40 perches long and a broad is an Acre of Land the Acre containing in all 160 fquare Perches.

10. The least denominative part of Time is a Minute, the greatest integer being a Year; from whence

is produced this following Table. I pele or perel

x Minute

The Tuble of Time. 191 19 29 log Oh 8 fuilmes t I. Enelish mile I Minute

4) order and an both!

60 Minutes 1 Hour

3-mary 60 - 200 min 600 - 7020 - - 22760 But the Year is mustly divided into 12 nnequal Ka lendar Months, whose names and the number of Days that they contain follow, viz.

days : 31 Bebruary to 28, lo sel of a se basy and said asan ban

March a organiza So that the Year containeth ball April; 20 Days, and 6 Hours, but the 6 Hour 21 is not reckoned but only every 4th May June 30 year, and then there is a day added to

July and the latter end of February, and then 31 | containeth 29 days, and that year August September 30 called Leaply car, and containeth 36

Ottober 31 days. November 120 1 200 1

40 Square Poles or Perches > main: December 11

Chapita and adoptives

And here note that as the Houris divided into 60 Minutes, lo each Minute is lubdivided into 60 Seconds, and each Second into 60 Turds, and each Third into

The Tropical Year by the exacted observations of the most accurate. Astronomers is found to be 365 Days, 5 Hours, 49 Minutes, 4 Seconds, and 31 Three

CHAP, HIL

Of the Species or Kinds of Arithmetich.

A Rithmetick is either Natural, Artificial, Analy-

2. Natural Arithmetick is that which is performed by the Numbers themselves; and this is either Positive or Negative. Positive which is wrought by certain infallible numbers propounded and this is either Single or Comparative; Single which considered the nature of numbers simply by themselves; and Comparative, which is wrought by numbers as they have Relation on to another. And the Negative part relates to the Rule of Falle.

a. Artificial (by some called Logarithmetical) Arithmetick is that which is performed by Artificial or borowed numbers invented for that purpose, and are called Logarithms.

4. Analytical Arithmetick, is that which thewe from thing unknown to find truly that which is fought a lways keeping the Species without Change.

Algebraical Arithmetick is an obscure and hidden of Accompting by amphers in resolving of bard uestions.

defilions.

6. Lineal Arithmetick is that which is performed by the dines to proportions, as Geometrical projections.

7. Inframental Arithmetick, is that which is performed by Inframents fitted with Circular and Right nes of Proportion, by the Motion of an infex of therwise.

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The parts of fingle Arithmetick are Numeration and the Estraction of Roots
 Numeration is that which by certain known

numbers propounded, we discover another number

of o. Numeration bath four Species ; viz. Addition Substraction, Multiplication, and Division.

CHAP. IV.

Of Addition of whole Numbers.

1. A Ddition is the Reduction of two or more num bers of like kind together into one Sum or Total. Or it is that by which divers monbers are added together, to the end that the Sum or Total value of them all may be discovered.

The first number in every addition is called the Addible number, the other, the number or numbers added, and the number invented by the Addition is called the A gregate or Sum containing the value of the Addition.

The Collation of the mambers, is the right placing of the numbers given respectively to each denomination, and the Operation is the Artificial adding of the numbers given together in order to the finding out of the Aggregate or Sum Just 101 Balanvil

2. In Addition, place the Numbers given respectively the one above the other, in Such fort, that the file degree, place or denomination, may fland in the fami Series, vir. Units under Units, Tens under Tens, Hun-dreds under Hundreds, &c. Pounds under Pounds, Shillings under Shillings, Pence under Pence, Co Yards under Yards, Feet under Feet, &c.

2. Having thus placed the numbers given (as before and drawns line under them, add them together, be ginning with the leffer Denomination, vir. at the right band and to on, fability the fam under the line Respectively; as for Example.

ne be given 2952 and 223 and 135 to be together, I fet the Units in each der each other, and so likewif Tens, Gr. and draw a line under them as in the N place of Units and add them together up-wards, faying, 2 and 3 are 6 and 2 make 8 193 which I fet under the line, and under the fame Figures added together; then I proceed to the next place, being the place of Tens, and add them up in the fame manner as I did the place of Units, flying 3 and 1 are 4 and 5 are 9, which I likewise set under the line respectively 5 then d and them up as I i go to the place of Hundreds, and add them up as I did file other, faying a and a are 3 and 2 are 6 which I also set under the line; and lastly i go to the place of Thousands, and because there are no other figures to add to the a. I set it under the line in its respective place, and to the work is finished; and I find the fain of the 3 given Numbers to be 2608. 4. But if the Sum of the Figures of any Series exceeds ten, or any number of tens, subscribe under the
fame the Excess above the tens, and for every ter
carry one to be added to the next Series towards the
left hand, and so go on until you have finished your addition: always semembring that how great soever the fum of the lights of the laft Series is, it must all be fer down under the line respectively. So 36.78 being given to be added to 23.57. I set them down as in before directed, and as you see in the Margent with a line drawn under them, then I begin and add them together, saying 7 and 8 are 15. 36.78 which is five above to wherefore I let under the tipe the late of the line and early 1 for the 10 to be added. ics laying a that I cherred and in 1924 of

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Charle 25 that I catricel and 2 are 3 and 4 are 6, which I fet down in its Respective place, thus the addition is enbe 6035, feveral Examples of this kind follows as made wards, faying, 3 and 2 2018 \$12 Which I he under the 1997 of the sales of th time by the next place, being the place of Icus, and and the thirty from and I meetively; then the place of thats, from the place of the pl Tens, and add them well our time manner as I did the place of Units, a 70.03 to care pare of land grade, and because there are no other figures to

add to the to det it ander the live in the neipedive

Numbers to be adoß.

place, and in the work is finding of the g

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3. If the Numbers given to be added, are contained under divers denominations; as of Pounds, Shil-lings, Pence and Farthings; or of Tuns, Hundreds, Quarters, Pounds, 696. Then in this case having dither of like kind; beginning at the leaf. Denomina-tion, (minding how many or one denomination do make an integer in the next) and having added them up, for every integer of the next greater denomina-tion that you find therein contained, bear an Unit in mind to be added to the laid next greater denominaexcels respectively under tion, expressing the line, proceed in this manner until your addition be to plain to the Learner. Thus given to be added. viz. 701. of 1. 10 f. denomination of

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THE ELECTION OF THE PROPERTY O

and add them up, faying wand on this war ward gare 4 and 2 make of now ! I die de de gra confider that o Warthings is 1 wo 1 30 1 3 04 penny, and a Parchings, where the joint of its place under the lines and an a hand of the lines and a line of the lines are the lines and a line of the lines are the lines and a line of the lines are the lines are the lines are the lines and a line of the lines are the lines keep I in mind to be sided to 200 a daying at 21s the next denomination of Pener; 20 20 1 20 1 then I go on, faying a that's careius and of I you bas ried and gare 6 and gare i gand to are 25 and gare 29, now I confider that so pence are a failling, and spence, wherefore I let the pence in order under The and keep a mining for the a millings, to be led to the shillings of then I go on, saying, a that I carried and o are it; and its are 20, and 7 are 36, and a 3 are 40 1 then I comider that 40 fillings are 2 pounds and 9 fittlings, wherefore I fet the 9 faillings under the line, and carry two for the 2 pounds, to the next and IAR denomination of pounds, and proceed, saying sother were ried and anake of and gare to and 9 are 16, and 6 are 23; I then fer down 5 and carry 2 for the a tens, and proceed, laying, 2 that I carry and 1 is 3, and 3 are 6, are 7 are 13, and 3 make 16, I fee down 6 and carry I for the 16, and go on, faying I that I carried and I are 2, which I fet in its place under the line, and the work is findhed; and this I find the Sum of the foreskid Manbers to be 2651. 9 m. d. 2972. This to the ingenious Practitioner is sufficient, but I shall (for the further albumbnating of weaker apprehensions) explain the operation of another Example in Troj weight; and here the Learner must take notice of the Table of Troj weight mentioned or fet down in the third Section of the fe-cond Unifier. The mimbers given in this Example are 38 ? For the pure \$8 gr. And 50 ?! TO be 10 p.w.s. 12 gas And 421 t. 68 oz. los pin. loghe And in ordered the addition thereof, le place them as you fee, and proceed to decration; aying, 10 and 12 are 28, and 18 are 45; now because 24 grains make Addition

Addition of the Chapter (Chapter) Cha 1 penny weight and 22 grains ; 38-07-13-18 wherefore I for down 22, and 50 10 1710 12 carry I for the semy weight, and 142 100 10 5 16 going on I fay, I that I carry and and carry I to the ounces, faying I that I carry and & are, o, and so are so, and 7 are 26, and because 26 owner make a pount a owner. I fet down a for the sun-ces and carry 2 to the pounts; going on, 2 that I carry and 2 are 4 and 8 make 10 that is 2 and go 1 4 them 2 I carry and 4 are 5 and 5 are 2 and 3 are 13, which I fet down as in the Margent, and the work is finished, and I find the sum of the land numbers to amount to 1321. 24 ding of the following Examples, or any other that thall come to the View. The Way of proving these en 75 18or any Sums in this Rule is thewed immediately after 50and c are to and c are a single of the course of the carry a for the carry and a carry a forth of the carry and a carry a forth of the carry and a carry a carry a carry a carry and a carry a 21-12-18-101 11841-09-10 13 1 1 176-10 07-3 10 0 in its emergence inc. and the port is midfied; and the required inc. and the required be and the required to the ingenious tradiand again the Addition of Troy Weight - sellage to soil 5-5-ASTOCIONAS DE SONO DE stand here the 8-2-I= 3-

Addition of Apothecaries Weights.

1. oun. dr. fer. gr.	1. oun. dr.fer. gr.
48-07-1-0-14	60-03-4-0-10
74-05-5-2-10	48-10-6-0-14 1 34-08-2-1-FS
64-10-7-1-16 17-08-1-0-11	18-11-2-2-11
34-09-6-1-09	160-07-1-2-15
240-05-6-1-00	35-02-5-1-07
	358-07-17-0-12/

Addition of Averdujois weight.

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m C.	rg. 1.	f. dr.
5-18	21	16-12
50-1	-17	THE WAR IN THE REAL PROPERTY.
21-07-	25	15 94 10
12-14-		10-00-09
8-6	005	106. 03 00
To los		100
April 10 Mariana	-	-

Addition of Liquid Measure.

n Pipe bbd. gall.	Time bhds. gall pre-
5 0 1 17	30 3 40 4 12 0 28 6
2 1 56	47 5 60 5 57 3 22 3
1-1-1-18	17-0-00-0
3 1 60	166-1-26-2

le and distriction to

Addition of Dry Measure.

chald. ars. bush. per	
13 1 4	50-1-3-
1636	1 40-2-0-
40-1-0-0	-
73 3 0	3 152 3

Addition of Long Measure.

		ells	
35 3	2	13-	-3
38-0-			
3-1-0			
2181	-	-	-
and the same	1.000	day	_

Addition of Land Measure.

			Acre Rood p
14-80	-0-	24	47 3
48-	-3-	30	73-2-60-0-
50-			04 2
185-	1000 000 000	19 May 1	286- 3

nweb to first confine the profess of Child

6. Addition is proved after this manner, when you have found out the fum of the Numbers given, then ceparate the uppermost line from the rest, with a stroke or dash of the pen, and then add them all up ugain as you did before, leaving out the uppermost line, and naving so done add this new invented sum to the uppermost line you separated, and if the sum of those lines he equal to the sum field found out, then the work was performed true, otherwise not: As for Example, let us prove the sirst Example of Addition of soney whose sum we found to be 26 cl. 9 s. 5 d. 2 grs. and which we prove thus, having aparated the uppermost number 18 s. d. qrs. ser from the rest. by a line as 126—12—04—2

and which we prove thus, having parated the uppermost number from the rest, by a line as ou see in the Margent, then I dd the same together again, teading out the said uppermost line, no the sum thereof Dict under he sist sum or true sum, which oth amount to 128 1. 16 5. or d. qrs. then again I add this new sum to the uppermost line that efore was separated from the est, and the sum of these two 265 1. 100 5. 65 d. 12 qrs. the

136—1	3-	04-2
33-	18—	10-3 09-1
265	9-	05-2
128-	16-	0-10
265-0		

me with the first Sum, and therefore I conclude hat the Operation was rightly performed.

The main end of Madition in Questions Resolvale thereby, is to know the sum of several Debts, arcels, Integers, &c. Some Questions may be them hat follow.

Quest. 1. There was an old Man whose age was reuired; to which he replyed, I have seven Sons, each awing two years between the birth of each other, and the 44 year of my age my eldest Son was born, thich is now the age of my youngest; I demand that was the Old Mans age?

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Now to refolve this Queftion, first set down the Fathers age at the birth of his first Child. which was 44, then the difference between the eldeft and the youngest, which is 12 years, and then the age of the youngest which is 44,0 100 and then add them all together, and their fum is 100 the complet Age of the Father.

Quest. 2. A Man lent his Friend, at several time these several Sums, (viz.) at one time 63 L at another time 50 L at another time 48 L at another time 156 l. now I defire to know how much was lent his

in all the state of the state o

Set the Sums lent one under another, 63 as you fee in the Margent, and then add 50 them together, and you will find their Sum 48 to amount to 317 L which is the Total of all 150 the feveral Sums lent, and fo much is due to the Creditor.

217 Quest. 2. From London to Ware is 20 miles, thence Huntington 29 miles, thence to Stamford 21 miles, thence to Tuxford 36 miles, thence to Wentbridge 25 miles from thence to Tork 20 miles. Now I defire a know how many miles it is from London to Tork accor ding to this reckoning.

Now to answer this Question, set down 20 the feveral distances given, as you fee in >29 the Margent, and add them together, and you will find their Sum to amount to 151, 25 which is the true Distance in miles between 20 de London and York.

Quest. 4. There are two numbers, the least when the of is 40, and their Difference is 14. I defire to know what is the greater number, and also what is the Sum of them both? First, set down greatest 51 ow the least, viz. 40, and 14 least 4 what is the greater number, the difference, and add them together, and their fum is 54 for the greatest number,

Sum o

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then I fet (40 the least) under 54 (the greatest) and add them together, and their Sum is 94 equal to the greatest and least numbers. and analy a line under them, then be

CHAP.

Of Substraction of whole Numbers.

2: O'Ubstraction is the taking of a leffer number out of a greater of like kind, whereby to find out third number, being or declaring the inequality, excefs, or difference between the numbers given; or Substraction is that by which one number is taken out of another number given, to the end that the relidue or remainder may be known, which remainder is also alled the Rest, Remainder, or Difference of the numbers given.

2. The number out of which Substraction is to be made, must be greater, or at least equal with the other Number given; the higher or superiour number s called the major number, and the lower or infetior is called the minor number, and the operation of Substraction being finished, the Rest or Remainder is

called the Difference of the Numbers given.

2. In Substraction place the Numbers given respefrively, the one under the other, in such fort as like degrees, places, or denominations may fland in the lame Series, viz. Units under Units, Tens under Tens, re. Pounds under Pounds, Gre. Feet under Feet, and Parts under Parts, dec. This being done, draw a ine underneath, as in Addition.

4. Having placed the Numbers given as is before diected, and drawn a line under them, substract the ower Number (which in this cafe must alwayes be offer than the uppermost) out of the higher number, and subscribe the difference, or remainder respectively below the line; and when the Work is finished, the

G 2 number

from 795836, I fet the leffer under the greater asi the Margent, and drawa line under them, then be ginning at the Right hand, I fay I out of 6 and there remains s, which I fet in order under the line; then I proceed 364521 to the next, faying 2 from 2 refts 1,

which I note also under the line, and

thus I go on until I have finished the Work, and then I find the Remainder or Difference of a greater of lake made whereby 215154 ad

5. But if it to happen (as commonly it doth) the the lowermost number or figure is greater than the uppermost; then in this case add ten to the upper most number, and substract the said lowermost num her from their Sum, and the remainder place unde the Line, and when you go to the next Figure below pay an Unit by adding it thereto for the ten you bor towed before, and subfinist that from the higher number or figure: And thus go on until your Substraction be finished. As for Example, Let 437503 be given from whence it is required to substract 153827, I di spose of the numbers as is before directed, and as you fee in the margent; then I begin, faying 7 from 3 cannot, but (adding to thereto I fay) of from 12 and

Line in order; then I proceed to the 437503 next Figure, faying a that I borrowed 41153827 and 2 is a from o I cannot, but a from 10 and there remains 7, which I like-283676 wife fet down as before; then I that I borrowed and 8 is 9 from 5 I cannot,

there remains 6 which I fet under the

but 9 from 15 and there remains 6 ; then I I borrow ed and z is a, from 7 and there remains 3 ; then from 3 I cannot, but 5 from 13 and there remains 8 then I I borrowed and 1 ard 2, from 4 and there rel numbers are substracted one from another, the Thequa lity, Remaindes, Excels of Difference is found to be

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Refts 2736374 1 . Refts 3609882

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6. If the Sums or Numbers to be Substrutted, are of feveral Denominations, place the leffer Sum below the greater, and in the fame rank and order as is shewed in Addition of the same Numbers; then begin at the Right hand and take the lower number out of the uppermost if it be leffer; but if it be bigger than the unpermoft, then borrow an Unit from the next greater Denomination, and turn it into the Parts of the leffer Denomination, and add those parts to the appermost Number, and from their Sum Substract the lowermoft. noting the remainder below the Line; then proceed and pay 1 to the next Denomination for that which you borrowed before, and proceed in this order until the work be finished. An Example of this Rule may be this that followeth, let 375 L 13's, 07 d. 1 gr. be given; from whence let it be required to fubstract 47 L 16 s. 03 d. 2 grs. In order whereunto I place the numbers as you fee in the Mar-

gent, and thus I begin at the least 1. Denomination, faying two from 375-13-07-1 one I cannot, therefore I borrow 57-16-02-2 one penny from the next Dencmination and turn it into Far- 317-17-03 things, which is a, and adding -

4 to I which is s, I fay, but 2 from 5 and there remains 3, which I put under the line; then going on, I fay, I that I borrowed and a is from 7 and there refts 2; then going on, I fay 16 from 13 I cannot, but (borrowing one pound and turning it into 20 faillings, I add it to 12, and that is 33) wherefore I fay, fixteen from 33, and there remains 17, which I fet under the line and go on, faying I that I borrowed and 7 is 8, from 5 I cannot, but 8 from 15 and there temains 7; the one that I

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borrowed and 3 is 6, from 7 there rests 1, and 0 from 3 rests 3, and the work is done: And I find the is mainder or difference to be 317 1, 17 s. 03 d. 3 que

Another Example of Troy-weight may be this, would fubstract 17 l. 10 oz. 11 p.w. 20 gr. from 24 05 oz. 200 p.w. 08 gr. I place the Numbers according to the l. oz. p.w. g Rule, and begin, faying 20 from 24-05-00-8 I cannot, but borrow 1 penny 17-10-11-1 weight, which is 24 grains, and

add them to 8, and they are 32, wherefore I say 20 from 32 reft 12; then 1 that I borrowed and

11 is 17, from 00 I cannot, but 12 from 20 (borrowing an Ounce which is 20 penny weight) and there re main 8; then 1 that I borrowed and 10 is 11, from I cannot, but 11 from 17 and there refts 6; then 1 that I borrowed and 7 is 8, from 4 I cannot, but 8 from 14 and there reft 6; then 1 that I borrowed and 1 is from 2 and there refts nothing; fo that I find the Remainder or difference to be 61. 607, 8 p.m. 12 gr.

7. It many times happeneth that you have man Sums or Numbers to be Jubstralled from one number; a suppose a Man should lend his Friend a certain sum of Money, and his Friend had paid him part of his Debat several times, then before you can conveniently know what is still owing, you are to add the severa Numbers or Sums of Payment together, and substral their Sum from the whole Debt, and the Remainder is the Sum due to the Greditor, as suppose A lendeth to B 564 l. 13 s. 10 d. and B. hath repaid him 79 l. 16 s.

their Sum from the whole D the Sum due to the Creditor B 564 l. 13 s. 10 d. and B. hath repaid him 79 l. 16 s. 08 d. at one time, and 163 l. 18 s. 11 d. at another time, and 241 l. 15 s. 08 d. at another time; and you would know how the Accompt flandeth between them, or what more is due to A. In order whereunto

l. s. d.

Lent 564—13—10

Paid at 79—16—01

several 163—18—11

payments 241—15—08

paid in all 485—11—03

Remains 79—02—01

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I first set down the Sum which A lent, and draw a line underneath it, then under that line set the several Sums of payment as you see in the Margent; and having brought the several Sums of payment into one Total by the fifth Rule of the fourth Chapter foregoing, I find their Sum amounteth to 48; l. 11 s. 3 d. which I substract from the Sum sirst lent by A, by the fixth Rule of this Chapter, and I find the Remainder to be 79 l. 2 s. 7 d. And so much is still due to A.

When the Learner hath good knowledge of what hath been already delivered in this and the foregoing Chapter, he will with case understand the manner of

working the following Examples.

Substraction of whole Money.

1 6	d.	7.		d.	qrs.
Borrowed 374-10	-03 1	700-	-10-	-11-	-2
A 2 metro 10 -					
Remains 304—14	-04	691	P5*	_n-	3
L	d.	L	an de	e d.	qrs.
Borrowed 1000—00 Paid 10—00	F-06	11-	13-	-00-	,
Rem. due 2 980-15	-o6	699	-09-	-11-	3
Borrowed	The X		-11c		
	170		0	-	-
Paid at severa	1) 251	11	3-1	0-	·I
payments a	£ 591	0	4	4	2
	119	13-32-33	and the second	CONTRACTOR OF STREET	
Remain due	210	10	7	Sub D	-I

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Substraction of Trey Weight,

4			33379	110000	I'm.	
1150	300	A PSET	9 3 (2)	Marie Land	1000	56
	RAL	Er 3.7	DENT S	00-	1311 1016	-00
Hol	T	5.00	Vacanta	-04-	-16-	
V. 7-35	2 49.4	- 45	Charles (C.)	Company of	MONTH A	DHC CA

Remains 95-07-16-09

a of sub-life labor (0 d p.m. 47)

Bold in all 245 10 07 07

Rem. unfold 225 00 05 17

Substration of Apothecaries Weights.

L. oz. dr. fcr. gr. l. oz. dr. fcr. gr. Bought 12-04-3-0-00 20-00-1-0-07 Sold 8-05-1-1-15 10-00-1-2-15 Remains 3-11-1-1-05 9-11-7-0-15

Substraction of Averdupois Weight.

Bought 25 0 15 5 07 1 10 10 09 3 Sold 16 2 20 3 17 1 16 09 13

Remains 18 2 20 1 1 09 3 22 00 08

Company of the state of the state of	A The submitted by the submitted of
Chap. 5. whole IV	ambers.
Substraction of	and the same of the
Surjet Surjet across of	Fidura mediation
Tun bha. gall,	Tun bhd. gall. sec.
Bought 40 1 30	69-15113-15142-4
Sold 16-1-40	ni da da da cellana da
Remains 23 - 3 - 53	44 w 3/3 3/058 01 W 5
Trock of Technique Tomana	Nothin madel 1820 to 10 to
Substruction of	Dry Measure.
503750 - 60 - 60 - 60 - 60 - 60 - 60 - 60 -	and the same and the characters
Chal. qrs. bufh. pec.	Chal. qrg. buff. pec.
Sold 54-1-04-3	46 2 30 30 3
Remains 45-2-03-1	
Remains 45-2-03-1	intent to too the last
Of citis Cours, where it is	required to heller 2
Substraction of	Long proglare
yards qrs. nails	yards. q's. nails
Bought 160—1—0 Sold 64—1—2	अर ३४४ त्रह प्रातितामाण्या से व
Sold 84 1-2	ने विकास अंगिया अन्य
Remains 95 3-2	104-2-12-2
10 m	वित्रा व्यवश्यातील क्षेत्रमाता वार्गा वर
Substraction of	Land Measure.
The state of the s	Acres road per
Bought 140 2 13	Acres rood per
Sold 70-3-22	54-6-16
Remains 69 2 31	and a Monteq Landy
178 5 373	\$45
	e et made, create and
Carlot Act and Control of the Act of State	Subfiraction.
8. When your Substracti	ion is ended, if you delire
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to prove your work, whether it be true or no, then add the remainder to the minor Number, and if the Azeregate of these two be equal to the major Number, then is your Operation true, otherwise falle; thus let us prove the first Example of the fifth Rule of this Chapter, where after Substraction is ended. the Numbers frand as in the Margent; 437503 the Remainder or difference being 283676. 153827 Now to prove the work, I add the faid Remainder 283676 to the minor number 283676 153827, by the fourth Rule of the foregoing Chapter, and I find the Sum or 437503 Aggregate to be 437503 equal to the major 153827 Number, or Number from whence the 283676 leffer is substracted; behold the work in the Margent. 437503

The Proof of another Example may be of the first Example of the fixth Rule of this Chapter, where it is required to substract 57 L. 16 s. 03 d. 2 grs. from 375 l. 13 s. 07 d. 1 gr. and by the Rule 1 find the Remainder to be \$17 L. 18 s. 02 d.

Remainder to be 317 l. 17 s. 03 d. 2 qrs. now to prove it, I add the faid Remainder 317 l. 17 s. 03 d. 03 qrs. to the minor number 57 l. 16 s. 03 d. 02 qrs. and their fum is 375 l. 13 s. 07 d. 1 qr. equal to the major number, which proves the work to be true, but if it had happened to have been either more or lefs than the faid major.

365-13-07-1 57-16-03-2 317-17-03-3

375-13-07-

number, then the operation had been falle.

9. The general effect of Substration is to find the differences or excess between two numbers, and the rest when a payment is made in part of a greater Sum, the date of Books printed, the age of any thing by knowing the present year, and the year wherein they were made, created or built, and such like.

The Questions appropriated to this Rule are such as

follow.

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Quest. 1. What difference is there between one thing of 125 foot long and another of 66 foot long?

To refolve this Question, I first set down the major or greater number 125, and under it the minor or lesser number 66, as is directed in the third Rule of this Chapter, and according to the fourth Rule of the same I substrate the minor from the major, and the Remainder, Excels or Difference I find to be 39; see the Work in the Margent.

Quest. 2. A Gentleman oweth a Metchant, 365 L. whereof he hath paid 278 L. what more doth he owe?

To give an Answer to this Question, I first set down the major number 365 l. and under 365 it I place 278 the miner, and substract the one 278 from the other, and thereby I discover the Exects, Difference or Remainder to be 87,000 87 and so much is still due to the Creditor. As per Margent.

Ouest. 3. An obligation was written; a book printed, a Child born, a Church built, or any other thing made in the year of our Lord 1687.

2572, and now we account the year of our 1572.

Lord 1687, the Question to know the age of the faid things, that is, how many years are passed since the faid things were made;

1 say if you substrail the letter number 1572, from the greater 1687, the Remainder will be 115, and so many years are pass since the making of the said things; as by the Work in the Margent.

Quest. 4. There are three Towns lie in a streight line, viz. London, Huntington, and Jork, now the Distance between the farthest of these Towns, viz. London and Tork is 151 miles, and from London to Huntington is 49 miles, I demand how far it is from Huntington to Tork.

To refolve this Queftine, fubstrall 49 the diflance between London and Huntington, from 131 131 the Distance between London and Torky 49 and the Remainder is 1702, if for the true distance between flantington and Torky See the 102 Work in the Margent

rich in the min of the man in the man in the color of the C H A P. . V L . .

Of Multiplication of whole Numbers.

1. Utiplication is performed by two humbers of like kind, for the Production of a third, which shall have such reason to the one, as the other hash to Unit, and in Effect is a most brief and artificial compound Addition of many equal Numbers of like kind into one Sum. Or Multiplication is that by which we multiply two or more numbers, the one into the other, to the end that their Product may come forth, or be discovered.

ber by another is to often as there are Units in that number, by which the other is increased, or by having two numbers given to find a third, which shall contain one of the Numbers as many times as there are Units

in the othersy value wo

2. Multiplication hath three parts, first the Multiplicand, or number to be multiplyed. Secondly, the Multiplyer, or number given, by which the multiplicand is to be multiplyed. And Thirdly, the product or number, produced by the other two, the one being multiplyed by the other, as if 8 were given to be multiplyed by 4, 21 fay 4 times 8 is 32, here 8 is 4 the Multiplyed and, and 4 is the Multiplyer, and 32 is the Product.

compound that confifts of many.

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Single

Single Multiplication is faid to confift of one figures, because the Multiplicand and Multiplier counsil each of them of a Digit, and no more, so that the greatest product that can arise by lingle Multiplication is 87, being the square of 9; and Compound Multiplication is faid to consist of many figures, because the Multiplicand or Multiplier consists of more places than one; as if I were to multiply 436 by 6, it is called Compound, because the Multiplicand 436 is of more places than one, (viz.) 3 places.

4. The Learner lought to have all the varieties of fingle Multiplication by heart before he can well proceed any further in this Art, it being of most Excellent Use; and none of the following Rules in Arithmetick but what have their principal dependance thereupon, which may be learnt by the following Table.

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Tarris Total	2	3	4.	3	6	1	8.	9
12	te of y	6	38.8	1010	14	144 V	QI Su	1816
Q103	26	1.9	012	dian	18	21	24	27
0193	8	12	116	20	2/ 1	28	32	36
5,5	1.0	15	20	1250	30	35	2400	1497
mi d	8128	ota	0.44	ragio 1	1360	1420	48	54
1247	74	279	28	33	42	19	56	62
B.	16	24.	32	49	48	56	3641	72
יפונה!	ne	lay	25	1457	984	969	72	8 10
E sie	CONTRACTOR	SETOIE .	12.113	Il marri	097/190	DEMONT	MARC	1-17116

The use of the precedent Table is this. In the appearant Line of Column you have expressed all the digus from a to of and blewise beginning at a and going downwards in the side Column you have the lane; so that if you would know the Product of the column and the column and any and any are the lane.

tin mind for the four Lens, then I proceed.

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any two fingle numbers multiplyed by one another, look for one of them (which you pleafe) in the uppermost Column, and for the other in the fide Column, and running your eye from each Figure along the respective Columns, in the common Angle (or place) where these two Columns meet, there is the product required. As for Example, I would know how much is 8 times 7, first I look for 8 in the uppermost Column, and 7 in the fide Golumn; then do I cast my eye from 8 along the Column downwards from the same, and likewise from 7 in the fide Column, I cast my eye from thence towards the Right-hand, and find it to meet with the first Column at \$6, so that I conclude \$6 to be the Product required, it would have been the same if you had looked for 7 in the top, and 8 on the side, the like is to be understood of any other such Numbers. The Learner being per-

s. In Compound Multiplication, if the Multiplicand confilts of many places, and the Multiplicand one Figure; first set down the Multiplicand, and under it place the Multiplyer in the place of Units, and draw a Line underneath them; then begin and multiply the Multiplyer into every particular Figure of the Multiplicand, beginning at the place of Units, and so proceed towards the left hand, setting each particular Product under the Line, in order as you proceed, but if any of the Products exceed 10 or any number of Tens, set down the Except, and for every 10 carry a Unit to be added to the next product, always remembring to set down the Total Product of the last Figure; which work being finished, the Sum of Number placed under the Line shall be the true and Total Product required. As for Example, I would multiply 478 by 6, first lifet down the 12478.

therefore I fet down 8 (the excess) and bear 4 in mind for the four Tens, then I proceed, say-

Units, and draw a line underneath them more of

ing 6 times 7 is 42, and 4 that I carried is 46, I then fet down 6 and carry 4, and go on, faying 6 times 4 is 24, and 4 that I carried is 28, and because it is the last Figure, I set it all down, and so the work is finifled, and the product is found to be 2969, as was required. - 17 into 18 sauster 12010

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6. When in Compound Multiplication the Multiplier confifteth of divers places, then begin with the Figure in the place of Units in the Multiplyer, and multiply it into all the Figures in the Multiplicand, placing the product below the line as was directed in the last Example; then begin with the Figure of the fecond place of the Multiplyer, (viz.) the place of Tens, and multiply it likewise into the whole Multiplicand (as you did the first Figure) placing its product under the product of the first Figure, do in the same manner by the third, fourth and fifth, drc. until you have multiplyed all the Figures of the Multiplyer particularly into the whole Multiplicand, still placing the Product of each particular Figure under the Product of its precedent Figure; herein observing the following Caution.

In the placing of the Product of each particular Figure of the Multiplier, you

chapter, viz. not to place Units under Units, and Tens under Tens, orc. but to put the Pigure or Cypher in the place of Units of the fecond line under the fecond figure or place of Tens in the line above it, and the Figure or Cypher in the place of Units of the third line under the place of Tens in the fecond line, &c. Observing this order till you have finished the work, why ftill placing the first figure of every line or product under the fecond Figure or place of Tens in that which was above it, and having to done, draw a line under all these particular products, and add them together; fo shall the fum of all these Products be the Total Product required.

As if it were required to multiply 764 by 27, I fet them down the one under the other with a line drawn under-

to multiply \$486 by 465, I dispose of the Multiplicand and Multiplyer, according to-5486 Rule, and begin multiplying the first Fi-465 gure of the Multiplyer, which is five into the whole Multiplicand, and the Product is 27430 27430; then I proceed and multiply the 32916 fecond Figure (6) of the Multiplier into the 21944 Multiplicand, and find the product to amount to 229 16 which is subscribed under 23,50900 the other product respectively, then do I multiply the third and last figure (4) of the Multiplyer into the Multiplicand, and the Product is 21944, which is likewise placed under the second Line respectively , then I draw a Line under the said Products being placed the one under the other ad cording to Rule) and add them together, and the fun is 2550990 the true Product fought, being equal to

5486 times 465, or 465 times 5486.

them down the one ander the other within the diawn

Another Example may be this; Let it be required

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More Examples in this Rule are these following

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Compendiums in Multiplication.

7. Although the former Rules are sufficient for all Cases in Multiplication, yet because in the Work of Multiplication many times great labour may be fixed. I shall be superior an american multiplication to the state of the st

labour may be faved, I shall the facto deminacquaint the Learner with forme Compendiums in order dore, Classic thereto, viz. If the Multipli-

cand or Multiplyer, or both of them end with Cyphers, then in your multiplying you may neglect the Cyphers, and multiply only the fignificant Figures, and to the Product of those fignificant Figures, and to many Cyphers as the Numbers given to be multiplied did end with; that is, annex them on the Right hand of the faid product.

the Right hand of the said product, so 32000 shall that give you the true product required. As if I were to multiply 32000 by 4300, I set them down in order to 56 be multiplyed as you see in the Margent, 128

but liegietting the Cyphers in both numbers I only multiply 32 by 43, and the 137600000 Product I find to be 1376, to which I

annex the 5 Cyphers that are in the Multiplicand and Multiplyer, and then it makes 137600000 for the true Product of 32000 by 4300.

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8. If in the Multiplyer Cyphers are placed be-

tween fignificant figures, then multiply only by the fignificant Figures neglecting the Alice Cap. 6. de Arithm. cant Figures neglecting the Cyphers, but here special no-

tice is to be taken of the true placing of the first figure after the neglect of such Cypher or Cyphers; and therefore you must observe in what place of the mustiplyer the Figure you multiply by standeth, and set the first Figure of that Product under the same place of the product of the first figure of your Multiplyer As for Example, let it be required to multiply 271 568

by 40007, first I multiply the Multiplicand by 7, and the Product is 2600976, then neglecting the Cyphers I multiply by 4, and that Product is 1486272, now I confider that 4 is the fifth figure in the Multiplier, 1486272 therefore I place two (the first Figure of the product by four) under 14865320976 the fifth place of the first Product by

40007

371568

7, and the rest in order, and having added them to gether, the Total Product is found to be 14865220976,

327586	1	7864	371
6030		200	
982758	i i sille	31467	484
1965516	rate bild	4718629	
1975349580	Audelion -	162037500	WANT TO A

other Examples in this Rule are these following.

9. If you are to multiply any Number by an Unit with Cyphers, (viz.) by 10, 100, 1000, 600. the annex fo many Cyphers before the Multiplicand, and that number when the Cyphers are annexed is the Product required; as if you would multiply 428 by 100 annex two Cyphers to 428 and it is 42800 : If it were required required to multiply roz by toood, milek 4 Cyphers and it gives 1020000 for the Product required.

The Proof of Multiplication.

In Multiplication is proved by Division, and to speak truth all other ways are falle ; and therefore it will be most convenient in the first place, to learn Division, and by that to prove gare & falle

Multiplication. There is a

Way (at this day generally used in Schools) to prove Multiplication, which is this, first add all the Figures in the Multiplicand together, as if they were fimple Numbers, casting away the Nines as often as it comes to fo much, and noting the Remainder at laft, which in this case cannot be so much as 9: Cast likewise the Nines out of the Multiplier as you did out of the Multiplicand, and note that Remainder , then multiply the Remainders, the one by the other, and caft the Nines out of that Product, observing the Remainder; and laftly, cast the Nines out of the Total Product, and if this Remainder be equal to the Remainder laft found. then they conclude the Work to be rightly performed; but there may be given a thouland (may infinite) falle Products in a Multiplication, which after this manner may be proved to be true, and therefore this way of proving doth not deferve any Example; but we shall defer the Proof of this Rule till we come to prove Division, and then we shall prove them both together.

11. The general effect of Multiplication is contained in the definition of the fame, which is to find out a 3d. Number, fo often containing one of the two given

Numbers as the other containeth Unit:

The fecond effect is by having the length and breadth of any thing (as a Parallelogram, or long Plain) to find the superficial Content of the same, and by having the Superficial Content of the Base and the length to find out the folidity of any Parallelopipedon, Cylinder or other folid Figures.

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The third sided is by the contents, price value buying, felling, expense, wages, exchange, fimple interest, gain or loss of any one thing, be it Money, Merchandize, to to find out the value, price, ex-pence, buying, felling, exchange, or interest of any Number of things of like Name, Name and Kind.

by the Contents, Value, or Price of one part of any thing denominated, to find out the Content, Value Price of the whole thing, all the parts into which the whole is divided, multiplying the price of one of Vay (at this day generally nied in School stray Boils

The fifth effethis, to aid, to compound, and to make other Rules, as chiefly the Role of Proportion, called the Golden Rule, or Rule of Three; also by it; things of one Denomination are reduced to another of o

of the Integer, the Product will discover the price of

the Quantity or Number of Integers given, bus

In the Cangular Solid, if you multiply the breadth of the Bale by the depth, and that Product by the length, this last Product will discover the Solidity of Content of the fame Solid

Some Questions proper to this Rule may be these following increase which star this

Quelte Le What is the Content of a fquare piece of Ground, whose length is 28 percher, and breadth as perches de Hillotul airs ho

Anfine 364 Square perches; for multiplying 28 the length by 13 the breadth, the Product is so much

Quest. 2. There is a square battle whose Flank is 47 Men, and the Files 19 deep, what number of Men doth that Battle contain ? Facil 892 ; for multiplying 47 by 19, the Product is 899. Tollar

Luch. 3. It any one thing coft a shillings, what shall o fuch things cost & Anfiver 36 shillings; for multiply ing 4 by 9, the Product is 26 the mile of this

Quest. 4. If a piece of Money or Merchandize be worth or coft 17 shillings, what shall ro such pietes

of Money or Merchandize ouft? Fuch 323 thillings,

which is equal to 16 L og s.

per Month, what is the Wages or Charges of 49 Soldiers or Servants for the fame time? Multiply 49 by 14, the Product is 6865, or 341, of 1, for the Anjust. 2011, 6. If in a day there are 24 hours, how many

Quelt. 6. If in a day there are 24 hours, how many hours are there in a year, accounting 365 days to conflict the year? Facil 8760 hours, to which if you add the 6 hours over and above 365 days as there is in a year, then it will be 8766 hours, now if you multiply this 8766, by 60, the number of Minutes in an Hour, it will produce 525960 for the number of Minutes in a Year.

to) are Divider, I LV as B. AcB. at the Day the Divide

all so t Of Division of Whole Numbers to band

Number or Quantity given into any parts affigned; or to find how often one Number is contained in another; Or from any two Numbers given to find a third that shall consist of so many Umis, as the one of those two given Numbers is comprehended or contained in the other was and and about the order.

2. Division but three Parts or Numbers remarkable, viz. First the Dividend Secondly, the Divisor. Thirdly, the Quotient. The Dividend is the Number given to be parted or divided. The Divisor is the Number given, by which the Dividend is divided: Or it is the Number which sheweth how many parts the Dividend is to be divided into, And the Quotient is the number produced by the Division of the two given Numbers, the one by the other.

So 12 being given to be divided by 3, or into three equal parts, the Quotient will be 4, for 3 is contained in 22 four times, where 12 is the Dividend, and 3 is the Dividen, and 4 is the Quotient.

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a crooked line at each end of it, and before the line at the left hand, place the Divisor, and behind that on the right hand, place the Figures of the

Quotient, as in the Margent, where it is required to divide 12 by 3 First I set

down 12 the Dividend, and on each fide of it do I draw a crooked line, and before that on the left hand do I place 2 the Divifor; then do I feek how often 3 is contained in 12, and because I find it 4 times, I put 4 behind the crooked line on the right hand of the

Dividend, denoting the Quotient.

4. But if when the Divisor is a fingle Figure, the Dividend confifteth of two or more places, then Chaving placed them for the Work as is before directed put a point under the first Figure on the left hand of the Dividend, provided it be bigger than (or equal to) the Divisor, but if it be lefter than the Divisor, then put a point under the second Figure from the left hand of the Dividend, which Figures as far as the point goeth from the left hand are to be reckoned by themselves, as if they had no dependance upon the other part of the Dividend, and for diffinction fake may be called the Dividual, then ask how often the Divifor is contained in the Dividual, placing the Anfwer in the Quotient; then multiply the Divisor by the Figure that you placed in the Quotient, and let the Product thereof under the Dividual; then draw line under that Product, and substract the faid Product from the Dividual, placing the remainder under the faid line, then put a point under the next Figure in the Dividend, on the right hand of that which you put the point before, and draw it down, placing it on the right hand of the Remainder, which you found by Substraction, which remainder with the faid figure an nexed before it, shall be a new Dividual; then feel again how often the Divisor is contained in this new Dividual; and put the Answer in the Quotient on the right hand of the Figure which you put there before then multiply the Divisor by the last Figure that you put al Garage by he ke he

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ut in the Quotient and fabferibe the Product mider he Dividual, and make Substraction, and to the Renainder draw down the next Digine from the going Dividend, (having first i point budeist yand put t on the right hand of the Remainder for a new thiidual as before, and proceed thus till the Work in finished. and the tild the which it will be in the

Observing this general Rule in all kinds of Division rfl-to-feck how often the dividor is contained in the ividual; then (having put the answer in the Quoent) multiply the divilor thereby rand substractithe reduct from the dividual in An Brampletor two buil ake the Rule plain. Let it be requireth to divide re directed, and as you feetin the Mary greed 812 ent, in order to the Work; then (because 76)2184(1 the divilor is more than a the first Hi-1 in of the dividend) I put a point ansarps rott r balle feword frigute, which makes as for the

vidual, then do I ask how often 6 the vilor is contained in a r, and because I not have it more than a times, t 2 in the Quotient, and thereby do I ultiply the divisor (6) and the product 18, which I fet in order under the didual, and substract it therefrom, and the

mainder (2) I place in order under the line, as you in the Margent. Then do I make a point under the xt Figure of the dividend being 8, and 6)2184(36 wit down, placing it before the Reinder 2, fo have I 38 for a new divi-O, sthert do b feek how often 6 is con- 11 11 02

chin allowand because I cannot have distinct re than diximes of Diput 6 and the Quas it updivid at, and thereby do I multiply the dior 6, and the product (36) I put under dividual (38) and Substract it therem, and the remainder 2 I put under the Line, as

fee in the Margent.

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Then do I put a point under the next (and laft) agure of the dividend (being q) and draw it down to the remainder 2, and putting 6 2184); it on the Right hand thereof, it put keth 24 for a new dividual; then II 1281 of feelt how offen 6 is contained in 24, and the Answer is 4, which I put in the quotient and multiply the Divisor (6) 36 thereby; and the product (24) I put under the dividual (24) and substract in the dividual (24) and substract in therefrom, hand the Remainder is of the contained in 2184 in the Quotient to be 264, I that in 6 is contained in 2184 being divided into 6 equal parts, 264 in one those parts.

Again, If it were required to divide 2646 by into 7 equal parts, the Quotient would be foun be 2781 as by the following Operation appeareth.

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of have it mere tishes tings, I was the Charlest, mere the Charlest, mere thereby do I that the distance of the content of the content of the charlest of the content of the charlest of the content of the charlest of the ch

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al, and libited it the places and the second and th

g. which I tet a oracegradat the die.

with drawn. Placing od sione and Ro-

So if it were required to divide out by 8, the tient will be found to be a 18, and a remaining Division is ended. The Work followeth and

Progue of the dividend in and conserved

and thereby no tracking the M.

L. and the product (26) I put under the grander to be greated to the re-

divioual (38) and fulliteach it there-

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signify multiply your D 4000, placeby your reign water and the same

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Many times the dividend cannot exactly be divided the divisor, but something will remain, as in the If Example, where 946 was given to be divided by 8, be quotient was 118 and there remaineth 2 after the livilion is ended. Now what is to be done in this lie with the Remainder, the Learner shall be taught then we come to treat of the reducing (or Reduction)

And here note that if after your Division is ended, ty thing do remain, it must be lesser than your divi-or, for otherwise your Work is not rightly performed. der une en elivis il

Other Examples are fuch as follow-

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5. But if the Divisor consistent of more places a one, then chule so many Figures from the left side the dividend for a dividual as there are figures in divisor, and put a point under the farthest Figure that Dividual to the Right hand, and seek how of the first Figure on the left side of the Divisor, contained in the first Figure on the left side of dividual, and place the Answer in the Quoties thereby multiply your Divisor, placing your wounder your dividual, and substract it therefore, cing the Remainder below the line; then put appunder the next Figure in the Dividend, and drawdown to the laid Remainder, and annex it on the ride thereof, which makes a new dividual, and process before, till the work is sinished.

And if it to happen that after you have choich a first dividual (as is before directed) you find it to lesser than the divisor, then put a point under a firmore near to the right hand, and seek how often first Figure on the lest side of the divisor in the two first Figures on the lest side of file divide and place the answer in the quotient, by which maply the divisor, and place the product thereof in der under the dividual, and substract it therefore

and proceed as before, she with an army

Always remembring, that (in all the cales of D fion) if after you have multiplyed your Divilor the Figure last placed in the Quotient, the product greater than the dividual, then you must cancel Figure in the Quotient, and instead thereof put a gure lesser by a Unit (or one) and multiply the D for thereby, and if still the product be greater the dividual, make the Figure in the quotient yet by a Unit; and thus do until your product be than the dividual, or at the most equal thereto, then make Substraction, 6%.

So if you would divide 9464 by 24, the quot will be tound to be 394. I first put down the p. Numbers, as before is directed in the third Rule:

Then I go on and make a point under the next and ft-Figure (4) in the Dividend, and draw it down to effemainder to, and it maketh 104, for a new vidual, which is also a Figure more than the Divisor, in therefore I seek how often two is contained, in a languer five times, but multiplying my Divisor, the product is 120, which is greater than the Di-lor, and therefore I make it but 4, and by it multiply the divisor, and the product is 96, which being plant under, and substracted from the dividual there reasneth 8, and thus the whole work of this Division coded, and I find that 9464 being divided by 24,

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or in 24 equal parts, is found to be 394, as was to before, and the Remainder is 8, as you fee in Work following.

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Another Example may be this, let there be require the quotient of 1183653 divided by 385, first 1 if spoke of the numbers in order to their 384)118264 dividing, and because 118 the three

first Figures of the dividend is lefter than the divisor 385, I therefore make a point under the fourth

how often 3 (the first Figure of the divisor) is contained in 11? The Answer is which I put in the Quotient, and thereby multiply Divisor 385, and the Product is 1153 which I fulbfin from the Dividual 1188, and there remains 28. Th

(as before) I draw down the next Figure, which is 6, and place it before the Remainder 28, fo have I 286 for a new dividual, and because it hath no

285) 1183653

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feek how often 3 (the first Figure in the divisor) contained in 2 (the first Figure of the dividual, the Answer is o, for a greater number cannot be o and thereby (according to the 5th Rule) I show

Ghaparia. nd of hoftracted from the dividual 286, the remainder sethe fame; wherefore I draw down the next Figure (5) from 385)1183653(307 tho dividend hand put it before and out out will the faid Nemainder alles to have 1990 1944 h 286 stor a new dividual, land not leading ers, (wz.) a place more than the divilor, I feek how often () (the 170 tained in 28 (the two first of the dividual) and I fay there is o times 2 in 28, but multiplying my whole divisor (284) thereby I find the product to be 3405, which is greater than the dividual 2865, wherefore I choose eight which is lesser by a Unit than nine, and thereby I multiply my divisor 385, and the product is 3080, which still is greater than the faid dividual, wherefore I choose another number yet a Unit letter, viz. 7; and having multiplyed my divisor thereby, the Product is 2695, which is Ieffer than the dividual 2865, wherefore I put 7 in the

Quotient, and Substract 2695 from the dividual 2865,

and there remains 170, then I draw down the last fi-gure (3) in the dividend, and place it before the said. Remainder 170, and it makes

(for the Reason abovesaid) I feek how often a is contained in 17, the answer is 5, but multiplying the Divifor thereby, the Product is (1925) greater than the dividual, wherefore I fay it will bear 4 (a Unit leffer) and by it I multiply the Divifor 285 and the Product is 1540, which is leffer than the dividual, and therefore I put 4 in the Quo-

1703 for a new dividual, then 385)1183653(3074.

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tient, and subfiract the faid Product from the dividual. and there remaineth 164, and thus the Work is finished, and I find that 1183633 being divided by 385, D.4

Divisionlos Chaps or into 38 sequal fhares or parts, the Quotient fo one of those parts) is goy 41 and besides there is to in the next Figure (s) from 284); reguinition And thus the Learner being well werfell in the thod of the foregoing Entrophs, he may be did ciently qualified for the dividing of any greater S or Number into as many parts as his pleafeth, that he may understand the method of dividing by a Dir for, which confifteth of 4 or 5, or 6, or any greate number of places, the method being the fame the foregoing Examples in every respect. If no had was tud , 3 Other Examples of Deution bas (laubi and the second state of th 275964

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So if you divide 47386473 by 58736, you will find the Quotient to be 800, and 45257 will remain after

the work is ended.

In like manner if you would divide 3846739204 by
483064 the Quotient will be 7963 and the Remainder

after Division will be 10057

Compendiums in Division.

I. If any given Number he to be divided by another number that hath Cyphers annexed on the right fide thereof, (omitting the Cyphers) you may cut off to many Figures from the right

hand of the Dividend, as there are Cyphers before the Divifor and let the Remaining Numbers in the Dividend, be divi-ded by the remaining humber or numbers in the Divisor, ob. Cla Mann cross in the Divisor, ob. Cla Mann cross in the Division is en-

Be If Divisor adju

ded any thing remain, you are to annex thereto, the number or numbers that were cut off from the divide and fuch new found number shall be the Remainder. As for Example! Let it be required to divide 45638 by 400; now 400)466 58(116 fore the Divisor, I car off as ma- 200 h at 1 1 10 ny Rights from before the Distantin harmon a vidend, biz. 58, to that then there it amail faint . 8 will remain only 466 to be divided by 4, and the Quotient will be 140, and there will remain 2, orth ion afternos to which I annex the two Figures to aska 24 s. 1.9 (48) which were cut of from the debute by grand true Roma Inder, forthat Econdiade A 2021

and 258 remainers after the Work is ended rus by the Work in the Margentino and to hory and so in

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a. And hence it followeth that if the Divilor be (1) or a Unit with Cyphers annexed, you may cut off fo many figures from before the dividend, as there are Cyphers in the Divisor. and then the figure or fi-

gures that are on the Left-hand, will be the Quotient, and those that are on the Right-hand will be the Remainder, after the Division is ended : As thus 45182 were to be divided by to, I cut off the laft Fi gure (3) with a dash thus (4578/3) and the work done, and the quotient is 4578 (the number on the left hand of the dash) and the Remainder is 3 (on the Right hand 5) in tike manner if the fame number 41782 were to be divided by roo, I cut off a Figure from the end thus (457)83) and the Quotient is 45 and the remainder is 82. And if I were to divide t fame by 1000, I cut off 3 Figures from the end th d the Quotient is 45, and 783 the Re mainder, car-

6. The General Effect of Division is contained the definition of the same (that is J by having two w equal numbers given to find a third number in fur proportion to the dividend, as the divisor hath to Un or 1, it also discovers what reason or proportion the is between numbers, to it you divide 12 by 4, it quot 2, which shews the reason or proportion of 4 to 12

triple.

The second Effect is by the superficial measure content, and the length of any Oblong, Rectangul Parallelogram, or fquare Plain known, to had out t breadth thereby, or contrariwife by having the fupe ficies; and breadth of the faid Figure, to find out t length thereof. Also by having the folidity and length of a Solid to find the Saperficies of the Bale of e con The third effect is, by the contents, reason, pro-

value, buying, felling, expences, wages, exchanginterest, profit or loss of any number of things (be Money, Morchandize, or what elfe. (to find out t contents, reason, price, value, buying, selling, ex-pence, wages, exchange, interest, profit or loss, of any one thing of like kind.

The fourth effect is to sid, to compose, and to make

other Rules, but principally the Rule of Proportion, called the Golden Rule, or Rule of Three, and the Reduction of Moneys, Weights, and Measures, of one denomination into another, by it also Fractions are abbreviated by finding a common measurer, unto the Numerator and Denominator, thereby discovering commensurable numbers.

If you divide the Value of any certain quantity, by the fame quantity, the quotient discovers the rate or value of the Integer, as if eight yards of Cloth coft 29 fhillings; if you divide (96) the value or price of the given quantity, by (8) the fame quantity, the quotient will be 128, which is the value or price of 1 of those yards. (7 contra.

If you divide the Value of Price of any unknown quantity, by the value of the Integer, it gives you in the Quotient that unknown quantity whole price is thus divided; as if to thillings were the value of a yard, I would know how many yards are worth 96 shillings: Here it you divide (96) the price or value of the unknown quantity, by (12) the rate of the Integer, or one yard, the quotient will be 8, which is the number of yards worth of ihillings.

Some Questions answered by Division may be these following.

Queft. 1. If 22 things coll 66 shillings, what will re furth thing cost; facir 2, inillings, for it you divide 66 by 17, the Quarrent is for the answer; for the 26 yandsor ells of my shing to bound or bod for 108 /. How much than I want of an be bought or fold for? Furth 27, for it will divide 108 to 18 yards the Quotient will be 2 to the office of the integral but of the integral of the integral of years amount to 868 I will it the Expence, Charges, or Wages of one years facts at the Expence, Charges, or Wages of one years facts at the Expence, Charges,

or Wages of one year? facil 124 ?. for if you divide:

Chap. \$68 (the Wages of 7 years) by 7 (the Number of years) the Quotient will be 124 for the Answer fee the Werk. ary one sign of the compact and a main other less that the compact and a main other less that are eightly the sale of Proportion, alled the Gold's Rule, or Rule of Three, and the seduction. I defect, where and Mean are stronger on are any other than the stronger on are any other than the stronger on are any other than the stronger of the stronger o ne denomination, are more to the it also to the second of the Namerators and as houstocking thereby differethe constraint of number of the constraint of th Pireft. 2. If the content of our Superficial Foot be rad Inches, and the breadth of a board be 9 inches, how many inches of that board in length will make fuch a foot * facilit 16 inches; for by dividing 144 (the number of fquare Inches in a fquare Foot, by 9 (the Inches in the breadth of the board) the Quotient is 14 for the number of Inches in length, of that board is make a superficial Foot. the state of the state of the state of the late of the late of the late of the late. ch er des fare, 'Il- quorent will be 8, which is the but or of yards world of things. Some Quellions anin cred by richmany be thefe following. thing coles in 2 I or theire Bucht. 4. If the content of an Acre of Ground be iso iquare Perches, and the length of a Furione (propounded) be as Perches, how many becomes will then go in breadth to make an Acro, later a Perches, form you divide 160 (the number of Perches in an Acro) by 80 (the length of the Furione in Perches) the Quotient is a Perches; and lo many in breadth of the Furlong will make an Acres 1150y one to asgrift a 838

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then the Levilon was to "ad," and "it to the Product, which is not to the Product, with the country to be account to the country to be considered.

Quelt. 5. If there be 893 Men to be made up into a battle, the Front confilts of 47 Men, what number mult there be in the File? Facil 19 deep in the File: For if you divide 893 (the number of men) by 47 (the number in Front) the Quotient will be 19 File in depth; the Work followeth;

47) 893 (19 deep in file

Quest. 6. There is a Table whose Superficial content is 72 feet, and the breadth of it at the end is 3 feet, now I demand what is the length of this Table? Facit 24 feet long; for if you divide 72 (the content of the Table in feet) by 3 (the breadth of it) the Quotient is 24 feet for the length thereof, which was required. See the Operation as followeth;

The Proof of Multiplication and Division.

multiplication and Division interchangeably prove each other; for if you would prove a Sum in Division, whether the Operation be right or no, Multiply,

the Quotient by the Divisor; and if any thing remain after the Division was ended, and it to the Product which Product (if your Sum was rightly divided) with be equal to the Division! And contrariwise, if you would prove a Sum in Multiplication, divide the Product by the Bushiplyer, and if the work was rightly performed, the Quotient will be equal to the Multiplicand. So the Example where the Work is done and undone Let 76:4 be given to be multiplied by 2242, the Product will be 248:4208 as by the Work appeareth.

153.08 3061.6 153.08 220.62

And then if you divide the faid Product 2481426 by 3242 the Multiplier, the Quorient will be 7634 equato the given Multiplicand.

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indiciplication and blotton interchangeaftly product others, for a repulsional discovered Same in Discovered the the Discovered Same in the Discovered Same in Discovered Same in the Di

Dividend.

In like manner (to prove a Sum of Number in Division). If 24814268 were divided by 3242 the Quotient would be found to be 7534; then for proof, if you multiply 7654 the Quotient by 3242 the Divisor, the Product will amount to 34814268, equal to the

Or you may prove the last or any other Example in Multiplication thus, viz. Divide the Product by the Multiplicand, and the Quotient will be equal to the Mul-

tiplyer. See the Work.

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charge the following the the if arrestes Did

From whence there assist this Corollary, that any operation in Drugon may be proved, by Drugon; fore if after your Drugon is ended, you divide the drugend by the Quotient, the new Quotient thence arising will be equal to the Drugor of the first operation; for tryal whereof, let the last Example be again repeated.

268 (7654 asm oli they bead one thor r). If 21812258 we Then for us out. at would be found to h register the Division no multiply Thea the Con-Product will among Sweet Tame on 1296 12968 For Proof whereof divide again 24814268 by the Quotient 7654, and the Quotient hence will be equite the first Divisor 3242; see the Work. 7654) 24814268 (3242 22962 18522 15208 30616 3308 13308

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But in proving Divition by Division, the Learner is to observe this following Caution, that if after his Division is ended there be any Remainder, before you gabout to prove your Work, substract that Remainder out of your Divinent, and then work as before, as a the following Example where it is required to divide 42376 by 765, the Ovortent here is 37, and the remainder is 277; fee the Work following.

ercof let tire last Example be again repeated.

765) 43876 (57

3824

5626

denies is the seekich burs together

enforce public and the contractions in the contractions in the contraction is or intervers to

Now to prove this Work substract the Remainder 271 out of the Dividend 43876 and there remaineth 43605 for a new dividend to be divided by the former Quotient 57, and the Quotient thence arising is 765, equal to the given Divijor, which proveth the Operation to be rightened and the provent of the contract of the cont

theoryeth as well as nothing in the property of which

17) 43605 (765 day

sales a least the D. Athan part alconding.

rober a Man or Mender of the control of into a Lifer, which doned and into a Lifer, which done on the more than it is forectable.

that income in value to the proper first given in the

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Thus have we gone through the four Species of Arithmetick, viz. Addition, Subfreection, Multiplication, and Division; apon appearance of the following of the f

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CHAP. VIII.

Transmitted the state of

Of Reduction.

I. D Eduction is that which brings together 2 or more numbers of different denominations is to one denomination; or it ferveth

Hills Arith. change or after Numbers, Money, Weigh Ch.rq. 192. Measure or Time, from one denomin tion to another; and likewife to abrid

Fractions to their lowest Terms. All which it do so precisely, that the first Proportion remaineth will out the least jot of Error or Wrong committed. So the it belongeth as well to Fractions as Integers, of which in its proper place. Reduction is generally performed either by Multiplication or Division; from when we may gather, that,

2. Reduction is either Defcending or Afcending.

2. Reduction Descending, is when it is required reduce a Sum or Number of a greater Denomination into a leffer; which Number, when it is fo reduce shall be equal in value to the number first given in the

greater Denomination; as if it were re Wing. Arith. quired to know how many fillings, pence or farthings are equal in value to an hu ch.7. 2,3,4. dred pounds? or how many ownces are col

tained in 45 hundred weight; or how many days, hours or minutes, there are in 240 Tears, Or . "And this kin of Reduction is generally performed by Multiplication

A. Reduction Ascending, is when it is Required Reduce or Bring a Sum or Number of a smaller Denom nation into a greater, which thall be equivalent to given number; as suppose it were required to fin out how many Pence, Shillings or Pounds are equin value to 42783 Parthings, or how many Hundre are equal to (or in) 3748 pounds, &c. and this kind a Redullion is always performed by Division.

into another Denomination, you are to confider whe

ther it ought to be relolved by the Rule delcending or afcending, viz. by Multiplication of Division: If it be to be performed by Multiplication, consider how many parts of the Denomination into which you would reduce it, are contained in a Unit or Integer of the given Number, and multiply the faid given number thereby, and the Product thereof will be the Answer to the Question. As if, the Question were, in 28 pounds, how many faillings? Here I confider, that in one pound are 20 shillings, and that the number of shillings in 28 pounds will be 20 times 28, wherefore I multiply 38 s. by 20, and that product is 760, and so

many fhillings are contained in 28 pounds, as in the

Margent.

tions between the Number given, and the Number required, you may (if you please) reduce it into the next interiour Denomination, and then into the next lower than that, Ge. until you have brought it into the Deno-mination required : As for Example, let it be demanded in 132 pounds how many farthings First, I multiply 132 (the Number of pounds given by 20 to bring it into pillings and it

multiply the (billings (2640) by 12, to bring them into pence, and it producerh 31680, and fo many pence are contained in 2640 faillings, or 132 points, then do I multiply the sence, viz. 21680

But when there is a Denomination, or Denomina-

2640 AN

by 4 to bring thereof to be 1267

6. And if the number propounded to be reduced, is to be divided, or wrought by the Rule Afcending,

Pedalion.

confider how many of the given numbers are equal to an Unit or Integer, in that denomination to which you would reduce your given number, and make that your Divides, and the given number your Dividend; and the Quotient thence arifine will be the number fought or reenired : As for Example, Let 15 very Mander lings into pounds, here I confider 20) 264 0 (132 that 20 shillings are equal to one pound, wherefore I divide 2640 (the given number) by 20, and the Quatient is 132, and fo many pounds are contained in 2540 hillings In Reduction descending and ascending the Learner is advised to take particular notice of the Tables delivered, inthe fecond Chapter of this Book, where he may be informed what. Multipliers or Disagors to make the of in the reducing of any Num-

ber to any other Denomination what sever, especially English Moneys Weights, Measures, Time and Motion; but in this place it is not convenient to meddle with Foreign Coyns, Weights, or Measures.

Foreign Coyns, Weights, or Meatures.

But if in Reduction Afcending it happen that there is a denomination or denominations between the number given, and the number required, then you may reduce your number given into the next Jupariour denomination, and when it is so reduced, being it into the next above that, and so on until you have brought it. into the Denomination required. As for Example,
Let it be demanded in 126720 farthings, how many

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pounds? First, I divide my given number (being furthings, by 4, to bring them into sence, (because 4 far-things make one penn) and they are 31680 pence, then I divide 21680 pence by 12, and the quotient giveth 2640 (hillings, and then I divide 2540 (hillings by 20, and the quotient giveth 132 pounds, which are equal in value to 126720 farthings. See the whole Work as it followeth.

1267	2001(3	2) 2080	20) (264)
12	San	1	ANA .
4-		MENDER NO.	Carried Street, Street
27,		48	1
3	1	(0)	a in
(0	N'ame	Star I	Same?

7. When the number given to be reduced, confileth of divers denomination, as points, fillings, pener and furthings, or of bundreds, quarters bounds and onces, 600 then you are to reduce the highest of greatest) denomination into the next inferious and add thereunto the number standing in that denomination which your greatest or highest number is reduced to it then reduce that Sum into the next inferious Denomination! adding theretoethe number standing in that denomination! adding theretoethe number standing in that denomination is do not if you have brought the number given into the denomination proposed. While I sumber given into the denomination, by multiplying it by 20, and the product is 950 shillings, to which I add the Is shillings, and they make a 15 shillings, to which I add the Is shillings into pence; and they make a 16 pence, to which liadd the is pence, and they make a 16 pence, to which liadd the is pence, and they make a 16 pence, to which liadd the is pence, and they make a 16 pence, to which liadd the is pence, and they make a 16 pence, to which liadd the is pence, and they make a 16 pence, to

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960 Millings

Sum 973 Shillings

1946 973

11676 pence

Add

Sum 11686 pence

s. If (in Reduction Ascending) after Division ended, any thing remain, such Remainder is of the Denomination with the Dividend.

Example. In 4783 farth. I demand how many pounds.

First, I divide the given number of Farthings, (vin 4783) by 4 to bring them into pense, and the Quotient is 1195 pense, and there remaineth a after the work of Division is ended, which is a farthings.

Again, I divide 1144 pense (the faid Opatient) by 12 to reduce them into failings, and the Quotient is 9 shillings, and there is a Remainder of 7, which is

pence.

And then I divide 99 shillings (the last Quotient) by 20, to bring it into pounds, and the Quotient is 4 l. and there remaineth 19 shillings: so that I conclude the in 4783 (the proposed number of farthings) there is a pounds, 19 fhillings, 7 pences 3 farthings, view the following Operation.

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97	nick born	15 (19) Shilling	5
4	1	9		1
31	Bem.	(7) pense		. 1
3	THE NEW	and the second		
3 / a 15		1.	s. d.	grs.
3.4	Course	acit O4-	10-07-	-02

Remains (3) farthings

Mere Examples in Reduction of Coins

shi the first with a many fillings of Last the many fillings of Last top fillings, for by multiplying 438 by 200 the Foods amounteth to so much, see the Work.

438 pounds

Facit 8760 fbillings

Quest. 2. In 467 l. how many Pence? First, multiply the given number of punds (467) by 20 to bring it into shillings, and it makes 19340 shillings, then multiply the shillings by 12, and it produceth 112080 pence, thus,

467 pounds

9340 Shillings

Pact sactor

Or this Question rughe lave been thus resolved, with Multiply 5673 (the given symbols of panals) by 950 (the number of farthmosds towns) and it produced the same filed, as you open fee by the Work.

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Or it may be resolved thus, viz. multiply the give number of pounds (467) by (1240) the number of pendin a pound, and the Product is the same, viz. 1120% sence, as by the Operation appeareth.

> 11467 pounds (19) flittings 101240 cons (+) 18696 934 ----- Pacit 112080 pence

Queft. 3. In 5673 1. how many farthings ? Firt Multiply the given number by 40, to bring it into shillings, and it produceth 113460 shillings, then multiply that produced by 12, to bring it into pence, and it produceth #361520 pence; then laftly, multiply the by A and it productly 44 60 lot farthings. So mounted to so that the tree to the thork.

Auft jennas

113460 Shillings

Quelt' . In 457 l. best many Pence : cirft, multithe give member of peeds (467) by 20 to bring it go hillings, and it maled sout hillings, then multithe the thillings by in, and it produceth rines pence, 1361520 pence

or pounds

Facit 5446080 farthings

Or this Question might have been thus resolved viz. Multiply \$673 (the given number of pounds) by 960 (the number of farthing cist a pound) and it produceth the fame Effect, as you may fee by the Work.

Facil Macolo Pink

5673

5673 pounds	20 sbillings
340380, 51057	240 pence 4
\$446080 farthings	960 farthing

Otherwise thus: First bring the given number 5673 le to shillings, and multiply the shillings by 48, the unber of farthings in a shilling, and the same Effect is creby likewise produced, viz.

5673	pounds	12 pence
113460	Millings	48 farth.
907680 543840		
A CONTRACTOR OF THE PARTY OF TH	E NA	

These various ways of Operating are expressed to inm the Judgment of the Learner, with the Reason of Rule, more ways may be shown, but these are suffint even for the meanest Capacities.

Quest. 4. In 458 1. 16 s. 7 d. 3 qrs. how many jarys. To Resolve this Question consider the seventh le of this Chapter, and work as you are there dited, and you will find the aforesaid given number amount to 440479 farthings, viz.

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1. d qrs.
458—16—07—3
20
9160 shillings
Add 16
Sum 9176 shillings
12
18352
9176
210112 pence
Add 07
Sum 11019 pence
4
440476 sarthings
Add 3
Sum 440479 farthings.

This last Question (or any other of this kind, where the number given to be reduced consistent veral Denominations) may be more consistent thus, viz. when you multiply the pounds by 20 bring them into shillings, to the product of the Figure, add the Figure standing in the place of in the Denomination of shillings, but because the Figure in the Multiplier is (o) I say o times the string, but 6 is 6, which I put down for the singure in the product, then because this Multiplier I go on no surther with it, for if I should, the Product would be 0, but proceed, and when I to multiply by the second Figure in the Multiplier to the Product of it, I add the Figure standing place of Tens in the Denomination of shillings

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(1) faying 2 times 8 is 16, and (the faid Figure) 1 is 17, then I fee down 7, and carry a Unit to the Product of the next Pigure, as is directed in the fifth Rule of the fixth Chapter foregoing; and finish the Work. So that you now have the whole Product and Sum of Millings at one operation, which is the fame as before, and when you multiply the skillings by 12, to bring them into pence (after the fame manner) add to the Product the number standing in the denomination of pence, and to when you multiply the pence by 4 to ber standing under the Denominations of Farthings. the last Question thus wrought.

Facit 440479 farthinge

After the Method last prescribed (which if Rightly onfidered, differeth not any thing from the 7th. Rule of this Chapter) are all the following Examples that re of the fame nature wrought and refolved.

Quell. S. In 4375866 Farthings, I demand how ma-Pounds, Shillings, Pence, and Farthings?

To resolve this Question; First, I divide the given number of Farthings by 4, and the Quotient is 1993966 nded, (which by the 8th Rule foregoing) is two Farhings; then I divide ro93966 Pence by 12 and the Quotient

Quotient is 91163 Shillings, and there remaineth after Division, which by the faid 8th. Rule is so ma Pence, viz. 10 d. then I divide 91163 Shillings 20, and the Quotient is 4558 l. and there cemaine 3 Shillings; so the work is sinished, and I find that 4375866 Farthings there are 4558 l. 03 s. 10 d. 24 See the Operation,

4) 4375866	(1093966 (24. 图 加罗亚·周
37 36 5	13 12 12 19	11 10
38 36	76 72	16 16
26 24 26	(10) pe	(03) Shillings
(2) for 1.		d. 98

Quest. 6. In 4386 L. I demand how many Grot To Resolve this Question, I reduce the given mober of Pounds into Shillings, and they are 877 Shillings, now I consider that in a Shilling are 3 Grot therefore I multiply the Shillings by 3, and it proceth 263 160 Groats. See the Work.

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pic Qo 4386 pounds 20 20 87720 fbillings

Facit 263160 greats

This Question might have been otherwise resolved thus, viz. considering that in a Pound (or 20 Shillings) here are 2 times 20 Groats, which make 60, by which I multiply the number of Pounds given, and it produceth the same Effect at one Operation, as followeth.

4386 pounds 20 s. 3

Facit 263160 greats in 4386 l. 60

Quest. 7. In 43758 three Pences, I defire to know

now many Pounds?

To refolve this (and many fuch like) Question; First, divide my given number of Pences by 4, because 4 three Pences are in a Shilling; and the Quotient is 10939 shillings; and there remaineth 2 after Division is ended, which is 2 three Pences (by the 8th. Rule of this Chapter) which are equal in value to 6 d. then I divide 10939 Shillings by 20; and the quote giveth 546 l. and 19 s. Remain; so that I conclude in 43758 pieces of three pence per piece, there are 546 l. 19 s. 26 d. as by the Work appeareth.

43758 (1093|9 (546—1
4 10
37 9
36 8
15 13
12 12
38 19 (billings

vh

.(2) three pences, or 6 d.

36

This Question might have been otherwise Resolve thus, viz. first multiply the given Number of thus pences 43758, by three the Number of pence in the pence, and the product (viz. 131274) is the Number of pence equal to the given Number of three pences which number of pence may be brought into pound by dividing by 12 and by 20, and the Quotient you will find to be equal to the former work, viz. 3461 195.6 d.

43758 3 2 0 1. s. d. 12) 131274 (1093|9 (546—19—06

12		10
	12	•
U	08	8
4	7	13
	6	12

114 rem. (19) shillings.

Or thus, divide the given Number of 3 pences by be number of 3 pences in a pound or 20 shillings which you will find to be 80, if you multiply 20 s. y, 4, the number of three pences in a shilling) and ou will find the quote to be \$46 l. as before, and a semainder of 78 three pences, and if you divide those 8 three pences by 4, (because there are 4 three pences in a shilling) were will find the quote to be 10. pes in a shilling) you will find the quote to be 19 s. and 2 three pences Remain, which are equal to 6 d. which is the same that was before found:

(A.).		, Se	d.
8 0)	4375 8 (54	6-19-	00
	37		
	32	a C 1	700
	48 5.		17.
1000	4		
	38		
		ee pences	or 6 de

Quest. 8. In 4784 l. 13 s. how many pieces of 131d. per piece?

This Question cannot be resolved by Reduction, defeending, or afcending, absolutely, because 131d. is no even part of a pound) but rather by them both jointly, viz. by Multiplication and Division; for if you bring the number given into half pence, and divide the half pence, by the half pence in 13 d. viz. a7, the quotient will be the Answer; for having brought

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brought 4785 l. 135. into half pence, I find it may 2297112, which I divide by 27, (because there as so many half-pence in 131d.) and the quote gives 85078 pieces of 131d. and 6 half pence remain on and above; observe the work following.

1. 4785 20	-13	Sur (c)	d. 134 2		
95713	shillings half-pence in	a shilling	27 b	alf-pens	
82852	113			CIE.	1000

2297112 half-pence in the given number.

27) 2297112 (85078 pieces of 133

216	
137	e)) ((),
211	Çe .
222	Test (s)

Remain (6) half-pence

It would have produced the fame aniwer if you had reduced your given number into farthings, and divided by the farthings in 13.4. viz. 54. (for always the Dividend and the Dividor must be of one Denomination) and then you would have had a Remainder of 12 farthings, which are equal in value to the former Remainder of 6 half-pence, as you may prove at your leifure.

Quest. 9

Queft. 9. In 540 Dollars at 4 s. 4 d. per Dollar how

many pounds feeling?

First, Ering your given Number of Dollars into Pence, and then your Pence into Pounds according to the former Directions. Thus in 43. 4 d. (viz. a Dollar) you will find 52 pence, by which multiply 540 Dollars, and it produced 28080 pence, which if you divide by 240 (the pence in one pounds) the quotient will give you 1471. which are equal in value to 540 dollars, at 45. 4d. per dollar observe the Operation.

The same of the sa	s. d.
540	- 4-4
-3-	
1080	52 pence
2700	(c)
24 0) 28 8 0	(117
7,30	CONTRACTOR DE 1011 MAINTE
24	the three of the work in rock
Figure 1978	M AND AND ONE HE CAME
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Months A Control	recognise is a colory and selection
168	in a product if you alvied because in a fulfilling) and in a fulfilling) and in a fulfilling).
168	e miles 10253 l. c9 c. g d.
(0)	

The foregoing Question might have been otherwise wrought, thus, viz. Multiply (540) your given number of Dollars, by 13 the number of Groats in a Dollar (or 45. 4d.) and it produceth 7020 groats, which divide by 60 (the groats in 1 pound or 20 shillings) and the quote is 117 L as before. See the Work.

Chap

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30	540			4
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1	1620	7354	A LE	3
id.	and the second	· /-	I	36
-	540		44	et:
.10	702 0	(TT))
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V. 2	O.	100	hon. A	1
	10	100		-
10.30	6	100		Mi.
		1 40		3
- 4	42			
	42		100	7
		.150	20	4.3

Quest. 10. In \$47386 pieces of 4 d. per piece, demand how many Pounds, Shillings, and Pence?

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color C. anight passed into each cherville is a set of baltiple (a.) your, even near a set of baltiple (a.) your, even near a set, by the limit of a color of the color of t

First, Bring your given number of four pence half penies all into half-pence, which you will do if yo multiply by 9 the number of half-pence in 4 1d. an the product is 4926474 half-pence, which are brough into pounds, if you divide them by 24 (the half-pence in a shilling) and 20 (the shillings in a pound it makes 10263 L 09 s. 9 d. as by the Work.

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	547386 9	-		d. 4 1 2	
24)		2 0) (20526) 9 (1026)	9 half	penoe
	48 126 122	05		31	
+	64 48	12 12 f	l. acit 1020	53-09-	d. 5
	167 144	6 6 (09) 1	hilling a		
	216	(09)]		1. A	-1

Rem. (18) half pence or 9 d.

Quest. 11. In 4386 L. I demand how many pieces of 6 d. of 4 d. and of 2 d. of each an equal Number? that is to say, what Number of Six pences, Groats, and two pences, will make up 4386 L. and the Number of

each equal?

The way to refolve questions of this Nature, is to add the several pieces (into which the given Number is to be brought) into one Sum, and to reduce the given Number into the same denomination with their Sum, and to divide the said given Number (so Reduced) by the said Sum, and the Quotient will give you the exact Number of each piece. And after the same Method will we proceed to Resolve the present Question, viz.

So that I conclude by the operation that \$7720 fix pences, and \$7720 groats, and \$7720 two pences are just as much as (or equal to) 4386 l. or if you admit of 5 s. to be thus divided, it is equal to 5 fix pences, and 5 four pences or Groats, and 5 two pences. For if two Right lines (or two Numbers) be given, and one of them be divided into as many Parts, or Segments as you please, the Restangle (or Produst) comprehended under the two whole Right lines (or numbers given) shall be equal to all the Restangles (or Produsts) contained under the whole line (or Number) and the several Segments (or Parts) into which the other line (or Number) is divided, Euch. 2. 1.

Another Question of the same Nature with the

last may be this following, viz.

Queft. 12. A Merchant is defirous to Change 148 h into pieces of 13 $d^{\frac{1}{2}}$, of 12 d, of 9 d, of 6 d, and of 4 d; and he will have of each fort an equal Number of pieces, I defire to know the number?

Do as you were taught in the last question, vizadd the several pieces together, and reduce the Sum.

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into half-pence, then reduce the Sum to be changed, viz. 148 Linto the same denomination, and divide the greater by the seller, and in the Quotient you will and the Answer, viz. 798 is the Number of each of the pieces required, and 18 remaineth, which is 18 half-pence by the 8th. Rule of this Chapter. See the work as followeth.

1	1000			
148	A. D. W. S.	Kyun ka	13 -	Salt in Co
240 P	ence in a l.		12	
5920		· · · · · · · · · · · · · · · · · · ·		400
296			OR OF	
35520 P	ence in 148 l		Sun 44	
. 2			2 -	
71040 h	alf pence	de ding lan	89 ha	lf-pence
		The Bridge	The State of the s	The same of

89) 71040 (798 pieces of each fore

A carlo Laura A Thire of South

874 801 730

Remain (18) balf-pence

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The truth of the two foregoing Operations will thus be proved, viz. multiply the Answer by the parts, or pieces into which the given Number was reduced, and having added the several Products together, if their Sum be equal to the given Number, the Answer is Right, otherwise not.

So the Answer to the 11th. Question was 87720,

which is proved as followeth, viz.

Six-pences make 2193 87740 Four-pences make 1462 Two pences make 731

The total Sum of them 4386 which me

The Answer to the 12th. Question was 798, and 18 half pence remained after the Work was ended, now the truth of the work may be proved as the forms was, wiz.

Pieces of 12 make—44—17—99
Pieces of 12 make—39—18—90
Pieces of 9 make—29—18—66
Pieces of 6 make—19—19—00
Pieces of 4 make—12—06—00

The Total Sum of them 148-00-00

which Total Sum is equal to the Number that was fell given to be changed, and therefore the Operation was rightly performed.

Reduction of Troy-weight.

We come now to give the Learner some Example in Iroy-weight, wherein we shall be brief, having given so large a Taste of Redustion in the foregoing Examples of Coyn, and now the Learner must be mindful of the Table of Iroy-weight delivered in the second Chapter of this Book.

Queft. 13. In 482 L 07 02. 13 p. w. 21 gr. how ma

fry Grains ?

Multiply by 12, by 20, and by 24, faking in the Figures standing in the several denominations, according to the Direction given in the 7th. Rule of this Chapter, and you will find the Product to be 2780013 Grains, which is the Number required, or Answer to the Question. See the whole work as followeth.

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eng fod	480	07 - 13 - 2	Ending had	TOTAL P
Amout 6	-		to regularization	
100	971	1.000		in the Control
	5791 0	nces		
hero and	20			18.0
	115833 P	enny meight		A TO THE
101 3 21 1	24			
hard or	463333			
Bacit :	2780013 8	rains		
Quelt.	14. In 278	DOI 2 grains	4 demand he	w many
rounas, t	Junes Echi	IY-SV CIETICS,	dud Otating t	The state of the s
This is refolved	but the for	egoing Que	tion inverted	, and is
This is refolved	but the for by dividing 5 482 L 07	oz. 13 p.w.	and Grains ? (tion inverted, and by 12, 21 gr.	l, and is and the
This is refolved Answer it	5 482 1. 07	2 0)	and by 12, and by 12, 21 gr. 12) l. (5791 (48:	
ADIWEF E	5 482 1. 07	2 0)	21 gr. 12) l.	
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Quest. 75. A Merchant sent to a Goldsmith 15 Ingob of Silver each containing in weight 2 l. 4 oz. and ordered it to be made into Bowls of 2 l. 8 oz. per Bowl and Tankards of 1 l. 6 oz. per piece, and Salts of 10 oz. 10 p.w. per Salt, and Spoons of 1 oz. 16 p.w.per Spoon, and of each an equal number, I desire to know how

many of each fort he must make?

This Question is of the same Nature with the in and 12 Questions foregoing, and may be answered after the same Method, viz. First, add the weight of the several Vessels (into which the Silver is to be made into one Sum, and reduce it to one Denomination and they make 1248 penny weights; then reduce the weight of the Ingot into the same denomination, viz. penny weights, (and it makes 560 penny weights) and multiply them by the Number of Ingots, viz. 16, and the product will give you the weight of the 16 Ingots, viz. 8960, then divide this product by the weight of the Vessels, viz. 1248, and the Quotient giveth you the Answer to the Question, viz. 7, and 224 p.w. remaining over and above.

1. oz.	1. or. p.w. 2-08-00
12	1-06-00
28. 20	0-10-10
	Sum 5-02-08
560 penny weights 16 Ingots	62
3360 560	20
22 - 2 - 2	1248 p.weights
1248) 8960 (7 Vessels of each 8736	
Rem. (224) penny weights	

with the day

The Proof of the Work is as followeth, viz.

(Bowls of 2 08 00 per Bowl to 18 08-Tank, of 1-06-00 per Tank is 10-06-00 Salts of 0-10-10 per Salt is 66-01-10 Spoons of 0-01-18 per Spoon is 01-11-04

224 penny weight remaining is 00-11-04

Total Sum 27-04-00

So that you fee the Sum of the Weights of each Veffel, together with the Remainder is 27 1. 4 02. thich is equal to the Weight of the 16 Ingots deliveed. For if 37 1. 04 ez, be reduced to Penny Weights. t makes 8960.

Reduction of Averdupois Weight.

In Reducing Averdupois weight, the Learner must ave Recourse to the Table of Averdupois weight deliered in the ad. Chapter foregoing.

Quest. 16. In 47 C. 1 gr. 20 A how many Ounces? Multiply by 4, by 28, and by 16, and the last Pro-uct will be the Answer, viz. 84992 Onnces.

C. qrs. -I-20 LANGER & STORE AND ASSESSED

189 quarters

1412 280

of aprile being &

5312 1. 16

31872 5312

Facit 84992 ounces

Queft.

LY DEBUTE LIP

cn

Queft. 17. In 84992 Ounces, I demand how man

C. qrs. b 02.

This is the foregoing Question Inverted, and wi he Resolved if you divide by 16, by 28, and by and the Answer is 47 6. 1 gr. 20 L equal to the give Number in the foregoing Question.

Quest. 18. A Chapman buyeth of a Grocer 4C. In 141. of Pepper, and ordered it to be made up in Parcels of 141. of 121. of 81. of 61. and of 21 and of each Parcel an equal number, now I would know the number of each parcel.

This Example is of the fame nature with the n and 12, and 15 Questions foregoing, and after to fame manner is refolved. See the Operation as for

loweth.

	Reda	Elion.	1.	19
			AL La	
77	4		2	
* 140 35		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	* 42	Soruça
42)490(11				
42 70 F40	it za parc	els of eas		
42 Rem. (28) pos				
mente (mo) box				

Reduction of Liquid Measure.

Quest. 19. In 45 Tun of Wine, how many Gallons ? Multiply by 4, and by 63 the product is 11350 Galons for the Answer.

> E80 1080

Racil 11340 gallons

Queft. 20. In 34 Rundlets of Wine, each containing

8 Gallons, I demand how many Hogsheads?
First, Find how many Gallons is in the 34 Rundlets, which you may do if you multiply 34 by 18, the content of a Rundlet, and the Product is 612 Gallons, which 567

63) 612 (9 Hbds.

Remain (45) gallons

facit 9 Hhds 45 galla

Quest. 21. In 12 Tun how many Rundlets of a

Reduce your Tuns into Gallons, and divide them 14, the Gallons in a Rundlet, and the Quotient (21) is your Answer. See the Work following.

14) 3024 (216 rund).

(o) facit 216 rundlets

Reduction

6

t

n

Reduction of Long Meafure.

Queft. 22. I demand how many Furlongs, Poles, Inthes and Barley Corns will reach from London to Tork, it being accounted an 151 Miles?

> 151 miles 8 furlongs in a mile

1208 fierlengs 40 poles in a furlong

48320 poles 11 balf yards

48320

531520 balf yards 18 inches in balf a yard

4252160

9567360 inches 3 barley carns in an inch

Facit 28702080 barley corns in 151 miles.

Quest. 23. The Circumference of the Earth (as all other Circles are) is divided into 360 Degrees, and each degree into 60 Minutes, which (upon the Superficies of the Earth) are equal to 60 miles; now I demand how many Miles, Furlongs, Perches, Yards, Feet, and Barley-Corns will reach round the Globe of the Earth?

360 degrees 60 minutes or miles to a degree

21600 miles about the Eurob 8 furlongs in a mile

172800 furlongs about the Earth 40 perches in a furlongs

6912000 poles or perches about the Earth
11 half yards in a perch

6912000

2) 76032000 half yards about the Earth

(38016000 yards, viz. the half yards
3 divided by 2.

114048000 feet about the Earth 12 inches in a foot

228096000

1368 576000 inches about the Earth
3 barly-corns in an inch

facit 4105728000 barly-corns.

And so many will reach round the World, the who being 21600 Miles, so that if any Person were to Round, and go 15 Miles every Day, he would go t whole Circumference in 1440 Days which is 3 Yes 11 Mouths, and 15 Days. 1

1

Reduction of Time.

Queft: 24. In 28 Years, 24 Weeks, 4 Days, 16 Hours, 20 Minutes, you many Minutes?

years weeks days hours min. 28 24 4 16 30 92 Weeks in a year.

60

143

1489 Weeks

1

10364 Days

41461

20729

248752 Hours

14925150 minutes

Note, That in Resolving the last Question after the Method expressed, there is lost in every year 30 Hours, for the Year consistett of 365 Days and 6 Hours, but by multiplying the Years by 52 Weeks, which is but 364 Days; You lose 1 Day and 6 Hours every Year, wherefore to find an exact Answer, bring the odd Weeks, Days, and Hours into Hours, and then multiply the Years by the Number of Hours in a Year, viz. 8766, and to the Product add the Hours contained in the odd time, and you have the exact time in hours, which bring into Minutes as before. See the last Question thus resolved.

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neeks days bours

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	Charles and a		and the same of
	days, b	TAX RESERVE AND RE	2
28	305	6 14 1 C	141
8766	24	500	A STATE OF THE STA
	-	69	4
172	1466	34	AND THE PARTY OF T
	A CONTRACTOR OF THE PARTY OF TH	Sept.	The second secon
172	730		
197	Transmitted		4 bours
228	8766	ours in a y	ear -
		STEEL AND	A11-1
249592 bours			
249592 40013		2 2 1 1 1	
00			

14975520 Minutes in 28 years and 4144 bours.

So you fee that according to the Method first up to resolve this Question, the Hours contained in a given time are 248752, but according to the last, but or true Method, they are 249592 which exceeds a former by 840 hours.

But for most occasions it will be sufficient to me tiply the given years by 365, and to the Product at the days in the odd time, if there be any, and the there will be only a loss of 6 hours in every years which may be supplied by taking a fourth part of a given years, and adding it to the contained days, at you have your defire.

Quest. 29. In 438657540 Minutes, how many years Facis 834 years, 4 dayes, 19 bours.

and them immissing the Years by the Number of House in a Year, sign 8769, and to the Product add the Boyrs contained in the odd time, and you have the Ports time in laters, which being into Minutes as in-

	Reda			3
Marcolo at Pis	1540 (721	6) JEA.	days	Mol.
60) 43865	de Thomas	18 5 VOW	An Max	ard all
of 1 190 100 2 181 no	al all 29	oregades at 8	efficas i	I' Ou
	SERVICE CO.	144	79V9	TOTAL COLUMN
in A state of the	2 1418- 311	1064	Children ?	The made
sciffuhali-	mini 24)	115 (4	annight.	E Eccelly
mi lo 254.		ba g6 th co	a botton in holita	not rec
102 Milliant 201 L	Rem.	(19) DOWY.	A TOURS OF THE PERSON NAMED IN	10年中に
15 p. 114 54 9	Tribel pell 12	ide Dosposite	q and Mi	CPMC
Hillian Soul aid	-riting and in	mar Associat	dien were	Admini.
Queft. 26. I nutes it is fin	ce the burti	of our Sav	10ur elu	s Christ
this present y This Question	ear, being	accounted fame natur	with th	e 24th.
regoing and a ultiply the giv 0 is 1470058	en number	of years by	8766, t	he pro-
ct is 8820349	20 Minutes	. See the	work.	ie bio-
MARKET F. L. L. C. CONT.	8766 bours	- Carlotte Carlotte Carlotte		
100 to	062 010	tive Anti	ompired as of Ne	0/10
ioda Jedar	g dallogi.	Diza evit	mana() F	
the restauration	. Drive Charge	in a form was		
165 I. day	REPORT SERVICE CO.	48 53 562 3 45 45 5	Bulletin - Th	PERSON E
8820	34920 minu	tes in 1677	years	Note

Note that as Multiplication and Division do in changeably prove each other, to Reduction Descendand Ascending, prove each other by Inverting Question, as the 13 and 14 and likewise the 16 17 Questions foregoing, by Inversion, do in changeably prove each other, the like may be formed for the proof of any Question in Reduction whatsoever.

Thus far have we discoursed concerning single Ar metick, whose Nature and Parts are defined in fecond, eighth, winth, and tenth definitions of third Chapter of this Book, for although Beduchi not reckoned or defined among the parts of fi Arithmetick, yet confidered Abstractly, it is the pr effect of Multiplication and Division; and as for extraction of Roots (which ought to be handled the next place as parts of fingle Arithmetick) wel omit it in this place, and refer the Learner to Mr.Co Decimal Arithmetick, which is (with great care pains) now published, together with his Logarith tical Arithmetick, shewing the Genesis or Fab metick, erc. As also his Algebraical Arithmetic taining the Dectrine of composing and resolv Equation, with all other Rules necessary for the derstanding of that Mysterious Art, go.

CHAP IX.

820aus 20. Minutes

Of Comparative Arithmetick, viz. The l

are confidered to have relation one to Bostius another, and this confide either in lib. 1. ca.

a. Rei

a Relation of Numbers in Quantity, is the Reference or Respect, that the Numbers pentelves have one to another, Vide Wing. A there the Terms or Numbers pro-visit. cap. 34.

ounded are alwayes two, the first saled the Antecedent, and the other the Confequent. The Relation of Numbers in Quantity confifts in Differences, or in the rate or reason that is found betwixe the Terms propounded, the difference of two Numbers being the Remainer found by Substraction, but the rate or reason

by Subfraction, but the late of received mat. lib. 2.cap.
betwist two Nambers is the Quotient mat. lib. 2.cap.
of the Antecedent divided by the Con-Alfted, Mathemat lib. 2.cap.

fement. So 21 and 7 being given, but the rate of reason that is betwint 21 and 7 will be ound to be triple reason, for 21 divided by 7 quotes the reason or rate.

4. The relation of Numbers in Quality, (otherwise called Proportion) is the Reference or Respect that he Reason of Numbers have one unto another ; there-

han two. Now this Proportion of Affed, math. another, is either Arithmetical, or Geometrical.

s. Arithmetical Proportion (by fome called Pro-reffior) is when divers Numbers differ one from anoher by equal Reafon, that is, have equal differences.

So fills Rank of Numbers, 3, 5, 7, 9, 71, 73, 19, 17, iffer by equal Reafon, vir. by 2, as you may prove.

2. In a Rank of Numbers that differ by Arithmeti-

Proportion, the furn of the first and hast term, bemultiplyed by half the Number of Terms, the protable total function all the Terms.

Of the fotal function all the Terms, the product
of multiply the number of the Terms by the
function of the first and last Terms, the product
reof will be the total function given, and 17 is 20,
ich multiplied by a (wie half the number of Terms)
ich multiplied by a (wie half the number of Terms)
the

the product gives 80, the fum of all the Terms multiply 8 (the Number of Terms) by 10 (half fum of the first and last Berms) the product gives

as before.

So alfo 21, 18, 15, 12, 0, 6, 3, being given, furn of all the Terms will be found to be 84; for ! the Number of Terms, is 7, and the fum of the and last (viz. 21 and 3) is 24, half whereof, (viz. multiplyed by 7 produceth 84; the fum of the Te fought.

7. Three Numbers that differ by Arithmetical portion, the double of the mean (or middle num

is equal to the fum of the Extreams.
So 19, 12, and 15 being given, the double of mean, 12 (viz. 24) is equal to the fum of the Extre

g and Is

8. Four Numbers that differ by Arithmetical P. portion (either continued or interrupted) the fun the two Means is equal to the fum of the two

So 9, 12, 18, 21, being given, the fum of 12 and 18 will be equal to the Vide Win fum of 9 and 21, viz. 30; allo 6, 8, rab, cap. 14, 16, being given, the fum of 8 and

14, is equal to the fum of 6 and 16, viz. 22, GG. 9. Geometrical Proportion (by some called Geo

trical Progreffion) is when divers numbers differ cording to like Reafon.

So 1, 2, 4,8, 16, 32,64, ore. differ by double fon, and 3, 9, 27, 81, 242, 729, differ by triple fon, 4, 16, 64, 236, Gc. differ by quadruple

10. In any numbers that, increase by Geomet proportion, if you multiply the last berm by the stient of any one of the terms divided by another the Terms, which being less is next unto it, and had deducted, or substracted, the first Term out of Product, divide the remainder by a number that unit, less than the faid Quotient, the last quote give you the fum of all the Terms.

The state of the s	
Care of ST.	
Cup, 90 of Numbers.	IOI
So.1, 2, 4, 8, 16, 32, 64, being even first I take one of the Terms, 2, 8, and divide it by the Term	(4) 8 (2 MA
eiven, first I take one of the Terms	12 (2) 8 75 1A
THE SHARE THE LAND SHARE THE STATE OF THE ST	is e viet (songin
tich is befored next to the Term	1281 16 hupe at
which is less and next to it, (viz-	From Sence at
by A) and the Quotient is 2, by which multiply the last term 64,	and the second s
which I multiply the last term 64,	tion, walch for t
and the Product is 128 from whence	1) 127 (127
(fubstract the first term (viz. 1.)	
the Bemainder is 127, which divided	he the Quetlent
a made less ber a fair a Vale anda in	by the Quotient
a made less by 1 (viz. 1.) the quote is	127, for the luin
of all the given terms, as by the World	in the Margent.
So if 4, 16, 64, 256, 1024, wer	re given, the fum
of all the famus will be found to be	2
1634. Forfirst, I divide 64 one of	1024
the terms by his next leffer term	16) 64 (4
he terms by his next leffer term, and the Quotient is 4, by which I	T. THE PARTY OF
and the Shotlent is 4, by which I	madal a de de
multiply the last term 1024, and it	4095
producath 4096; from whence I	4.
noducath 4096; from whence I abstract the first term 4, and the terminater is 4092, which I divide	314 140 E1113 EN 186
demainder is 4092, which I divide	2)4002(1251
w the quote less I (wir. 2.) and the	mansi and the toral
by the quote less i (viz. 3.) and the mote is 1364, for the torn sum of all	I the Terms, as
er Margente	statistic 180 de la
to the carriered by the said and an army at the	fell cossessib è
So likewife if 2, 6, 18, 54, 162,	486
too, were given the Sum or Potal	6) 18 (3
of all the Terms will be found to	The state of the same of the
oc 728. See the Work.	1448
11. Three Geometrical Propor-	. M. Q .O
be 728. See the Work. 11. Three Geometrical Propor- tionals given, the Square of the	at odt at bouser
Man it could be the Barrier	TO NO COURT A
Mean is equal to the Rettangle, or product of the Extreams.	2) 1450 1729
rounce of the Extreams.	come can elsent on
So 8, 16, 32 being given, the Squar	re of the Mean,
W. 16 15 2 ch. which is equal to the	Drodge of the
extreams 8 and 22, for 8 times 22 is	coual to 246.
12. Of A Geometrical Proportional	numbers alven
he Product of the two Means is account	ed che Bendung
the two Extractions is equal	to the Froduct
Tatreams 8 and 32, for 8 times 32 is 12. Of 4 Geometrical Proportional the Product of the two Means is equal of the two Extreams.	Juverle Lake
med of the two Means, viz. 16 times 2	2. which 15 < 12
equal to 8 times 64, the product of	the Extreams.
	Alfo
ward .	Allo

Anguoi,

Allb if 3, 9, 21, 69, were given (which are in rupted) I say 9 times 21 is equal to 3 times 63, w is equal to 189.

From hence ariseth that precious Gem in Arithmick, which for the Excellency thereof is called

Golden Rule, or Rule of Three

21 41 2000 p 211 (.T. at the eigen .- X. a. q. A. Hv D c in the blarge be.

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HE Rule of Three (not undefervedly calls Golden Rule) is, that by which we find a fourth number, in proportion unto three given Num fo as this fourth Number fought may bear the Rate, Realon, or Proportion to the third (given) ber, as the second doth to the first, from whence it also called the Rule of Proportion.

2. Four Numbers are laid to be Proportional when first containeth or is contained by the second, as o as the third containeth, or is contained by the four

Vide Wingates Arith. Chap. 8. Sed. 4. So these Numbers are faid to be Proportionals. 2, 6, 9, fo, for as often as the fifft Number is tained in the second, to often is the third contain in the fourth, viz. twice. Allo 0, 3, 14, 5, are to be Proportional, for at often as the first Number of taineth the second, so often the third number cont eth the fourth, wir. 2 times.

3. The Rule of Three is either simple or composit

The fimple (or fingle) Rule of Three, confile of 4 Numbers, that is to lay, it hath a Numbers and to find out a fourth 3 and this is citizer Direct.

Inverse. Vide Alfted. Math lib. 2. cap. 73.
5. The ling e Rule of Timee direct, is when the in portion of the first term is to the second, as the third to the fourth; or when it is required that the Ma fou

might (vir.) the fourth Momber must have the same reportion to the second, as the third hatis to the sisse.

6. In the Rule of Three, the greatest difficulty is after the Question is propounded) to discover the ride of the 3 terms, vir. which is the first, which the second, and which the third, which that you may inderstand, observe, That (of the three given Numbers) wo are always of one kind, and the other is of the lame kind with the Proportional Number that is sought; is in this Question, viz. If 4 yards of Cloth cost 12 stillings, what will 6 yards oost at that Rate? Here the two Numbers of one kind are 4 and 6, viz. they both simile so many yards; and 12 shillings is the same kind, with the Number songht, for the price of 6 yards is sought.

Again, observe, that of the 3 given numbers, those two that are of the same kind, one of them must be the sirst, and the other the third, and that which is of the same kind with the number sought, must be the second number in the Rule of three; and that you may know which of the said Numbers to make your first, and which your third, know this, that to one of those two Numbers there is always affixed a demand, and that momber upon which the demand lieth must always be reckoned the third Number. As in the forementioned Question, the demand is affixed to the number 6, for it is demanded what 6 yards will cost? and therefore 6 must be the third number, and 4 (which is of the same denomination (or kind) with it) must be the first, and consequently the number 12 must be the second, and then the numbers being placed in the forementioned order will stand as followeth: with

wellen Fould-see

ards 129 1900 of yards

7. In the flule of Three Direct (having placed the numbers as is before directed) the next thing to be done will be to find out the fourth number in proportion, which (that you may do) multiply the fecond number

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by the third, and divide the product thereof by hirst, (on which is all one) multiply the third term number) by the second, and divide the product them by the first, and the Quotient thence arising is the number in a direct proportion, and is the number source or Answer to the Question, and is of the same denomination that the second number is of, As thus, let him Question be again repeated, viz. If 4 yards Cloth cost 12 shillings, what will 6 yards cost?

Having placed my numbers according to the & Rule (of this Chapter) foregoing, I multiply (the cond number) 12, by (the third number) 6, and the Rudust is 72, which Product I divide by (the first maker) 4, and the Quotient thence arising is 18, which is the fourth Proportional or number sought, viz. 18 shillings, (because the second number is shillings) which is the price of the 6 yards, as was required by the Quo

Rion. See the Work following.

Quest. 2. Another Question may be this, viz. 7. C. of Pepper cost 21. L. how much will 16 C. co

at that Rate?

To refolve which Question, I consider that (according to the 6th Rule of this Chapter) the terms or numbers ought to be placed thus, viz. the Demand lying upon 16 G. it must be the third number, and that of the same kind with it must be the first, viz. 7 C. and 21 (being of the same kind with the number sought) must be the second number in this Question; then I proceed according

of Three Direct. Chap. 10.

105

according to this 7th Rule, and multiply the second 226, which Ldivide by the first number 7, and the Quotient is 48 1. which is the value of 16 C. of Pepper at the rate of 21 l. for 7 C. See the Work as followeth,

Having orders and warping my wantees record

Description of the state of the

8. If when you have divided the Product of the fecond and third numbers by the first, any thing remain after Division is ended, such Remainder may be multion that are equal to an Unit (or Integer) of the fecond number in the Quellion, and the Product there-of divide by the first number in the Quellion, and the Quotient is of the same Denomination with the parts by which you multiplyed the Remainder, and is part of the fourth number which is fought. And furthermore, if any thing remain, after this last Division is ended, multiply it by the parts of the next inferiour denomination equal to an Unit of the last Quotient, and diride the Product by the same Divisor (viz. the first number in the Question) and the quote is still of the same denomination with your Multiplyer; follow this Method until you have reduced your Remainder into the lowest Denomination, &c. An Example or two

will

The fingle Rule Chap. 10.
will make the Rule very plain, which may be this fel.
lowing.

Quelt, a. If 13 yards of Velvet (or any other thing coft 21 l. what will 27 yards of the fame coft at that

Rate ?

Having ordered and wrought my Numbers according to the 6 and 7 Rules of this Chapter, I find the Quotient to be 43 L and there is a Remainder of 1 so that I conclude the price of 27 yards to be more than 43 /. and to the intent that I may know how much more, I work according to the foregoing Ruk vie. I multiply the faid Remainder 8 by 20 s. (be cause the second number in the Question was Pound and the product is 160, which divided by the fin number, viz. 13, it quotes 12, which are 12 shilling and there is yet a Remainder of 4, which I multiple by 12 pence, (because the last Quotient was shilling and the product, is 48, which I divide by 13, (a first number) and the Quotient is 3 d. and yet the remaineth o, which I multiply by 4 farthings, a the product is 36, which divided by 12 again, quotes 2 fasthings, and there is yet a remainder farthing) may be neglected, or rather fet (after the farthings) over the Divilor, with a Line between the and then (by the 21 and 22 Definitions of them Chapter of this Book) it will be \$\frac{1}{2}\$ of a farthing to that I conclude, that If \$2.7 and of Velvet coil 21. 27 mode of the fame will coil \$2. 125 of \$2. \$\frac{1}{2}\$ are which Fraction is 10 thirteenths of a \$6. \$\frac{1}{2}\$ for the Operation as followeth.

any time remain, after this last Division is coded, and tipe out the parts of the next infection denomination equal to in Utilit of the last Quotient, and divide the Froduck by the fame Division (vir. the first number in the Question), and the quote is still of the sime denomination with your Stuffighter; follow this method with you have reduced your Remainder.

lliw

Quest: 4. Another Example may be this following, viz. If 14 l. of Tobacco cost 27 s. what will 478 L cost at that rate?

Work according to the last Rule, and you will find it to amount to 921 s. 10 d. 1 +2 qs. and by the 50%

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9. In the Rule of Three it many times happeneth, that although the first and third numbers be Homogeneal (that is, of one kind) as both Money, Weight, Measure, &c., yet they may not be of one denomination, or perhaps they may both consist of many denominations, in which case you are to reduce both numbers to one denomination; and likewise your second number (if it consistent (at any time) of divers denominations) must be reduced to the least name mentioned, or lower if you please, which being done, multiply second and third together, and divide by the first, as is directed in the 7th Rule of this Chapter.

And note that always the Answer to the Question is in the same denomination that your second number

is of, or is reduced to, as was hinted before.

Quest. 5. If 15 Ounces of Silver be worth 3 1.

15 s. what are 86 Ounces worth at that Rate?

In this Question the numbers being ordered according to the 6th Rule of this Chapter, the first and third numbers are ounces, and the second number is of divers denominations, viz. 3 1. 15 s. which must be reduced to Shillings, and the shillings multiplyed by the third number, and the product divided by the first, gives you the answer in shillings, viz. 430 shillings, which are reduced to 21 L. 10 s. See the Work.

In refolving the last Question, the Work would have been the same, if you had reduced your feeth number into pence, for then the Answer would have been \$160 pence, equal to 211. 102, or if you have duced the second number into farthings, the Quoties or Answer would have been 20040 farthings equal the same, as you may prove at your ferfure.

Quest. 6. If 81. of Pepper coft 4 s. 8 d. what w

7 C. 3 grs. 14 L coft ?

In this Queltion the first number is 8 l. and the thin is 7 C. 2 grs. 14 l. which must be reduced to the fact denomination with the first, viv. into pounds, and the cond number must be reduced into pence; then multiply and divide according to the 7th Rule foregoing and you will find the Answer to be 6174 pence, which is reduced into 25 l. 14 s. 6 k.

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4410 02 2 0 L 8) 49392 (6174 (51)4 (25) 48 60 4 13 17 11 1-1 8 12 10 59 54 14 fbillings 56 48 32 (6) pence 32 1. s. d. Queft. 7. If 3 C. 1 gr. 14 l. of Raifins coft 9 L. o.s.

what will 6 6. 2 grs. 20 1. of the same cost?

Were the first and third numbers each consist of divers denominations, but must be brought both into one denomination, Gr. as you fee in the Operation which followeth; the Answer is 388 s. which is reduced into 19 1. 8 s.

C. qr. 1. G. qrs. 1. If 3-1-14 mft 9-9 what will 6-3-20 ceft? 1 PFo 2 pence 28 हिस्कार्य महामण्डा 27 28 28 102236 216 56 278 pounds. 776 pounds. 189 fecond number Ser. (38) days 6984 6208 2(0) l. d. 776 378) 146664 (38 8 19-8 1134 3326 . 18 3024 801 (08) (billings (d.) animma 3024 3024

voye the yearly Scot of a Houle, it facit 19 or Wages be 73 f. 'I define to know

Such 8. If in a week I spend is r. a it how long still se it that the still se of the late? The still se it has late? The still se it has been seen as the work. See dock is the fame, for a neither multiplyed not and adeting and 79 cannot be divided by 36%, because the

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Quest. 9. Suppose the yearly Rent of a House, yearly Pension, or Wages be 731. I defire to ke how, much it is per day.

Here you are to bring the year into days, and if 365 days require 731, what will one day require Now when you come to maltiply 73 by 1, the reduced is the forms for a nation of the forms.

duct is the fame, for I neither multiplyeth nor an deth, and 73 cannot be divided by 365, because t Divifor is bigger than the Dividend, wherefore bring the 73 l. into shillings, and they make 1460, which divide by the first number 365, and the Quote is 4 shillings for the Answer, as you see in the Work.

Quest. 10. A Merchant bought 14 pieces of Broad Cloth, each piece containing 28 yards, for which he gave after the Rate of 13.5.6 1 d. per yard, now I desire to know how much he gave for the 14 pieces

t that Rate?

ife,

First, Find out how many yards are in the 14 piees, which you will do if you multiply the 14 pieces y 28 (the number of yards in a piece) and it makes 92; then fay, If I yard cost 13 s. 6 td. what will 92 yards cost? Work as followeth; and the Answer ou will find to be 127400 half-pence, which reduced nake 2651. 8 s. 4 d. For after you have multiplyed our fecond and third Numbers together, the Product 127400, which (according to the leventh Rule) hould the divided by the first number, but the first umber is 1, which neither multiplyeth nor divideth, ad therefore, the Quotient or fourth number is the me with the Product of the second and third, which in half-pence, because the second number was la educed. See the Work, as followeth, into queriers, the ER to enumeral and in aposition

are 1630 surveys, then in To equation and the society of the society and the total quarter of the total quarter of the control of the control

Quell. 11. A Draper bought 420 yes of broad-cle and gave for it after the rate of 14 s. 10 d. per English, now I demand how much he paid for whole at that Rate?

Bring your Ell into quarters, and your given your onto quarters, the Ell is 5 quarters, and in 420 you are 1680 quarters, then fay, If 5 quarters cost 14 to 14 (or 715 farthings) what will 1680 quarters cost? facit 250 L 05 s. 00 d. See the Operation.

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The same of the sa	A. A. A.	20	100	

Quefl. 12. A Draper bought of a Merchant 90 pleases of Kerleys, each piece containing 34 Ells Flemish, the Ell Flemish being 3 quarters of a yard) to pay fiter the Rate of 8 s. Ad. per Ell English, I demand low much the 30 pieces cost him at that rate?

stall Ask I fem and what it flood him in the Dunce

Amver do follon s. e 185 . See the weeks

First, Find how many Ells Flemish are in the 50 pieces by multiplying 50 by 34, the Product is 1700, which bring into quarters by 3, it makes 5100 quarters, then proceed, as in the last Question; and the answer you will find to be 102000 pence, or 425 %.

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Quest. 13. A Goldsmith bought a Wedge of Go which weighed 141. 3.02. 8 p.m. for the Sum 534 l. 4 s. I demand what it stood him in per Ounce Answer 60 shillings, or 3 l. See the work.

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s there were in ba First, Find out hor ork you will find t 8 packs, as by the following are 9320 yards; then i

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By this time the Learner is (I suppose) well exercised in the Practick and Theorick of the Rule of Three Direct, but at his leasure he may look over the following Questions, whose Answers are given, but the operation purposely omitted as a Touchstone for the Learner, thereby to try his Ability in what hath been delivered in the former Rules.

Question 16. If 24. L of Russias cost 5 2. 6 8, what will as Frails cost, each weighing Neat 2 ars. 18 1. Answer

241. 175. 034.

Quest, 17. If an Ounce of Silver be worth & shillings what is the price of 14 Ingots, each ingot weighing 7 l. 4 or. 10 p.w.? Answer 313 l. 5 s.

Queft. 18. If a piece of Cloth coft 10 1. 16 s. 8 d. I demand how many Ells English there are in the same, when the Ell at that rate is worth 8 s. 4 d.?

Anjw. 26 Ells Engliff

Quest. 19. A Factor bought 84 pieces of Stuffs, which cost him in all 537 1. 123, at 52. 4 d. ser yar. I demand how many Yards there were in all, and how many Ells English were contained in a piece of the same. Answer 2215 Yards in all; and 194 Ells English per piece.

Quefi. 20. A Draper bought 242 yards of Broad-cloth, which cost him in all 244 l. 10 s, for 86 yards, of which he gave after the Bate of 27 s. 4 d. per yard, I demand how many he gave per yard for the Remain-

der! Anon 200. 10 d. - 14 per yards.

Quell. 21. A Factor bought a certain quantity of Sarge and Shalloon, which together coff him as 1, 14 3. sorge and Shalloon, which together continuous. 143; so it, the quantity of Serge, he bought was 48 yards at 25, 4d per yard, and ide every two yards of Serge he had 5 yards of Shalloon, I demand how many yards of Shalloon he had, and how much the Shalloon coff him per yard. Adhe 120 yards of Shalloon at 1 l.

166, 05 1 d. per yard.

28ch 22. An Oyl, man bought 2 Tun of Oyl, which coff him 151 l. 34 s. and it so chanced that it leaked out 85 gallons, but he is minded to fell it again, so as that he may be no loser, but it I demand how he

that he may be no loser by it, I demand how he

The fingle Rule 120 must fell it per gallon ! Answer,

Bought & packs of Cloth, each pack of taining 12 Cloths, which at 8 , 4 d. ser Ell Flem coft 1080 L. I demand how many yards there were each Cloth? Anjwer 27 yards in each Cloth.

Queft. 24. A Gentleman hath \$35 l. per annum, a his Expences are one day with another 18 s. 10 3 qrs. I defire to know how much he layeth up

the years end? Answer 1911. 25. 0 d. 1 gr. with another 27 s. 10 1 d. and at the years end eth up 340 l. I demand how much is his yearly

Queff. 26. If I fell 14 yards for 10 L. 10 s. 00 how many Ells Flemish shall I sell for 282 L. 17 s. 6

at that rate? Answer 504? Ells Flemish. at the fame rate? Answer 41. 10 5.

Quest. 28. If 100 L. in 12 Months gain 6 t.

reft, how much will it gain in 7 Months at that a

Anfwer 3 L. 10s.

Queft. 29. A certain Ulurer put out 75 1. for Months, and received Principal and Interest 81 demand what rate per Cent. he received Interest? fiver 8 1. per Cent.

Quest. 30. A Grocer bought 2 Chests of Sugar, one weighed neat 17 C. 3 grs. 141. at 21, 65. 1 per C. the other weighed neat 18 C. 1 gr. 21 L at 4. per 1. which he mingleth together, now I defire know how much a C, weight of this mixture is worth Aufwer 21. 45. 34. 2552 95.

Queft. 21. Two men, wx. A and B departed to from one place, the one goes East, and the other we the one travelleth 4 miles a day, the other 5 miles day, how far are they diftant the oth day after the departure ? Anfwer 91 miles. M 8 4 gallons, but

urt

of may be no losse at it, I decrease tow he 1 10 .24

the 4th day after by B, posting so miles a day, now the Question is in 18. Quest 7: how many days, and after how many days, when they have yelled soot miles.

11. The general Effect of the Rule of Three Difir, is contained in the definition of the fame, that is, find a fourth Number in proportion conflicting of the equal Regions, as hath been fully shewn in all the

regoing Examples.
The second Effect is, by the price of value of one ing to find the price or value of many things of like

The third Exect is, by the price or value of many ings to find the price of one, or by the price of ny things (the laid price being 1) to find the price many things of like kind.

The fourth Effect is, by the price or value of mathings, to find the price of value of many things like kind.

The fifth Effect is, thereby to reduce any Number Moneys, Weight, or Measure, the one fort into the er, as in the Rules of Reduction contained in the the Chapter foregoing. Examples of its various etts have been already answered.

The Rule of 3 Direct is thus proved, siz, mul-

by the first Number by the fourth, d note the Product, then multi-The Proof of the the second number by the third, Rule of Times If this Product is equal to the Direct.

so the first Question of this Chapter (whose Aner, or fourth number we found to be 18 s.) is thus oved, viz. the first number is 4, which multiplied 18 (the fourth) produceth 72. And the second and ird numbers are 12 and 6, which multiplied togeer produce 72, equal to the Product of the first and butth, and therefore I conclude the work to be rightperformed.

Always obser the lecond and this Same denomination with

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the fune denomination -So the Fourth Que So the Fourth Quellion of this again repeated, viz. If 141, of To what will 478 1, coff at that Bate? fourth number) was 46 l. of s. 10 d. 1 things, and it makes 44249, which mu firk number 14, produceth 619488 (the remaineth being added ther eto) th duce my fourth lecond (viz. 27 s.) into farthings, and shey as which multiplyed by the shird number 47%, to duct is 619488 equal to the Product of the duct is 619488 equal fourth Numbers. When fairth Numbers. Wherefore I conclude to be true. This is an infallible way Rule of Three Dirett, and it is deduced from t Section of the oth Chapter of this Bo

Thus much concerning the fingle ner is fufficiently qualified to refolve Geometrical Magnitudes. Those that are de fixth Chapter of (the ingenious) Mr. Kerley, to Wingates Arithmetick. Or the fixth Cha Oughreds (Incomparable) Clauis Math both which Authors this Rule is largely d being grounded upon the 19th Prop. of the 19th Prop. of the 9th of Euclid. Ele

named is a, which man took of or ducoil of Andri lecond and

sort beilaidiam d'in le parte d'ese back in our to decome with a

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tale of Three Taverfa.

charten Rule of Rule of a Inverse, is when each are a Mumbers given to find a fourth, in their to the a given Numbers, so as the each from the econd, according to the Resion, or Proportion that the first protes third, or the Proportion is, hird number is in proport. Aisted. Matth. Second, so is the first to the 2. cap.14.

rif the gumbers given were 8, ra, and 16, and it required to find a fourth number in an inverted portion to these, I say that as 76 (the third Numis the double of the first term or number (8) so I the double of the first term or number (8) so I 12 (the second number) be the double of the th; so will you find the fourth term or number to And as in the Rule of a Direct, you multiply the me and third together, and divide their Product a fourth Proportional Number : So, In the Rule of a Inverse, you must multiply the add term by the first (or first term by the second)

divide the Product thereof by the fined ferm, so the set will give you the fourth term sought in an Individual that of a Direct, for placing and divide the given numbers, and after your numbers that in order, that you may know whether your tion be to be resolved by the Rule Direct of Inobered the general Rule following.

When your Question is stated, and your numbers by all patent, doubter in the first place whether ourth term or number sought, ought to be more is than the second term; which you may easily and if it is required to be more, or greater than econd term, then the lesser Extream must be your for; but if it required less, then the biggest Extended.

ifor the if it require less, then the biggest Ex-

tream must be your Divisor, (in this Case the first third numbers are called Extreams in respect of the cond,) and having found out your Divisor, you know whether your Question belong to the Rule I or Inverse, for if the third term be your Divisor, it is a Direct Rule. As in the following Question Question. It is a Labourers can do a certain pier content of the co

work in 12 days, in how many days will 16 l

Having placed the numbers according to the 6th of the 10th Chapter, I consider that if 8 Men can finish the lab. dese Work in 12 days, 36 Men will do it in leffer (or fewer dayes, than 12,) therefore the biggeft Extream mult be the Divilor, 16) of which is 16, and therefore it is the Bule of 3 Inverse, wherefore I mul-tiply the first and second numbers together, vig. 8 by 12, and their Fact 6 day Product is 96; which divided by 36, Quotes 6 days for the Anjwer, and in far days will 16 Labourers perform a piece of s

when 8 can do it in 12 days. Queft. 2. If when the measure (viz. a peck) of veoft 2 shillings, the penny Loaf weighed (according the Standard, Statute, or law of England, 8 Out demand how much it will weigh when the per worth 1 s. 6 d. according to the same Rate or Pro

tion? Answer 10 oz. 13 p.m. 8 gr.
Having placed and reduced the given numbers as
ding to the 6 and 9 Rules of the 10th Chapter, 1 fider, that at 1.5. 6 di per peck, the penny Loaf weigh more than at 2 s. per peck, for as the prior creafeth, and as the prior creafeth, fo the weight diminisheth, wherefore become after the penny Loaf that the penny Loaf weight diminisheth, wherefore become after the penny Loaf weight diminisheth, wherefore become after the penny Loaf weight diminisheth, wherefore become after the penny Loaf weight diminisheth. the term requireth more than the ferond, the le Extream must be the Divisor, 15, 6 de or 18 de having finished the work, I find the Answer to be so 8 gr. and fo much will the penny Loaf weigh, a the peck of Wheat is worth 1 s. 6 d. according a given rate of 8 ounces, when the peck is worth lings, the work is plain in the following operation.

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Quelt. 2. How many pieces of Money or Merchandise at 20 s. per piece are to be given or received for 240 pieces, the value or price of every piece being 12 shilings? Anheer, 144. For if 12 s. require 240 pieces, then 20 shillings will require less; therefore the biggest Extream must be the Divisor, which is the third number, Gr. See the Work. If 12—249—20

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2|0) 288|0 (144 pieces # 20 p. per piete

00)

Queft. 4. How many yards of 3 quarters broad required to double, or be equal

in measure to 30 yards, that are 3 quarters broad? Answer 30 yards, For say, if 5 quarters wide require 30 yards long, what length will three quarters broad require? Here I consider that 3 quarters broad will require more yards than 30, for the narrower the Cloath is, the more in length will go to make equal measure with a broader piece.

3) 150 (50) 150 (50) no gri

Quest. 5. At the Request of a Friend I lent his 200 l. for 12 Moneths, promiting to do me the li Courtesse at my Necessity; but when I came to quest it of him, he could let me have but 150 l. no I desire to know how long I may keep this Mosto make plenary satisfaction for my former kinds to my Friend? Answer 16 Months. I say, if 200 require 12 Months, what will 150 l. require? To will require more time than 12 Months, therefore besser the same of the Divisor, Mul

divide, and you will find the fourth inverted to be 16, and fo many Months I ought to 1 140 L for fatisfaction.

miles how many miles that 1800 h be carried for fame Money? Anjour 24 miles 200 h carried 36 miles for the fame Money? Anjour 1800 h

8: If too Workmen in 12 days finish a piece of work or service, how many Workmen are sufficient to do the same in 3 days? Answer 400, Workmen.

Queft. 9. A. Colones is befreged for a Town in which

Moneths, the Question is, how many of his Soldiers must be difinish, that his Victuals may last the remaining Soldiers 6 mouths? Answer, 900 he must keep, and difmils as manyor

Buelt, to. If Wine worth 20 1, is fufficient for the Ordinary of 100 Men, when the Tun is fold for 40 f. how many Men will the same 20 pounds worth suffice, when the Tunis worth 24 L. Anjwer, 125 Men.

Queft. 11. How much Plush is sufficient to line a

Clock which hath in it 4 yards of 7 quarters wide, when the Plush is but a quarters wide? Answer, 94 yards of Pluth. The Table 10

Queft 12. How many yards of Canvas that is Ell-wide, will be sufficient to line 20 yards of Say, that

is 2 quarters wide & Angeer, 12 yards.

Queft. 13. How many yards of Matting that is two foot wide, will cover a Floor that is 24 Foot long, and

Resh 14. A Regiment of Soldiers confifting of iboo, are to have new Coats, and each Coat to conwide, and they are to be lined with Shalloon that is a quarters wide, I demand how many yards of Shalloon will line them? Answer, 16666? quarters of yards, or 4166! yards. pac a morrowit o

Queft.

Quest. 15. A Mellenger makes a Journey in 24 when the day is 12 hours long. I define to kn how many days he will go the fame when the d

Quest. 16. Borrowed of my Friend 64 l, f. Months, and he hath occasion another time for to row of me for 12 Months, I defire to know much I must lend to make good his former kind

tained in the definition of the fame, that is, to he fourth term in a Reciprocal Proportion, inverted

the Proportion given.

The fecond Effect, is by two prices, or value two feveral pieces of Money or Merchandize kno to find how many pieces of the one price is to be ven for so many of the other. And consequently Reduce and Exchange one fort of Money, or M chandize, into another. Or contrariwise to find price unknown of any piece given to Exchange in

crorocal Proportion.

Sal reliw udi The third Effect, is, by two differing prices of measure of Wheat bought or fold, and the weights the Loaf of Bread, made answerable to one of the prices of the measure given, to find out the weig of the fame Loaf, answerable to the other price the faid measure given. Or contrariwise by the to faveral Weights of the fame prized Loaf, and the price of the measure of Wheat answerable to one of the Weights given, to find out the other price of the measure answerable to the other weight of the same

The fourth Effect, is, by two lengths, and or breadth of two Rectangular Planes known, to find ou another breadth unknown. Or by two breadths at one length given, to find out another length unknow in an inverted Proportional and the state

The fifth Effect, is, by double time and a capital Sum of Money borrowed or Lent, to find out another capital Sum answerable to one of the given Times

two Capital Sums, and a time answe-

The fixth Effect is, by two differing Weights of Carriage, and the difference of the places in Miles or in tagues given, to find another difference in miles anwerable to the fame price of payment: Or otherwise of two differences in miles anwerable to the fame price of payment: Or otherwise of two differences in miles, and the weight answerable to one of the differences (being carried for a commitment of the differences (being carried for a commitment) to find out the weight answerable to the other differences for the fame. er distance for the fame price.

The feventh Effect is by double Workmen, and the time answerable to one of the numbers of Workmen given, to find out the time answerable to the other mber of Workmen, in the performance of any work or ervice. Or contrariwife, by double time and the Worken answerable to one of thosh times given, to find out the monber of Workmen answerable to the other time, in the performance of any work or service.

Alfo by a double price of Provision, and the numof Men, or other Greatures nourished for a cerain time, answerable to one of the prices of Provision iven, to find out another Number of Men or other creatures answerable to the other price of the Provibers of Men or other Creatures nourished, and one price of Provision answerable to one of the numbers of Creatures given, to find out the other price of the ame Provision answerable to the other number of Creatures, both being supposed to be nourished for the ame, oc. As in the foregoing Examples is fully declared.

To prove the Operation of the Rule of a Inverse, multiply the third and fourth terms together, and note their Product; and multiply the first and second gether, and if their Product is equal to the Product! of third and fourth, then is the Work truely wrought, but if it falleth out otherwise, then it is crroneous.

As in the first Question of this Chapter, 16 (the third number) being multiplied by 6 (the fourth number)

GS

the Product is 66, and the Product of I number) multiplyed by 12 (the fee count to the first Product, which prove

be Right.

And Note, that if in Division any thing refuch Remainder must be added to the Product of third and fourth terms, and if the Sum be equal Product of the first and second (the humogeneal being of one denomination) the work By

CHAP. XII

The Double Rule of Three Direct.

VE have already delivered the Rules of S

the Rules of Phiral Proportion.

"" Planal Proportion, is when more Operations is
Rule of Three than one, are required before a tion can be given to the Question propounded. The fore in Questions that require Plurality in Free there are always given more than three numbers.

2. When there are given 5 numbers, and a fir

required in Proportion thereunto, then this fixth portion is faid to be found out by the double Rule

as in the Question following, viz.

If 100 L in 12 mouths gain 6 ls interest, how

will 75 le gain in 9 months?

2. Queffions in the double Rule of 2 may be folved either by two fingle Rules of Three, or by fingle Bule of Three, compounded of the five a Numbers.

4. The double Rule of g is either Direct, or

Inverse.

5. The double Rule of 3 Direct, is when unto given Numbers a fixth proportional may be found by two fingle Rules of Three Direct.

6. The five given Numbers in the double Rule

arts, viz. First, supposition, and e three first of the five given Numbers, and the Deand lies in the two last; as in the Example of the sand Rule of this Chapter, oie; If too l in 12 norths gain 61, increest, what will 75 l gain in 9 norths? Here the Supposition is expressed in 100, 12, ad 6; for it is said, if (or suppose) 100 l in 12 norths gain 6 l. Interest, and the Demand lyeth in

months gain & L. Interest, and the Demand lyeth in a and a; for it is demanded how much 75 L will a gain in 9 months?

7. When your Question is stated, the next thing will be to dispose of the given Numbers in due order and place, as a Preparative for Resolution; which stat you may do. First, observe which of the given Numbers in the Supposition is of the same Denomination with the Number required; for that must be the second number (in the first operation) of the single Rule of 3, and one of the other Numbers in the Supposition (it matters not which I would be the first Number. tion (it matters not which) must be the first Number, Denomination with the Demand which is of the fame Denomination with the first, must be the third number, which three Numbers being thus placed, will make one perfect Question in the single Rule of Three, as in the forement sound Example. First, I consider that the Number required in the Question is the Interest or Sain of 75 L. therefore that Number is the Supposition which bath the time name (viz. 6 l. which is the in-

lecond Number in the first Operation, 120-5-75 and either 100 or 12 (it matters not 100)

half ha fairle

which) must be the first Number; but I will take tee, and then for the third Number, II put that Number in the Demand which bath the fame Denomination with 100, which is 75, (for they both fignific sounds principal) and then the Numbers will Rand as you fee in the Margent. Sheet Level took basin i.

But if I had for the first Number put the other We ber in the Supposition, viz. 12 which significate Months, then the third number must in the Demand which hath the fame Denomination with the first, wiz. 9 Months, and the they will stand as you see in the Margent.

There yet remain two Numbers to be disposed and those are, one in the Supposithat which is of the Suppolition, I 12 Numbers, and the other which is in the Demand I place under the third sumber, and then 2 of the tirms in the supposition will stand (one over 100 the other) in the first place, and the

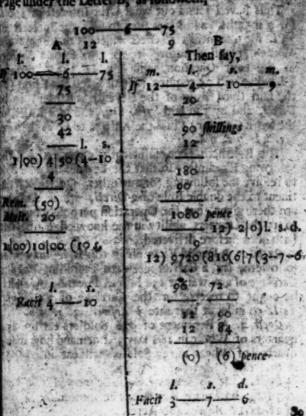
2 serms in the Demand will fland (one over the other in the third place, as in the Margent.

8 Having disposed, or ordered the numbers give according to the laft Rule, we may proceed to a R lurion, and first I work with the three upperm Numbers, which according to the first disposition at require 6 L (Interest) how much will 75 L require which by the the third Rule of the cleventh Chapter find to be Direll, and by the 7 and 8 Rules of the tenth Chap. I find the fourth Proportional number to be 4 1. 10 s. fo that by the foregoing fingle Question ! have discovered how much Interest 75 will gain it 12 mon.; the operation whereof followeth on the let hand under the letter 4 ; and having difcovered how much 75 th will gain in 12 Months, we may by ano ther Question castly discover how much it will gain it e months, for this fourth number (thus found) I put in the middle between the two lowest Numbers of the five after they are placed according to the seventi Rule of this Chapter; and then it will be a fecond Number, in another Question in the Rule of Three,

the numbers being 12 4 to 9 the first and third

numbers

dere being of one Denomination, vir. both Months, it may be thus expressed, if 12 months require 4 h. i. Interest, what will 9 months require? And by ethird Rule of the 12th Chapter I find it to be the rell Rule, and by working according to the directions it down in the 7. 9, and 9 Rules of the 10th Chapter I find the fourth Proportional number to the last singlend may be thus ex os. Interest, who e Question to be 3 1. 67 s. of d. which is the fixth operational number to the s given numbers, and is the fingle Question is expressed on the Right side of the Page under the Letter B; as followeth,



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So that by the foregoing Operation I conclude the fit now I. in a a months gain & I. Interest, 75 i. will go a l. 76. 6 d. in 9 months, after the fame, and the fit the 5 given Numbers had been needed to 15. 6 d. according to the ferond Method, size as 100 m.

secording to the fecond Method, size as 400 you fee in the Margent.

For first, I say, if 12 months gain 6 & what will

months gain? This Question I find to be Direct by the get Bule of the state Chapter, and by the geant Rules of the state Chapter, I find the fourth Propertional Number to these three to be 4 h. 10 s.

Thus have I found out what is the Interest of 100 leaves

or months, and I am now to find the Interest of Number (found as before) to be my fecond Num in the next Question, and fay, If 100 L requi the faid third Rule of the eleventh Chapter) to Dired, and by the faid 7th, 8th, and oth Rules the tenth Chapter, I find the Answer to be as before viz. 31. 75. 6 d.

This Rule hath been sufficiently explained by the to resolve the following (or any other) Questions pe tinent to the double Rule of 3 Dired, whole Anla are there given, but the Operation purposely omit to try the Learners ability in the knowledge of wh

hath been before delivered.

Queft. 2. A Second Example in this Rule may be followeth, viz. a Carrier receiveth 42 fhillings for the Carriage of 200 weight 150 Miles, I demand how much he ought to receive for the Carriage of 7 C. 34 14 1. 50 miles at that rate ? Infirer, 36 s. 9 d.
Queft. 3. A Regiment of 936 Soldiers eat up 31

quarters of Wheat in 168 Days, I demand how man quarters of Wheat 11232 Soldiers will eat in 56 Day at that rate? Answer, 1404 grs.

Queft. 4. If no Acres of Grafs be moved by 8 me in 7 Days, how many Acres shall be mowed by 24 mil an 28 days ? Animer, 480 Acres. Quel

Queft. 5. If 48 Buthels of Corn (or other feed) yield 6 Buthels in 1 Tear, how much will 240 Buthels eld in 6 years at that rate! That is to fay, if there are fowed 240 Bulhels every one of the 6 years

Quest, 6. If 40 hillings is the Wages of 8 Men for 3 days, what thall be the Wages of 32 men for 24 days? Answer, 768 faillings, or 38 l. 8.

Quest. 7. If 14 Hories cat 56 Business of Provender to Days, how many Business will 20 Hories cat in 19 Days? Answer, 120 Business will 20 Hories cat in 19 Days? Answer, 120 Business.

Such. 8. If 8 Cannons in 1 Day spend 48 Earrels of Powder, 1 demand how many Barrels 24 Cannons all spend in 22 days at that rate? Answer, 1728 arrels.

Quest. 9. If in a family conditting of 7 Persons there are drunk out 2 Rilderkins of Beer in 12 days. how many Kilderkins will there be drunk out in 8 days by another Family confifting of 14 Persons? Answer,

48 Gallons, or a Kilderkins and 12 Gallons.

Quest. 10. An Usurer put 75 l. out to receive Interest for the fame, and when it had continued a Months, he received for Principal and Interest 78 1. 7 1. 6 d. I demand at what rate per Cent. per Annun, he received Interest ! Answer, at 6 l. per Cent. per Annum.

CHAP XIII

nilides attacim o literatura The Double Rule of Three Inverse.

HE Double Rule of a Inverse, is, when a Question. In the Double Rule of a is refolved by 2 Single Rules of 3, and one of those Single Rules falls out to be Inverse, or requires a fourth number in Proportion Reciprocal (for both the Questions are never Inverse.)

2. In all Questions of the Double Rule of 3 (as well liverse as Direct,) you are (in the disposing of the e

given.

numbers) to observe the seventh stude of the Lath Charter, and in resolving of it, by two single Rules, of serve to make Choice of your Numbers for the first and second, single Questions according to the directions given in the eighth Rule of the same Chapter, as in the Example following, viz.

Quest. 1. If 100 l. Principal in 12 Months gain 61, Interest, what Principal will gain 31. 75. 6d in

months?

This Question is an Inversion of the first Question of the 12th Chapter, and may serve for a proof thereof. In order to a Resolution, I dispose of the 5, given Numbers according to the 7th Rule of the last Chapter, and being so disposed, will stand as followeth,

Here observe, that according to the eighth Rule of the twelfth Chapter, the first Question, if you take the from the 5 Numbers, (as they are ordered or placed first) will be; If 12 months require 100 L. Principal what will 9 months require to make the same Interest? This (according to the third Rule of the 11 Chapter) is Inverse, and the Answer will be found (by the 2 Rule of the 1115 Chapter) to be 123 L. 618 8 L. the second question them will be. If 16 L interest, require 132 L. 618 8 L. Principal, how much Principal will 3 L. 7 5. 6 L. require? This is a direct Rule, and the Answer in a direct Proportion is 75 L. See the Work.

Fieft I fay,

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So that by the foregoing Work I find that if 6 l. In terest be gained by 100 L in 12 months, 3 l. 74.64

will be gained by 75% in 9 months.

But if the resolution had been found out by the Numbers as they are ranked in the second place, the the second Question in the single Rule would have been Inverse, and the first Question Direct, and the conclusion the same with the first Method, viz. 75%

Quest. 2. If a Regiment confisting of 936 Soldiers can eat up 351 quarters of Wheat in 168 days, how many Soldiers will eat up 1404 quarters in 56 days at that rate? Answer, 11232 Soldiers.

Quest. 3. If 12 Students in 8 Weeks spend 48 L. demand how many Students will spend 288 l. in 1

Weeks? Answer, 32 Students.

Queft. 4. If 48 L. ferve 12 Students 8 Weeks, how any weeks will 288 L. ferve 4 Students? Anjwer 244 (cels).

Rueff. 5. If when the Buffel of Wheat coff 3 : 4d. the peny Loaf weigheth 12 ounces, I denand the weight of the Load worth 9 d. when the Buffel coff 14 s. Answer 36 ounces.

Pueff. 6. If 48 Proncers in 12 days caft a Trench

Rueft. 6. If 48 Proncers in 12 days caft a Trench 14 yards long, how many Proncers will caft a Trench 168 yards long in 16 days? Animer 242 Proncers.

Quelt. 7. If 12 C, weight being carried 100 mile call \$ 1, 12 i. I defire to know how many C. weight may be carried 150 miles for 12 l. 27, at that rate? Inswer, 18 C.

August, 18 C.

Quest. 8. If when Wine is worth 30 l. per Tun, 20 pounds worth is sufficient for the ordinary of 100 lien, how many men will 4 l. worth suffice when it is worth 24 l. per Tun? Anjwer 25 men.

Men, how many men will 41, worth fuffice when it sworth 241 per Tin? Anjwer 25 men.

Queft. 9. If 6 men in 24 days mow 72 Acres, it low many days will 8 men mow 24 Acres? Anjwer, it 6 days.

Quest. 10. If when the Tun of Wine is worth 30 L. 100 Men will be fatisfied with 20 L. worth, I define to know what the Tun is worth, when 4 L worth will trisfie 25 men at the same rate? Answer, 24 L per Tun.

the business CHAP XIV.

Mill of the man

The Rule of Three composed of five Numbers.

THE Rule of Three Composed, is, when Queftions (wherein there are 5 Numbers given to find a 5th in Proportion thereunto) are relolved by one finale Rule of 3 composed of the 5 given Numbers. 2. When Questions may be performed by the dou-

2. When Questions may be performed by the double line of 3 Direct, and it is required to resolve them by the Rule of 3 composed, (first order or rank your Numbers according to the 7th Rule of the 12th Chapter, then)

the language of the Rule is

Multiply the Terms or (Numbers) that stand on over the other, in the first place, the one by the other, and make their Product the first Term in the Rule of Three Direct, then multiply the Terms the stand one over the other in the third place, and place their Product for the third Term in the Rule of Three Direct, and put the middle Term of the Three uppermost for a second Term; then having sound a south Proportional, direct to these Three, this sourch Proportional so found, shall be the Answer required.

So the first Question of the 12th Chapter being propoled, viz. If 100 h in 12 Months gain 6 h Interest what will 75h gain in 9 Months? The Numbers being ranked (or placed) as is there directed and done.

Then I multiply the two first Terms, 100 and 12

Then I multiply the two first Terms, 100 and 12 the one by the other, and their Product is 1200 (for the first Term;) then I multiply the two fast Term 75 and 9 together, and their Product is 675 for the third Term. Then I say, as 1200 is to 6, so is 675 to the Answer, which by the Rule of Three Direct was found to be 3 1. 7 5. 6 d. as was before found.

3. But if the Question be to be answered by the

3. But if the Queftion be to be answered by the double Rule of Three Inverse, then (having place the five given Terms as before) multiply the lower most Term of the first place, by the uppermost Term of the first place, and put the Product for the first place, by the lowermost Term of the first place, by the lowermost Term of the third place and put the Product for the third time, and put the second Term of the three highest Numbers for the thiddle Term to those two, then if the Inverse Proportion is found in the uppermost three numbers, the 40 Proportional Direct to these three shall be the answer so the sirst Question of the 12th Chapter being stated, viz. If 100 l. Principal in 12 Months gain 6 l. Interest, what Principal will gain 21, 75, 6 d. in 9 Months! State the Numbers as is there directed in the first order, viz.

have gone about and and small small n reduce the 64 and 31. 74, 6 d. into pence, the 61. is 1440 d. and 3 l. 7 s. 6 d. is 810 d. then multi-by 1440 by 9, the Product is 12960 for the first erm in the Rule of Three Direct, and multiply 810 9 12, the Product is 9720 for the third Term, then lay, As 12960 is to 130 l. fo is 9720 to the Anced after the fecond order, viz.

where an discontinuous and the Tentrology the Rule of May and time dil May an act and all had a strong the of the one directly such as

delicination of the same of the contractor in the the Inverse Proportion is found in the lower numbers, and having composed the Numbers for a ingle Rule of Three as in the fecond Rule foregoing, hen the Answer must be found by a fingle Rule of three Inverse, for here it falls out to multiply 820 by 12 for the first Number, and 1440 by 9 for the third Number, and then you must say, as 9720 is to 180 lt so it raped to the Answer, which by investe Proportion will be found to be 75 lt as before the The Questions in the sarband 13th Chapters may

ferve for thy farther experience.

Let it show wer Long in CHAP. XVe mail to mis

the total Gamther alguel Fellowick

TELLOWSHIP is that Rule of Plural Proportion, whereby we ballance Accompts depending pending between awers Periods having put together general Stock. So that they may every man has his Proportional part of Galo, or infinin his Proportional part of Lofs.

2. The Rule of Fellowship is either single, or it

3. The fingle Rule is when the Stocks propounde are single Numbers without any respect or relation to time, each Purcher continuing his Money in Stock for the Same time.

is the winder Stock of all the Partners, is in Proportion to the total Gain or Loft, for is each of the particular than in the Stock, to his particular than in the Stock, to his particular than in the Gain or Loft. Therefore take the Partal of all the Stocks for the first Term in the Rule of three, and the whole Gain or Loft for the fecon Term, and the particular Stock of any one of the Partners for the third Term, then multiply and divide according to the 7th Rule of the 9th Chapter, and the Artners for the third Term, then multiply and divide according to the 7th Rule of the 9th Chapter, and the Proportional Number is the particular lots or go to thin whole Stock who made where ferond annual wherefore repet the fulle of a soften as therein particular flocks, and again the respective Gain as Loft of those quarticular Stock given, as in the Examples following.

Of Realt, is Two Sterious who A and B bought a Teor Witter for so d. of which a pain to Land B paid to and they gained in the Sterious who a land a land they gained in the Sterious and a land and they gained in the Sterious and a land a land and they gained in the Sterious and a land a land and they gained in the Sterious and a land a land they gained in the Sterious and a land and they gained in the Sterious and a land a land and they gained in the Sterious and a land a land and they gained in the Sterious and a land and they gained in the Sterious and a land a land and they gained in the Sterious and a land and they gained in the Sterious and a land and they gained in the Sterious and a land and they gained in the Sterious and a land and they gained in the Sterious and a land and they gained in the Sterious and a land a land and they gained in the Sterious and a land a

First, I find the Sam of their Stocks, by addit them together, viz. 12 L and 8 L. which are 20 L then according to the Stocks Require 3 L. the total Gain, how much will 12 L. 20 L (the Stock of A) require? I while the ninth Chapply and Divide by the seventh Rule of the ninth Chapply and Divide by the seventh Rule of the ninth Chap

ter, and the Answer is 3 l. for the flare, of A in the

8 L require? The Antwer's a L. which is the gain

8 L'require? The Answer is a l.

B. So I conclude that the share of and the there of B in the 5 5 A # 1 360 Luts

de schadende et 20) 60 (21.

Quality 2. Three Merchants, vir. A, B, and C, enter toon a joint Adventure, A put into the common flock of l. B put in 117 l, and C put in 234 l, and they find when they make up their Accompts) that they have sined in all 264 l. now I define to know each Mans particular flare in the gains?

First I add their particular stocks to the control of their sum is 429 l, then 78 and their sum is 429 l, then 78 and what III lead what will 20 l.

gain? and what 117 /. and what will 234
234 /. (the Stocks of A, B, and C.)
gain? Work by 3 feveral Rules of 3; firm 429
and you will find that

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therein according to his Charge in Building her.

Quest. 4. A, B, and C, enter Partnership for a certain time. A put into the common stock 2641. B put in 4821. C put in 5001, and they gained 8671, nor I demand each mans share in the gain Proportionals to his Stock.

Aufwer, 1. s. d. A (234-09-3-1); B (310-09-5-1); O (322-08-3-1); Sum 867-00-0

g. To prove the Rule of Single Fellowship, add earl mans Particular gain or lost together, and if the total Sum is equal. The Proof of the to the general gain or dolls, then Rule of Single is the Work rightly performed, Fellowship, but otherwise it is erroneous. Example, in the first Question of this Chapter, the Analysis.

ample, in the first Question of this Chapter, the Asser was that the gain of A was 3 l. and the gain of B 2 l. which added together make 5 l. equal to the total gain given.

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If in finding out the particular shares of the several fathers, any thing remain after Division is ended, such remainders must be added together, (they begall Fractions of the same Denomination) and their sim divided by the common Divisor in each Question (viz. the total stock) and the quotient add to the particular gains, and then if the total Sum is equal to the Total gain the work is right, otherwise not.

As in the fourth Question, the Remainders were 354, 62, and 930, which added together make 1346, which divided by 1346, (the Sum of their Stocks) the Quotient is 1 d. which I add to the pence, &c. and the sum of their shares is 867 l. equal to the total

Gain; wherefore I conclude the work is right.

CHAP. XVI.

Double Fellowship.

DOUBLE Fellowship is when several Persons enter into Partnership for unequal time, that is hen every Mans particular stock hath relation to a

aticular time.

2. In the double Rule of Fellowship, multiply each nitular stock by its respective time, and having added the several products together make their sum the stramber (or term) in the Rule of 3, and the total in or loss the second number, and the product of any as particular stock by his time, the third term, and the ath introduct in Proportion thereunto is his particular in or loss, whose product of stock and time is your aird number.

Then repeat (as in Single Fellowship) the Rule of as often as there are Products (or Partners) and a 4 terms thereby inversed are the numbers required.

Queft. 1. A and Bender Partnership, A put in 40 l. 3 months, E put in 75 l. for 4 months, and they

14

gained

Chapque G gained 701. now I demand each mans there in the gains, proportionable to his flock and time? Anfor P A.20 L. B 50 L.

To resolve this Question, I first multiply the store

of A, (viz. 401.) by its time (3 months) and the product is a . . . 120, then I multiply the flock 40 40 of B by its time (viz. 75 by 4) and it produceth 2004 which I add to the Product of A his A 120 B 300 Stock and Time, and the fum is 420. Then by the Rule of a Direct, I fay ; As 420 (the Sum 420 Sum of the products) is to 70 (the total gain) so is 120 (the Product of A his flow

and time) to 20 t. (the fhare of B in the gains.) All

fo much ought each to have for his share.

Quest. 2. A, B, and C, make a Stock for 12 Month A put in at first 3641. and 4 Months after that hen in 40 l. B put in at first 408 L. and at the end of Months he took out 86 l. C put in at first 148 and a Months after he put in 86 1. more, and a month after that he put in 100 % more, and at the end of Months their gain is found to be 1496 1. I define know each mans share in the gains according to flock and time?

First, I consider, that the whole time of the Partnership is 12 Months. Then I proceed to find the feveral products or flock and time as followeth.

A had at first 364 l. for 4 Months, wherefore their Product is

Then he put in 40 l. which with the first Sum makes 404 1. which continued the remainder of the time, viz Months, and their Product is

The Sum of the products of the? flock and time of A is

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Chap. 17. 6

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Quest. 2. Three Grafiers, A, B, and C, take a pier of Ground for 46 l. 10 s. in which A put in 12 Over to for 8 Months, B put in 16 Oxen for 5 months, and c of put 18 Oxen for 4 Months, now the question is, what I shall each man pay of the 46 l. 10 s. for his than in that charge ?

> Answer, a (18-00 fhall pay < 15-00 46-10

3. The proof of this Rule is the fame with that of Single Fellowship, laid down in the stb Rule of the 1d

Chapter; and note that,

If a loss be fustained instead of gain amongst Parners, every mans share to be born in the loss, is to be found after the same method as their gain, whether their Stocks be for equal or unequal time.

CHAP. XVII.

Alligation Medial.

HE Rule of Alligation is that Rule in plun proportion, by which we refolve question wherein is a composition or mixture of divers simple as also it is useful in the composition of Medicines but for quantity, quality, and price. And its species at two, viz. Medial and Alternate.

2. Alligation Medial is when having the fever quantities and prices of feveral fimples propounded ion. we discover the mean price or rate of any quantit now of the mixture compounded of those simples, at wor

the proportion is,

piece As the sum of the simples to be mingled is to the Over total value of all the simples, so is any part or quantity and of the Composition or Mixture, to its mean Rate or whe Price

than Quest. 1. A Farmer mingleth 20 bushels of Wheat at es. per bufhel, and 36 bufhels of Rye at 3 s. per bufhel, with 40 bushels of Barley at 2 s. per bushels, now I defre to know what one bushel of that mixture is worth?

To resolve this Question add together the given quantities and also their values, which is 96 bushels, whose total value is 141. 81. as appeareth by the Work following, for

bush 20 of Wheat at 5 s. per Buffel, is 5-0 36 of Rye at 3 s. per Buskel, is 5-8 40 of Barley at 2 s. per Buskel, is 4-0

The Sum of) the given 96 and their value is to be quantities is

Id

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Then fay by the Rule of a Direct, If 96 Bushels cost (or is worth) 14 1. 8 s. what is 1 Buffel worth ?

Quest. 2. A Vintner mingleth 15 Gallons of Canary at &s. per gallon, with 20 gallons of Malaga at 75. 4d. per gallon, with 10 gallons of Sherry at 6 s. 8 d. per gallon, and 24 gallons of White-wine at 4 s. per gallon, now I demand what a gailon of that Mixture is worth? work as in the last Question, and you will find the Anfwer to be 6 s. 2 d. 2 grs. 45

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Quest. 3. A Grocer hath mingled 3 C. of Sugar at 36 s. per C. with 3 C. of Sugar at 3 L 14 s. 68 d. w. C. and with 6 C. at 1 L 17 s. 04 d. per C. I dele to know the price of a hundred weight of that misture? Answer 2 L 13 s. i.d. 4?

3. The proof of this operation is by the price of any quantity of the mixture to fine The Proof of out the total value of the whole com-Allig. Medial. polition, and if it is equal to the total value of the leveral timples, the

Work is right, otherwise not. As in the first Example, the answer to the question was that 3.5 is the price of one bushel, wherefore I say by the Rule of Proportion, If roushel be 3 stillings, what is 96 bushele Answer 141. 8 1. which is the total value of the several simples, wherefore the Work is right.

CHAP. XVIII.

Alligation Alternate.

Lligation Alternate is when there are given the particular prices of several simples, and there by we discover such quantities of those simples, as being mingled together shall bear a certain rate propounded.

2. When such a question is stated, place the given prices of the simples one over the other, and the propounded price of the composition against them in such fort that it may represent a Root, and they so many branches springing from it as in the following Example

Quest. 1. A certain Farmer is desirous to mix as bushels of Wheat at 5 s. or 60 d. per bushel, with Re at 3 s. or 36 d. per bushel, and with Barley at 2 s. or 24 d. per bushel, and Oats at 1 s. 6 d. per bushel, and defireth to mix such a quantity of Rye, Early and Oats with the 20 bushels of Wheat, as that the whole camposition may be worth 2 s. 8 d. or 32 d. per bushel.

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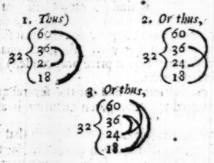
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The prices of the simples being placed according to the last Bule, with the price of the composition propounded as a root to them will stand as followeth.

32 36 36 24 18

2. Having thus placed the given Numbers you are to link or combine the several rates of the simples the and to the other, by certain Arches, in such fort that one that is lesser than the root (or mean rate) may be linked or coupled to another that is greater than the mean rate, so the question last propounded will stand.



4. Then take the difference between the root and the feveral branches, and place the difference of each against the number or branch, with which it is coupled or linked, and having taken all the Differences and placed them as aforesaid, then those differences so placed will shew you the number of each simple to be taken to make a composition to bear the mean rate propounded.

So the branches of the last question being linked to-

gether as in the first manner, I say the difference between 32 and 60, is 28, which I put against 18, because 60 is linked with 18, then the difference between 32 and 36 is 4, which I

 $32 \begin{cases} 60 \\ 36 \\ 24 \\ 18 \end{cases} \begin{vmatrix} 14 \\ 8 \\ 4 \\ 28 \end{vmatrix}$

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put against 24, because 36 is linked or coupled with 24, then I say the difference between 32 and 24 is 4 which I place against 36 (for the reason aforesaid) then I say the difference between 32 and 18 is 14 which I place against 60; and then the Work will

stand as you see in the Margent.

So I conclude that a composition made of 14 bushes of Wheat at 60 d. per bushel, and 8 bushels of Rye a 36 d. per bushel, and 4 bushels of Barley at 24 d. per bushel, and 28 bushels of Oats at 18 d. per bushel, will bear the mean price of 32 d. or 25.8 d. per bushel. And here observe that in this composition there is but 14 bushels of Wheat; but I would missible 20 bushels, and this kind (or rather case) of Alligation Alternate, (viz.) when there is given a certain quantity of one of the simples, and the quantities of the rest sought to mingle with this given quantity, (that the whole may bear a price propounded) is called Alternation partial.

And the proportion to find out the several quantities to be mingled with the given quantity is as fol-

loweth, viz.

As the difference annexed to the branch that is the value of an Integer of the given quantity, is to the other particular Differences, so is the quantity given

to the feveral quantities required.

So here, to find out how much Rye, Barley and Oats must be mingled with the 20 bushels of Wheat, I say by the single Rule of 3 Direct, If 14 bushels of Wheat require 8 bushels of Rye, what will 20 bushels of Wheat require? Answer, 11-2 bushels of Rye.

Again; if 14 bushels of Wheat require 4 bushels of Barley, what will 20 bushels of Wheat require? Answer, 514 bushels of Barley. Again I say, if 14 bushels of Wheat require 28 bushels of Oats what will 20 bushels of Wheat require? Answer, 40 bushels of Oats!

And now k fay, that 20 bushels of Wheat mingled with 11-4 bushels of Rye, and 5-10 bushels of Barley, and 40 bushels of Oats, each bearing the Rates as aforefaid, will make a composition or heap of Corn that may yield 32 d. per bushel.

But if the branches had been coupled according to the fecond order, or manner, the differences would have been thus placed, viz. the differences between 32 and 60 is 28, which I fet against 24, because 60 is linked thereto; and 32 24 28 the difference between 32 and 4 18

36 is 4, which I fet against 18,

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and the difference betwixt 32 and 24 is 8, which I fet against 60; then the difference between 32 and 18 is 14, which I set against his yoke-fellow 36, and then I conclude that if you mix 8 bushels of Wheat with 14 bushels of Rye, 28 bushels of Barley, and 4 bushels of Oats, each bearing the foresaid prices, the whole mixture may be sold for 32 d. per bushel, as by the work in the Margent.

You see by this work we have found how many bushels of Rye, Barley and Oats, ought to be mixed with 8 bushels of Wheat, and to find out how many of each ought to be mixt with 20 bushels of Wheat, I say, as 8 is to 14, so is 20 to 35 bushels of Rye. As 8 is to 28, so is 20 to 70 bushels of Barley. As 8 is to 4, so is 20 to 10 bushels of Oats, whereby I conclude, that if to 20 bushels of Wheat I put 35 bushels of Rye, 70 bushels of Barley, and 10 bushels of Oats, bearing each the foresaid prices per bushel, that then a bushel of this mixture will be worth 32 d. or 2 s. 8 d.

And if the branches had been linked as you fee in the third place, where each branch bigger than the root, is linked to two that are leffer than the root, then in this case you must have placed the several differences between the root and branches, against those two with which each is coupled, as first the difference between 32 and 60 is 28, which I put against 24, and 18 be-

cause it is coupled.

(60	1 .8,14	22
$32 \begin{cases} 60 \\ 36 \\ 24 \\ 18 \end{cases}$	8,14	22
24 2)	28,4	.32.
(18)	2814	32
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Alligation Alternate. Chap. 18

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D94. with them both, then the difference between 32 and 26 is 4, which I fet likewise against 24 and 18, be cause 36 is linked to them both, then the difference between 22 and 24 is 8, which I put against 60 and 26, because 24 is linked to them both, then the difference between 32 and 18 is 14, which I put against 60 and 26, the yoke-fellows of 18.

Laftly, I draw a line behind the differences, and add differences which stand against each branch, and put the Sum behind the faid line against its proper branch,

as you fee in the Margent.

And now by this work I find that 22 buffels of the Wheat mingled with 22 bullels of Rye, and 22 bullet of Barly, and 32 bufflets of Oats, each bearing the find sprice will make a mixture, bearing the mean rates 32 d. per bushel.

And to find how much of each of the reft must be

mingled with 20 buffiels of Wheat, I fay,

As 22 is to 22, fo is 20 to 20 bushels of Rye. 22 je to 32, fo is 20 to 29 1 bufnels of Barly. As 21

is to 23, to is 20 to 29 buffels of Oats.

Whereby you fee the questions of Alligation Alter - pate will admit of more true answers than one for we have found three feveral answers to this fill aneftion.

Questions of Alternation partial are proved the fam way with Questions in Alligation The Proof of Alter- medial which you may fee in the nation partial. 3d Rule of the 17th Chapter.

Quest. 2. A Grocer hath 4 lon of Sugar, viz. of 12d. per l. of 10 d. per 1. of 6 d pa and of 4 d. per l. and he would have a compositi worth 8 d. per l. the whole Quantity whereof flow contain 144 1. made of thele 4 forts, - I' demand to much of each he must take?

Questions of this Nature are resolved by that par of Alligation alternate called by Arithmeticians Alte nation total, wiz. where there is given the fum, an prices of feveral fimples to find out how much of each timple oughts to be taken to make the faid fum quantity Chap. 18. Alligation Aletmant.

quantity, fo that it may bear a certain Rate pro-

pounded.

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To refolve this question I place the several prices of the fimples and mean rate propounded, and link them together, as is directed in the 2 and 2 Rules of this Chapter, and place the differences between the soot and branches according to the 4th Rule of this Chapter, which will then stand one of these three ways, viz.

tirft. Second.

Then add the feyeral differences together, which I have done and the fums of the first and second order are 121. and of the third 241. as you may fee above. but it is required that there should be 144 L of the composition, therefore to find the quantity of each fimple, to make the whole composition 144 1. observe this general Rule, viz.

As the fum of the differences is to the feveral diffeb rendes, plotisthe total quantity of the composition to

to the quantity of each simple.

So to find how much of each fort of Sugar I ought. to take tomake 144 L at 8 d. per L I fay,

As 12 is to 4, fo is 144 to 48 L at 12 d. per l. . As 12 is to 2, So is \$44 to 24 1. at ro d. per l. As 12 is to 2, So is 144 to 24 l. at 6 d. ser l. 12 13 to 44 fo is 144 to 58 1. at 4 d. per l. whereby.

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whereby ind that 48 l. at 12 d. per l. and 24 l. at 10 d. per l. and 24 l. at 6 d. per l. and 48 l. at 4 d. per l. will make a composition of Sugar containing 144 l. worth 8 d. per land make a composition of Sugar containing

but as the branches are linked in the second order, the answer will be 241, at 12d, per 1, and 481, at 1 d, per 1. and 241, at 4 d, per 1. to make the said quantity, and to bear the said price.

And if you had worked as the Branches are linked after the third order, then you would have found the

quantity of 361. of each.

Quest a A Vintner hath 4 forts of Wine, viz Canary at to soper Gallon, Malaga at 8 s. per gallon; Rhenish wine at 6 s. per gallon; and White-wine at 4 s. per gallon, and he is minded to make a Composition of them all of 60 gallons that may be worth 5 shillings per Gallon, I desire to know how much of such has my Character.

each he must have ? The numbers or forms being ranked according to the fecond Rule of this Chapter, the branches will be linked as followeth, and will admit of no other manner of coupling, because there is but one branch that is leffer than the Root, therefore all the rest must be linked unto it; and the in (100) 8 differences between the Root and the three first. branches, viz. 10, B, and 6, which are 5, 3, and I, must be fet a. gainst 4 because they are all coupled with it, and the difference between the Root (viz. 14. Jand 49 which is must be set against the a other, because it is linked to them all; fo I find I gall of Canapy : 1 gallon of

As 12 is to 1, fo is 60 to 5 gallons of Canarya

As 12 is to 1, fo is 60 to 5 gallons of Malaga.

As 12 is to 1, fo is 60 to 5 gallons of Rhenish.

Abv12 is to 9, fo is 60 to 45 gallons of White-wise.

Malaga, 1 gallon of Rhenish Wine, and 9 gallons of White-wine, prized as above being mingled together, will be worth 5 s. per gallon, the Sum being 12 gal-

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So that 5 gallons of Canary, 5 gallons of Malaga, gallons of Rhenish, and 45 gallons of White-wine mingled together, will be in all 60 gallons, worth 5 s. per gallon, which was required.

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Quest. 4. A Goldsmith hath Gold of a several forts of finencis, viz. of 24 Careas fine. and of 22 Careers fine, of 20 Careers Read Chap. 2. fine, and of 15 Carells fine. And diff. 2. of this he would mingle fo much of each with alloy, that the whole Mass of

28 ounces of Gold so mingled may bear 17: Carells fine in demand how much of each he must take. the fecond and third Rules of this Chapter being obkreed, (for instead of the alloy I put o, because it bears no fineness, but it makes a branch in the Operation) the terms may be alligated and the differences.

added any of these 4 ways following, viz.

First thus, Sum 56 Secondly thus. 20. Sum 56

Thirdly thus, 2,

Sum 41

Fourthly,

Fourthly thus,

24
22, 17, 19
22, 17, 19
23, 17, 19
7,5 3 15
7,5 3 15

Sum 187

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More ways may be given for the Alligating, or linking of the Terms in this Question, but these are sufficient for the industrious, and it shall also suffer to give an answer to the question as the terms are link'd the first way, not doubting but the ingenior practitioner will be able at his science to find Answer to the other 3 ways, viz.

As 56 is to 17, so is 28 to 8 10 of 24

As 56 is to 2, so is 28 to 10 00 of 22

As 56 is to 19, so is 28 to 0 10 00 of 20

As 56 is to 18, so is 28 to 4 00 of 15

As 56 is to 10, so is 28 to 4 00 of 15

Thus much well practiced and understood is sufficient and on the second of the

cient for the understanding of Alligation.

In questions of Alternation Total,
the Answer given is true, when the The proof of A
sum of each of the quantity of ternation Total
fimples found, agrees with the Sum
or Quantity propounded; as in the last Question, the

or Quantity propounded; as in the last Question, the Answer was 8.07. 10 p.m. of 24 Carects fine, 10 a of 22 Carects fine, 9.07. 10 per of 20 Carects fine, 407. of 15 Carects fine, and 5 of Alloy, which add together make 28.02. the quantity propounded.

CHAP. XIX.

Reduction of Vulgar Fractions.

feveral kinds, hath been already thewed the 19, 20, 21, 22, 23, 24, and 31 definitions of the

first Chapter of this Book, which the Learner is desi -

red diligently to observe before he proceeds.

2. To reduce a Vulgar Fraction (which discovereth the principal knowledge of Fractions, and therefore ought greatly to be regarded) we shall discover plainly under these eight several heads (or Rules) following, viz.

1. To reduce a mixt number into an improper Fra-

aion.

fine

2. To reduce a whole Number into an improper Fraction.

3. To reduce an improper Fraction into its equi-

valent whole (or mixt) number.

4. To reduce a Fraction into its lowest terms equi-

5. To find the value of a Fraction in the known

parts of Coyn, Weight, Meafare, Voc.

6. To reduce a compound Fraction to a simple one of the same value.

7. To reduce divers Fractions having unequal denominators, to Fractions of the fame value, having an equal Denominator.

8. To reduce a Fraction of one denomination to

another of the same value.

I. To reduce a mixt Number to an improper Fradion.

The Rule is,

Vide Chap. 1. defin. 31.

Multiply the Integral part (or whole Number by) the denominator of the Fraction, and to the Fraction add the Numerator, and that Sum place over the Denominator for a new Numerator; so this new Fraction shall be equal to the mixt Number given. As for Example.

the whole number 18 by 7 the denominator, and to the Product add the numerator 3, the fum is 129, which put over the denominator, and it makes 139 for the

answer as followeth.

7 facit

1.60

129·

2. Reduce 183 1 to an improper fraction, facit 3. Reduce 5613 to an improper fraction, facit 1119

II. To reduce a whole Number to an improper Fraction.

The Rule is,

Multiply the given Number, by the intended denominator, and place the Vide Chap. 1. product for a numerator over it. As defin. 23. for Example.

1. Let it be required to reduce 15 into a Fraction whose denominator shall be 1.2.

To effect which, I multiply 15. 15. by the intended denominator 12 (12) the product is 180, which I place over 12 as a numera-30. tor, and it makes 180 which facit 1 % o is equal to 15, as was required; as per Margent. 180

2. Reduce 36 into an improper Fraction whole denominator shall be 26, facit 935.

2. Reduce 125 into an improper Fraction, whole denominator shall be 16, facit 1159.

III. To reduce an improper Fraction into its equivalent whole or mixt number ..

The Rule is,

Divide the Numerator by the Denominator, and the Quotient is the whole number equal to the fraction, and if any thing remain, put it for a Numerator over the Divisor. Example, 1: Reduce

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1. Reduce 436 into its equivalent mixt numberdivide the Numerator 436 by the denominator 8, and the Quotient is 543 and 4 remains, which put for a Numerator over the Divisor 8, the Answer is 542 as followeth.

8) 436 (54

facit 541 36'

2. Reduce 3475 to a mixt number, facit 23111:

3. Reduce 11175 to a mixt number, facit 114772

IV. To Reduce a Fraction into its towest terms equivalent to the Fraction given.

The Rule is,

1. If the numerator and denominator are even numbers, take half of the one, and half of the other as often as may be, and when either of them falls out to be an odd number, then divide them by any number that you can discover will divide both numerator and denominator without any Remainder; and when you have thus proceeded as low as you can reduce them, then this new Fraction so found out shall be the fraction you defire, and will be in value equal to the given Fraction. Example.

1. Let it be required to reduce 133 into its lowest

terms. First, I take

the half of the Numerator 192 and it is 96,
then half of the De-

mminator and it is 168, so that now it is brought to 181, and next to 48, and by halfing still to 24, and their half is 13, and now I can no longer half it, because 21 is an odd number, wherefore I try to divide them by 3, 4, 5, 6, 8c. and I find 3 divides them both without any remainder, and brings them to 4 as per Margent.

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There is yet another way more excellent than the former to reduce a fration into its Vide Ought. Cla. lowest terms, and that is by finding a common Measurer, viz. the grea- Matth. cap, 7. test number that will divide the

162

numerator and denominator without any remainder, and by that means reduce a fration to its lowest terms at the first work; and to find out this common measure divide the denominator by the numerator, and if any thing remains divide your Divisor thereby; and if any thing yet remains, then divide your last Divisor by it do fo until you find nothing remains; then this lift divisor shall be the greatest common measurer, which will divide both numerator and denominator, and reduce them into their lowest terms at one Work.

4. Reduce 32 into its lowest terms by a common measurer. To effect which I divide the denominate 204 by the numerator 228 and there remains 76, the I divide 228 (the first Divisor) by 76 (the Remainder) and it quotes 2, and nothing remains; wherefore the last Divisor 76 is the common measurer, by which divide the numerator of the given Fradion, viz. 221, it quotes 3 for a new numerator, then I divide the denominator 304 by 76 and it quotes 4 for a new dem minater, so that now I have found a equal to 328.

5. Reduce 5048 into its lowest terms by a comme measurer, facit -?

6. Reduce 1041 into its lowest terms by a conmon measurer, facit 13.

A Compendium. Note that if the numerator and denominator of a fin Gian, and each with a Cypher or Cyphers, then of off as many Cyphers from the one as from the other, and the remaining figures will be a fraction of the same value, viz. 1400 will be found to be reduced to

by cutting off the 2 Cyphers from the numerator and denominator, with a dath of the Pen, thus, 341.3, and 350, will be 35 thus 350. Ge.

V. To find the Value of a Fraction in the known parts of Coyn, Weight, &c.

The Rule is,

Multiply the numerator by the parts of the next inferiour denomination that are equal to an Unit of the fame denomination with the Fraction, then divide that Product by the denominator, and the quotegives you its value in the same parts you multiplied by, and if any thing remain multiply it by the parts of the next inferiour denomination, and divide as before, do so till you can bring it no lower, and the several quotients will give you the value of the fraction as was required, and if any thing at last remain, place it for a numerator over the former denominator, some sew Examples will

make the Rule plain.

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1. What is the value of \(\frac{3}{3}\) l. Sterling? To answer this Question I multiply the numerator 27 by 20 (the shillings in a pound) the product is 540, which I divide by 29 (the denominator) and the Quotient is 18 s. and there remains 18 which I multiply by 12 pence, and the product (216) I divide by the denominator 29, the Quotient is 7 d. and 13 remains, which I multiply by 4 farthings, the product is 52, which I still divide by 29, the Quotient is 1 Farthing, and there remaineth 23, which I put for a Numerator over the denominator 29, so I find the value of \(\frac{2}{3}\) l. to be 18 s. 7 d. 1 qr. \(\frac{2}{3}\), as by the following Operation, and after the same manner are the values of the fractions in the several examples following found out.

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All 27 and and art 1023 to a chief of the state of the st

29) 540 (18 £

Remains (18)
Multiply 12

36

29) 216 (74.

Remains (13)

29) 52 (113

29

Remains (23) * s. d. qr. Facit 18—7—1¹³/₂

2. What is the value of 11 l. Sterling? facit 145.8 d.

3. What is the value of 13 l. Sterling? facit 4 s.

1 d. 13.

4. What is \(\frac{1}{2}\) \(\frac{1}{2}\) \(C.\) weight ? facit 3 qrs. 1 l. 3 oz. \(\frac{7}{2}\) \(\frac{1}{2}\) \(\fra

6. What is \$! of a year ? Answer, 299 da. 7 h.

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7. 7.

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VI. To Reduce a compound Fraction to a simple one of the fame value.

What a compound Fraction is, hath been shewed in Chap. 1. Definition 24, and to reduse it to a fimple Fraction of the fame value.

The Rule is.

Multiply the Numerator continually, and place the last product for a new Numerator, then multiply the Denominators continually, and place the last product for a new denominator. So this fingle Fraction shall be equal to the compound Fraction given. Example.

1. Reduce of 1 of 1 to a fimple Fraction.

. Multiply the Numerators 2, 3, and 5, together, they make 30 for a new Numerator; then I multiply the denominators 3, 5, and 8 together, and their product is 120 for a denominator, so the simple Fraction is and cutting off the Cyphers it is 13 equal to 1 by the fourth Rule foregoing.

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	he mailty referrations at
and the estate	Demonination, 5, 6-
15 bruet) oba 6	which is a "Inmerator,
	is equal to the articles
	THE TOTAL OF BY WORLD
120 30	that our a printer

Facit -10 or +1 or

2. What is -? of 5 of \$ of 11? Answer, 1540 or 154 or 37 in its leaft terms,

3. What is 11 of 13 of 11 ? Answer, 3003.

By this you may know how to find the value of a Compound Fraction, viz. first reduce it to a simple one, and then find out his value by the 5th Rule foregoing.

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Example.

What is the value of \$ of \$ of a pound?

VII. To reduce Braffions of unequal Denominators is Fractions of the same Value, having equal Denominators.

The Rule u,

Multiply all the Denominators together, and the Product thall be the Common Denominator. The multiply each Numerator into all the Denominator except its own, and the last Product put for a Numerator over the Denominator found out as before: So this new Praction is equal to that Fraction, whole Numerator you multiplyed into the faid Denominanators. Do so by all the Numerators given, and you have your defire.

Example.

1. Reduce 1, 4,8, and 2 to a common Denominator Multiply the Denominators 4, 5, 6, and 8, together continually, and the product is 960 for the common Denominator; then multiply the Numerator 3 into the Denominators, 5, 6, and 8, and the product is 720, which is a Numerator to 960 (found as before) fo 71 is equal to the first Fraction 1, then I proceed to find a new Numerator to the fecond Fraction, viz. 4, and I multiply 4 (into all the Denominators except its own; viz.) into 4, 6, and 8, which produceth 268 equal to 4, then multiply the numerator 5 into the denomintors 4, 5, and 8, the product is soc equal to 3. Then multiply the Numerator 7 into the Denominators 4, 5, and 6, the product is \$40 equal to 2, and the work is done; fo that for 3, 4, 5 and 2, I have 220, 268, 300 340

2. Reduce 11, 14, and 12 into a common denomi-

nator, faciunt 53,3, 3538, and 5244.

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VIII. To reduce a Fraction of one Denomination to another.

t. This is either Ascending, or Descending. Ascending when a Fraction of a smaller is brought to a greater Denomination, and Descending when a Fraction of a greater Denomination is brought lower.

2. When a Fraction is to be brought from a leffer to a greater Denomination, then make of it a Compound Fraction by comparing it with the intermediate Demoninations between it, and that you would have it reduced to, then (by the 6th Rule foregoing) reduce your Compound to a simple Fraction, and the Work is done. Example:

Quest. r. It is required to know what part of a pound Herling 4 of a peny is !

To refolve this, Teenfider that 1 d. is 1; of a fittle ling, and a fittling is 1 of a pound; wherefore 4 d. is 1 of 1 of 1 of 2 of a pound, which by the faid 6th Rule lind to be 1 of 1 ferfine of Enelish Money.

find to be to of a l. sterling of English Money.

Quest. 2. What part of a pound Troy weight is of a penny weight?

Answer, of to of the equal to

3. When a Fraction is to be brought from a greater to a leffer denomination, then multiply the Numerator by the parts contained in the feveral denominations betwirt it; and that you would reduce it to; then place the last product over the denominator of the given Fraction. Example,

Quest. 3. I would reduce \$1. to the Fraction of a Peny; to do which I multiply the Numerator 3 by 20 and 12, the product is 720, which I put over the Denominator 5, it makes 710 of a peny, equal to \$1.

Quest. 4. What parts of an Ounce Trey is - 4.?

CHAP. XX.

Addition of Vulgar Fractions.

I. IF your Fractions to be added have a common Denominator, then add all the Numerators to gother, and place their fum for a Numerator to the pu common Denominator, which new Fraction is the Sum of all the given Fractions; and if it be improper, reduce it to a whole or mixt Number, by the 24 Rule of the 19th Chapter.

Quest. a. What is the Sum of 150, 17, 16, and The Denominators are equal, viz. every one is 24 wherefore add, the Numerators together, viz. 7, 5

16 and 14, their Sum is 46, which put over the Ds nominator 24, it makes of the Sum of the given Fre ctions, which will be reduced to the mixt Number

121, or 121

2. But if the Fractions to be added have uneque Denominators, then reduce them to a common De nominator by the 7th Rule of the 19th Chap, at then add the Numerators together, and put the Sun over the common Denominator. over the common Denominator, Gre. as before in the last Example.

Quest. 2. What is the Sum of 1, 2, 7, and 11?

Quest. 2. What is the Sum of 1, 2, 12, and 11.

The Fractions reduced to a common Denominator lie

13. 41. 3, 41. 3, 41. 3, and 44. 3, the Sum of their are 4100, 4100, 4120, and 4400, the Sum of the Numerators is 15800, which put over the common Denominator, makes 15800 or 158 equal to the min number 314, or 32 for the Sum required,

Quest 3. What is the Sum of 13 23 and 14? At

2. If you are to add mixt numbers together, the nice add the fractional parts as before, and if their Sum be an improper Fraction reduce it to a mixt number, and add its Integral part to the Integral parts of the and given mixt Numbers, and the Work is done.

Queft.4. What is the fum of 133 and 245?

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First add the fractions and &, the fum is 122, then this Integer 1, to 13 and 24, their fum is 38, d put after it the fraction 1 it is 3813 for the Anfw. it is 38%.

Quefl. 4. What is the Sum of 481, 645 and 1301! uit 243 180, Or 24345

BORT 4. If any of the Fractions to be added is a Coms toand Fraction, it must first be reduced to a simple the action by the 6th Rule of Chapter 19, and then add whe reft according to the 2d Rule of this Chapter, ample.

Quift. 6. What is the Sum of 1, 1, and ? of 3 of 3? Reduce 2 of 2 of 1 into a simple fraction, and it is which reduced with the other two, and added 14686

Quife. 7. What is the Sum of 11 and 3 of 4 of 1? wer, 1-5.

mber 5. If the fractions to be added are not of one depination, they must be to reduced, and then proed as before.

Quift. 8. What is the Sum of 31. and 35?
Of the given fractions here, one is of a pound and nadd them rogether, you must reduce & s. to the ction of a pound as the other is (by the 8th le of Chapter 19) and it makes + 11. then 11. and " will be found to be 180 L or 18 L by the 7th le of Chapter 19, and in its lowest rerms 19% by e 4th Role of Chapter 19.

It would have been the fame, if (by the latter part the 8th Rule of Chapter 19) you had reduced 1/2, the traction of a shilling, which you would have nd to have been . . which added to . t. by the Tith Rule of the last Chap. the Sum is 155. 33 nich is equal to the Sum found as before, viz. (by the sth Rule of Chapter 19) the value of 14 1. be found to be 15 5. 10 d. and fo will 15'5. 20 be

and to be just as much.

Queft. 9. What is the Sum of \frac{1}{5} l. \frac{3}{5} s. and \frac{3}{5} d \frac{1}{15} fwer \frac{3}{5} \frac{7}{5} \frac{5}{5} \cdot \text{or} \frac{3}{5} \frac{7}{5} \frac{1}{5} \cdot \text{or} \frac{1}{5} \frac{1}{5}

CHAP. XXI.

Substraction of Vulgar Fractions-

Fractions to one denomination, are here to observed; for before Substraction can be made, the stions must be reduced to a common denominator, is substract one Numerator from the other, and place remainder over the common denominator, which frast hall be the excess or difference between the practions. Example,

Quell. 1. What is the difference between \(\frac{1}{2}\) and \(\frac{1}{2}\), then firatt the numerator 20 from the numerator 21, and in remains 1, which being put over the disaminator makes \(\frac{1}{2}\) for the answer or difference between \(\frac{1}{2}\)

Skell. 2. What is the difference between & a of 4?

Reduce the compound fraction of to a fine fraction, then proceed as before, and the aniwe

ado equal to 11.

2. When a fraction is given to be substracted from whole number, substract the numerator from the dense tor, and put the remainder for a numerator to the given mominator, and substract an Unit (for that you borrow from the whole number, and the remainder place fore the fraction found as before, which mixt number the remainder or difference fought. Example,

Quest. 3. Subtract -? from 48.

Anjar. 47-3; for if you subtract 7 (the numeral from 10 (the denominator) there remains 3, which over 10 is -3 and 1 (I borrowed) from 48 rests 4 to which join -3 and it makes 47 -3 for the excess.

Quest. 4. Subtract 13 from 57, remains 56 31.

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3. If it is required to Subtratt a fraction from a ixt number, or one mixt number from another, educe the fractions to a common denominator, and if he fraction to be subtracted se lesser than the other, en fabrraft the leffer numerator from the greater, and at is a numerator for the common denominator : hen fubtract the leffer integral pare from the greater, d the remainder with the remaining fraction thereto' mexed, is the Difference required between the two iven mixt numbers. Example,

Quit. 5. Subtract 26 3 from 54 5. mainder is $\frac{17}{42}$, then 26 from 54 remaineth 28, to which annex $\frac{1}{42}$, it makes $28\frac{17}{42}$ for the Answer.

4. But if the frattion to be subtracted is greater than e Fraction from whence you subtract, then having off reduced the Fractions to a common denominator, ake the numerator of the greater Fraction out of the enominator, and add the remainder to the humerator the leffer Fraction, and their Sum is a new numefor to the common denominator, which fraction ote, then (for the I you borrowed) add I to the Ineral part to be subtracted, and subtract it from the reater number, and to the remainder annex the 174tion you noted before, so this new mixt number hall be the difference fought, Example,

Queft. 6. Subtract ra ! from 29 4.

S.

The fractions reduced are, viz. 3 equal to 31, and equal co 18, now I should subtract 18 from 18, but I rannot, therefore I fuberact 21 from 28 refts 7, which added to 16 (the leffer numerator) makes 23 for a numerator to 28; vit. 21, then I come to the Integral parts 14 and 29, and fay I that I borrowed and 14 Te, which taken from 29 there refts 14, to which antexing 1 it is 1421 for the remainder or diffetence between 14 3 and 29 4.

Queft. 7. Subtratt 36 -? from 74 4 facit 37 4.

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CHAP. XXIL

Multiplication of Vulgar Fractions.

1. TF the Multiplicand and Multiplier are fimple (a fingle) Fractions, then multiply the numerate together for a new numerator, and the denominator for a new denominator, which new Fraction is the product required.

Queft. 1. What is the product of 1 by -?? facil For the numerators 5 and 9 being multiplyed m 45, and the denominators 7 and 11 being multiply

make 77.

Queft. 2. What is the product of 18 by 31? fa. 2. If the Fractions to be multiplyed are mixt num bers reduce them to improper Fractions by the il Rule of the 19th Chapter, then proceed as before,

Quefl. 3. What is the product of 487 by 138?

The given mixt numbers being reduced to improve fractions are 48 \(\frac{1}{2}\) equal to \(\frac{1}{2}\), and \(13\)\(\frac{1}{2}\) equal to \(\frac{1}{2}\) now 14 multiplyed by 13 according to the first B of this Chapter, produceth 2015? or 6727.

Quest. 4. What is the product of 430 to by 184

Meit 555474 or 793574.

3. If a compound Fraction is to be multiplied by fimple Fraction, first reduce the compound fraction into a fimple fraction, then multiply the one by the other, as is taught above.

Queft. 5. What is the product of 15 by 3 of 5 of 1 the Compound Fraction 4 of 5 of 4 reduced is 75.00 which multiplyed by 15 produceth 25 which it

its lowest terms is 15 for the Answer.

And if the Multiplicand and Multiplyer are both compound fractions, reduce them both to fimple ones then multiply these new fractions as before, so have you the product.

Quefl. 6. What is the product of 1 of 2 by 1 of 1?

Auswer, 13 in its lowest terms 1. Quest. 7. What is the product of 2 of 2 by 3 of 1? ANW. Anfm. 360 or 36, or in its leaft terms 3.

4. If a Fraction be to be multiplyed by a whole number, put under the given whole number an Unit or a Denominator, whereby it will be an improper Fraction, then multiply these Fractions as before. ple (a Example.

Quift. 8. What is the Product of 24 by $\frac{2}{3}$?

Inaura Anfin. $\frac{4}{3}$, for 24 by putting an Unit under it will is the be $\frac{24}{3}$, and $\frac{24}{4}$ by $\frac{3}{4}$ produceth $\frac{4}{3}$ or 16.

Quelt. 9. What is the Product of 36 by -?? Answer,

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CHAP. XXIII.

Division of Vulgar Frattions.

If the dividend and the Divisor are both simple Fractions, then multiply the numerator of the dividend into the denominator of the divitor, and the product is a new numerator, and multiply the denominator of the Dividend into the Numerator of the Divisor, and the product is a new Denominator, which new Fraction thus found, is the Quotient you defire. Example.

Queft. 1. What is the Quotient of & divided by 3?

Anim. 15 or 111, for if I multiply (5) the Numerator of the Dividend into (5) the denominator of

the Divisor, and the product (25) is anumerator for the Quotient, then I multiply (8) the denominator of the dividend into (3) the numerator of the Divisor, and the product (24) I put in the quotent for a denominator, fo I find at is the quotient fought.

Quest. 2. What is the quotient of 10 divided by 2?

Anfw. equal to in its lowest terms.

2. But if you would divide a fimple Fraction by a compound, or a compound by a fimple, first reduce

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fuch compound to a simple Fraction, then go on before, yell

Quest. 3. What is the quorient of +3 divided by of 3? Answer 30 or 3, first reduce \$4 of 3 into a ple Fraction, and it is +5, by which - being divide the Quotient is 36 equal in its least terms to And if the Dividend and Divisor be both compound Fractions, reduce them both to simple Fractions, the divide the one by the other as in Rule I beforego

Quest. 4. What is the Quote of 2 of 1 divided

of s?

Anfw. 180 or 18 or 1 or 11 in its loweft term 3. If the Dividend, or Divitor, or both are numbers, reduce them to improper Fractions, perform Division as you were raught before. Exam

Quist. 5. What is the quote of 122 divided by a Answ. 255, for 122 is equal to 4 and 214 is eq to 10%, and the quote of 54 divided by 10% is as

fore 355.

4. If you divide a Fraction by a whole number, a whole number by a Fraction, make the whole ne ber an improper Fraction by putting an Unit for a nominator to it as was taught in Rule 4. of Chap. and then perform Division as before was taug Example.

Quift. 6. What is the Quote of 8 divided by 31

Anja. 49 which is equal to $13\frac{1}{3}$ being reduced as is be- $\frac{3}{5}$ $\frac{8}{1}$ $\frac{40}{3}$ or $13\frac{1}{5}$ in the Margent.

Queft. 7. What is the Quotient of 3 divided by 8? Anfwer and as per Margent.

CHAP. XXIV.

The Rule of Three Direct in Vulgar Fractions.

A Sin the Rule of 3 in whole Numbers, fo likewife in Fractions, you must see that the Fractions of the first and third places be of the same denomination.

2. See that if any of the given Frattions be comfound, that they be reduced to fimple of the fame

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2. If there are given mixt numbers, reduce them to improper Fractions by the first Rule of Chap. 19.

4. If any of the three terms is a whole number, make it an amproper Fraction by constituting a Unit

for its dinominator.

Having reduced your Frattien as is directed in the 4 last Rules, then proceed to a Resolution which is performed the same way as in whole numbers, refeed being had to the Rules delivered for the working of Exactions, viz. multiply the 2d and 3d Fraction together, according to the I Rule of Chap. 22. and diside the product by the first Fraction, according to the 1 Rule of Chap. 23. and the Quotient is the Answer.

Or (which is better) s. Multiply the numerator of the first Fraction into the denominators of the fecond and third, and the product is a new denominator, then multiply the denominator of the first Eraction into the numerators of the second and third, and the product is a new numerator; which new Fraction is the 4th Proportional or answer. which (if it is an improper Fraction) must be reduced to a whole or mixt number by the third Rule of Chap. 19. Examples,

Quest. 1. If 3 yards of Cloth cost & 1. what will

yds coft ?

Having placed the given Fractions, according to the 6 Rule of Chap. 10. I proceed to the resolution, and first I multiply the numerator of the first Fraction (3)

Quest. 4. If \$ of an Ell of Holland cost \$ d pound, how much will 123 ells coft at that rate ? Anfiver, -30 equal to 7371.

In refolving the last question, and the two next, of ferve the Third Rule of this Chapter foregoing.

Queft. 5. If - of a C. coft 284 s. what will 7 10 coft at that rate?

Anjwer, 239-7 s. or 11 l. 19 s. 7 d.

Queft. 6. If 34 yards of Velver coft 35% how mud will Ic 2 yards cost at that rate?

Anfwer, 1117 1.

Queft. 7. If 3 y/s of Broad Cloth coft 24 1. what will 143 yds coft? 767

Answer, 136 9 s. 4 d.

In working the last question and the 4 next, observe the 4 Rule of this Chap. foregoing.

Queft. 8. If 14 1. of Pepper cost 14 s. 63 d., I de

mand the price of 733 % Answer, 31. 16 5. 733 d.

Quest. 9. If 11. of Cochenele cost 11. 93. what will 35-21. coft?

Answer, 45% 175. 6 d.

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Queft. to. If one yard of bread-cloth coft 15% s. what will 4 pieces, each containing 27% yards at that fate?

Anfwer, 85 l. 14 s. 33 d.

Quest. 11. A Mercer bought 31 pes of filk, each pe qu 243 ells at 6 s. 03 d. per Ell, I demand the value of 31 pes at that rate?

Anfroer, 26 l. 3 s. 44 d.

In folving the 4 next questions observe the 8. Rule

Queft. 12. If 3 of an ounce of Silver coft 2 5. I

demand the price of 113 1. at that rate?

Answer, 35 l.

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ł.

Quest. 13. If 525 l. of Gold is worth 6141. Sterling, what is I grain worth at that rate?

Answer, 11 d.

Quest: 14. If 2 yds of Silk is worth 2 of & i. what is the price of 153 El's Flemish?

Anfwer, 9 l. 12 s. 6 d.

Quest. 15. If 3 of 3 of a pound of Cloves cost 6 s.

Anfwer, 69 L 6 s. 8 d.

Note that when the Answers to the Questions is this and the next Chap, are given in Fractions, they are given in their lowest Terms.

CHAP. XXV.

The Rule of Three Inverse in Fractions.

Thath veen already raught (in the third Rule of the 11th Chap.) how to discover when the 4th proportional number (to the 2 given numbers) is to be found out by a Rule of 3 Direct, and when by a Rule of Three Investe, to which Rule the Learner is now referred.

2: When (in Fractions) you find a question to befolved by the Rale of 3 Inverse, viz. when the third Term is the Divisor, then (having reduced the terms

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173 The Rule of Three, &c. Chap. 16.

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exactly according to the Rules in Chap. 24.) multiply the numerators of the 3 Fractions into the denominators of the second and first Fractions, and the Product is a new Denominator, then multiply the denominator of the third Fraction into the numerators of second and first Fractions, and the product is a new numerator, which new traction thus found is the answer to the question.

Quest. 1. If 3 of a yard of Cloth that is 2 yds wide will make a Garment, how much of any other Drapery, that is 3 of a yard wide will make the fame

Garment?

Answer, 2 1 yds.

Quest. 2. Lent my Friend 46 L for 3 of a yer, how much ought he to lend me for 3 of a year?

Anfwer, 63 3 1.

Quest. 3. If 3 of a yard of Cloth that is 2 1 ju wide will make any Garment, what breadth is the Cloth, when 1 3 yas will make the same Garment?

Answer, 53 of a ya wide.

Quest. 4. How many inches in length of a board that is 9 Inches broad will make a Foot square?

Answer, 16 inches in length.

Quest. 5. If when the bushel of Wheat cost 4 to the penny Loaf weigheth 10? Ounces, what will weigh when the bushel cost 8 - 9 s.?

Anfwer, 51 45 Ounces.

Quest. 6. If 12 Men can mon 24 2 Acres in 10 days, in how many days will 6 Men do the same?

Auswer, In 21 days.

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ted as we have about a local Ha verseo tamed ach at rou and and al Rules of Practice. on I de stall

1. IN the fingle Rule of (3, when the first of the 3 Numbers in the Question fafter they are disposed according to the 6th. Rule of Chap. 101) happen

to be an Unit (or 1) that Question many times may be resolved far more speedily than by the Rule of 3, which kind of Operation is commonly called Practice, and indeed it is of excellent use amongst Merchants, Fradesmen and others, by reason of its speedings in finding a resolution to such kind of Questions.

2. The chiefest Question resolvable by these brief Rules may be comprehended under the several gene-

sal heads or cases following, viz.

When the given
Price of the Iuteger confiss,

6 Of pence and farthings
4 Of shillings under 20
5 Of (hillings, pence and farthings
6 Of Pounds
7 Of pounds, (billings, pence and farthings.)

Arithmetician to have by heart the feveral products of the Nine Digits multiplyed by 12, for his speedy reducing pence into shillings, or shillings into pence, which he may gain by the following Table.

3. Shillings are practically reduced into pounds thus, viz. cut off the figure standing in the place of Units with a dash of the pen and note it for shillings, then draw a line under the given Number, and take

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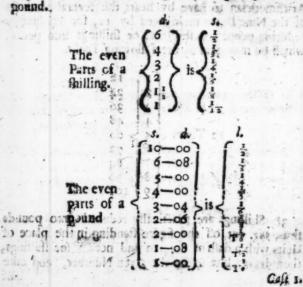
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half of the remaining figures (after the first is cut off) and fet them under the line, and they are so many pounds, but 4365 8 if the last figure is odd, then take the leffer half, and add to to the figure fo cut off (as before) for 2182 18 shillings, as if I were to reduce

426 48 shillings into pounds, first I cut off the last ngure (8) for shillings, then I take half of the remaining figures (4365) thus half of 4 is 2, which I put under the line, then 1 of 3 is 1, and because 3 is an odd number. I make the next figure 6 to be 16. and I go on, faying, 1 of 16 is 8, and then 1 of 5 is 2, which is the last figure, wherefore because s is an odd member, I add 10-10 the & I out off, and it makes 183, fo that I find it to be 2182 4- 18 3. as per Margent.

4. It is likewise convenient that the Learner be acquainted with the practical Tables following, the first containing the Aliquot (or even) parts of a shilling, the fecond containing the Aliquot parts of a



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Gufe 1.

4. When the price of the Integer is a Parthing, then take the fixth Part of the given Number, which will be so many three half-pences, and if any thing Bemains it is Farthings, by the 7th Rule of Chap. 9. then consider that three half-pence is i of a shilling, wherefore take the eighth part of them for shillings, and if any thing remain they are fo many a half-pence, which reduce into pounds by the Third Rule foregoing Example, What comes 67486 1, to at a Farthing per 1. First, I take of 67486 and it is 11247 three half-pence and 4 farchings, or one peny; then i of 11247 is 1405 s. and 7 remains, which is 7 three halfpence, or 101 d. which with the 4 farthings before make 11 d. and 1405 fhillings, which by the 3 Rule is 706 5 s. In all 701. 5s. 11 d. for the Answer. See the Work following.

Other Examples follow.

+ 318	3576 t. at	1 q1.	or aprile	5380 l. al	1970
1	1420	2 qui	wheel wheel	1063	a grs.
128	1718-	8 d. 220	10	13721	11 de
6113	1. 9.	d.		1. 's. 6—12—	d.
1, 1	8-13-	-8 facit	S. S. F. B.	6-12-	. When

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6. When the price of the Integer is 2 farthings, then take the third part of the given Number for so many three-half-pences, and the Remainder (if any) is half pence, then take the eighth part of that for shillings, cace ene fixen Pare

1 83471. at 2
2782 29
of the same of the same of
59102 To 341

7. When the price of the Integer is 3 farthings then take half the given Number for three halfpence, (and if any thing remain it is a farthings) then take the eighth of that for shillings as before, ever

1 1	4736 l. at 3 q	Examples.	5425 L at 3 grs.
1 8	2368	1000	2712 3 qrs.
1 20	2916	101-0130	3319
	1. s. 14 — 16 faci	11 -2 -01	1. s. d. qrs. 16-19-0-3 fa

Cofe 2.

8. When the given price of the Integer, is a part, or parts of a shilling (viz. pence) divide the given Number of laregers (whose value is sought) by the Denominator, of the fraction representing the even part, and the quote is shillings, (always minding the 7th. Rule of the 9th. Chap.) and those shillings may be reduced into f. by the 3d. Rule of this Chapter. Examp. Let it be required to find the value of When

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438 l. at 3 d. per l. I confider 3 d. is 4 of a fhilling, and 438 l. will coff to many 3 pences, wherefore I divide 438 by 4 the denominator of 4, and the quote is 109 shillings, and a remains, which is a three pences or 6 d. the whole value is 3 l. 9 s. 6 d. as by the following work appearents.

More Examples follow.

1. d. 3574 at 6 per l.	1. d. 5316 at 2. per t. :
178[7	Ex 6188
facit 89 1. 7's.	facit 44 l. 6 s.
1. d. 13 438 at 4 per l.	1 6389 at 1 per l. 1 7918 7 d. 1 facit 39 l. 185. 7 d. 1
1416.	1 7918 - 7 d. 1
facit 7 L 6 s.	facit 39 l. 18s. 7 d. 13.
1. d. 879 at 3 per L	1. d. 818 at 1 per l.
1 2119- 9 d	
Jacit 10 l. 19 s. 9 d.	facit 3 l. 8 s. 2 d.

9. If the price of the Integer be pence under 12, and yet not an even part, then it may be divided into even parts, and so the parts of the given Number taken.

184

ken accordingly, and added together, as if it were ed which is 2 d. and 2 d; viz. 2 and 2 of a fhilling, first take 4 of the given number, and then & thereof and add them together, and their Sum is the Answer in shillings, still observing Rule 7. of Chap. 9. for the remainders, (if any be) then bring the shillings into pounds by the 3 Rule foregoing. Likewise 7 d. is 1 and 1, fo 9 d. is 1 and 1, and 10 d. is 4 and 4, and It d. is 1 and 1 and 1 of a shilling, or elie many times your work may be shortned thus, viz. when the faid given price is to be divided into even parts of a shilling or of a pound, after you have taken the first even part, the other may be an even part of that part, as in the next Example, where is given 439 l. at 5 d. per l. now I may divide it thus, viz. into 4 d. and 1 d. and 4 d. being \(\frac{1}{3} \) of a shilling, and 1 d. being \(\frac{1}{4} \) of 4 d. I first take \(\frac{1}{3} \) of 430 l. and it gives 146 s. 4 d. and for the 1 d. I take 1 of 146 s. 4 d. which is 36 s. 7 d. which in all comes to 9 t 2 s. 114

Examples follow. yds. d. 417 at 9 per yd 439 at 5 per l. 146-208---6 104-1812-11 3112-9 91. 25. 11 d. facit 151. 125. 9d. facit ells d. ells d. 587 at 7 per Ell 386 at 10 1195-1 146 -128--8 161. 1 s. 8 d. facit 171. 25. 5d. facit

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10. When the price of the Integer is pence and farthings, if it make an even part of a shilling, work as before, but if they are uneven, as penny farthing, penny three farthings, 2 d. 1.qr. or 2 d. 3 qrs. 3 d. 3 qrs. or the like, then first work for some even part, and then consider what part the rest is of that even part, and divide that quotient thereby, then add

them together, and reduce them to pounds as before, Example, 3470 Å at 1 d. 1 qr. per l. first I work for the penny by dividing 3470 by 12, for 1 d. is 1 of a shilling, and the quote is 289 s. 2 d. then I conceive that one farthing is the 4 of a peny, and the value at one farthing, will be 4 of the value at 1 peny, and therefore I take 4 of 289 s. 2 d. which is 72 s. 3 d. 2 qrs. and add them together, and they are

1. qrs. 3470 at 5 289——2 72——3——2 3611——5——2 1. s. d. qrs. 18—1—5—2

181. 1 s. 5 d. a qrs. as by the Margent. Other Ex-

186	Rules of 1	rall	
T 2	1. d. 4360 at 1 1	1	yds d. 579 at 13
4	363-4	1	71 — 7½d. U— 11¾
	45 4-2	Page 1	83-64
	l. s. d. 22—14—2 facit		facit 4-3-63
1 6	4854. at 2 4 d.	1	520 yds at 7 1
1 8	80— 10 d. 10— 1 4	4	250 65
	90-114		2[2513 77 1.02
sin	41. 10s. 11 4 d.		164, 5 s. facit
1 3	654 L at 2 d	1 20	137 9ds at 101
4	109 27—3 d.	温丰	68 6 d. q
	13[6-3	8	11[9-1014
13	61. 16 s. 3 d.	1 .5	5% 195. 101 facil

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11. When the price of the Integer is 25. then cut off the figure in the place of Units of the given number, and double it for shillings, and the figures on the other hand are pounds. Example 436 yde at 2 s. per yd, cut off the last figure 6 and 4 4316 double it, it makes 12 shill and the a. ther 2 figures, viz. 42 are fo many 43 h 12 h pounds, fo that their value is 43 1. 12 s. as per Margent.

12. Hence

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12. Hence it is evident that (when the given price of an Integer is an even number of shillings, then if you take half of that (even number of shillings, and multiply the given number of Integers the reby, doubling the first figure of the product, and serring it spart for shill, the rest of the product will be pounds, which pounds and fittll, is the value fought. Example, What coft 526 yas at 8 s. per yd? To refolve which, I take 1 of 8 s. (the price of a yd) which is 4, and multiply 536 thereby, faying, 4 times 6 is 24, then I double the 546 7ds at 8 s.

first figure 4 makes 8 for shill. and carry a to the next product, e. I find the reft of the pro-

214 1. 8 3.

duct to be 214 which I note for pounds, fo the value of \$36 yds at 8s. per yd is 214 l. 8 s. as per Margent. More Examples follow.

56 yds at 6 s. per yd	420 yds at 12 s. per yd		
16 l. 16 s. facit	252 le facit		
123 ydsat 4 s. per yd	326 yds at 145. per yd		
24 l. 125. facit	228 l. 4 s. facit		
48 ells at 8 s. per ell	48 yds at 16 s. per yd 38 l. 8 s. facit		
19 I. 45. facit			
84 yds at 10 s. per yd	52 yds at 18 s. per yd		
42 L. facit	46 l. 16 s. facit		

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13. If the given price of the Integer is an odd number of faillings, then work first for the even number of shillings by the last Rule, and for the odd shilling rake of the given Number of Integers according to the 3 Rule of this Chap, and add them together, and you have your defire. Examples follow. 422

1ds s. 422 at 3 per yard	ells s. 431 at 13
1. s. 42—4 21—2	4. 5. 258—12
63-6 Jacit	200-03 facit
ells s. 916 at 7 per ell	ells s. 324 at 17 per ell
L s. 154—16 25—16	259—4 16—4
180-12 facit	275-8 facit

14. Except when the given price of the Integer is s. for then it is sooner answered by taking 4 of the given Number whole value is fought, as in the following Example.

Cafe 5.

15 When the given price of an Integer is shillings and pence, or shillings, pence and farthings; then if the fhillings and pence be an even part of a pound, divide the given number of Integers, whose value you seek by the denominator of that Fraction representing that even parc. As for Example, what is the price of 384 yds at 6.5. 8 d. pu va? Here I consider that 6s. 8 d, is ; of a pound, wherefore

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4 3. 12 eigh get

and out

18,

wherefore I divide 284 by 3, and the quote is the Aniwer, viz. 1281. fo that 384 yds at 61. 8 d. per yd amounts to 1281. as per margent, still. observing the 7th Rule of the 9th Chapter.

384 1281. facit

16. When the given value of the Integer is shillings and pence, and not an even part of a pound, yet many times it may be divided into parts (viz. 6 s. 6 d. is 4 s. and 2 s. 6 d. for the 4 s. work according to the 12 Rule foregoing, and for the 2 s. 6 d. take the eighth part of the given Number and add them together, then their sum is the value required.)

So 8s. 6 d. will be divided into 6s. and 2s. 6d. and the price of the given Number may be found

out as before, &c. Examples follow.

er i,

	386 at 8—9	s.	540 at 5—4
1.0	1281.—13—4 38—12—0	2	541.—• s.
1	1671. 55. 4d. facit		144 l. 03. facit
3.	tills s. d. 427 at 8-6	s.	yds s. d. 386 at 14—8
6 1 8	1284-2-0-53-7-6		1541. — 8-0
	1811. 95. 6d. fasit		2831. 1s. 4d. facit 17. When

Rules of Practice. Chap. 163

190

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17. When the given price of the Integer is shillings and pence, and you cannot readily divide them according to the laft Rule, then multiply the given number whose value you seek by the number of shillings in the price of the Integer, and then for the pence work by the 8th Rule foregoing, then add the Numbers together, and their Sum is the value fought in shillings; as for Example, what is the value of 39274s. at 6s. 9d. per rard. Here 6s. 9d. cannot be made any even part, nor indeed can it be divided into even parts of a pound, wherefore I multiply the given number of yards 392 by 6, for the 6s. the product is 2352 fhillings, then for the 9 d. I divide it into d d and 3.4. and work for them by the 8th Rule force going, and at last add the shillings together, they make 2646 s, and by the 3 Rule they are reduced to 1334 6 s. the value of 292 yds at 6 s. 9 d. per yard See the work following.

e garasi Mari da d Mari da da	o i	7ds. 3. d. 392 at 6-9
604 c c	almaja	2352 196 98 264[6
4	16 O	11321. 6 s. facit

5.	Other Exam	s.	ells s. A.
4 1/2 4/3	1920. 1 N 28 1 160	12	8784 244 183
	2320		921 1
i	116% facit	1	460 1. 115: facit 18. When

rai

6.

gs or-in in ds. de en act d

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18. When the given price of the Integer is shillings, pence and farthings, then multiply the given number of Integers by the number of shillings conrained in the value of the Integer, and for the pence and farthings follow the 10th Rule of this Chapter.

Examples.

Sie don mont mont be oro fac. 2621. 41. 9 d ...

50	yds: d. 4.438 at 8 6 3.
Simple 8	3504 219 27—434
	2750-41
lid	fac. 187 l. 20 s. 41d.

2	yds. s. d. 438 at 8-63.		ells s. d. 370 at 14—27
8 1	3504	5.	1480
1	27-4 5 4.	14	5180 d.
Rid	fac. 187 l. 20 s. 41d.	4	7 8 1
Sas Sas	ors is in the laft Bale, a and ca Bules beforegon	eds C I S	52614 91

s.	136 at 9 2 1
9 10 11	1224 - Soc 0 22 - 8. 5 - 8
	125 2-4
	fac. 62 1. 125. 4

s.	ells s. d. 431 # 2-4 1
2	862 . 29 di b
418	53 - 10 T.
	7 :
	facit BIL 35. 7 1d.

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Cafe 6.

then multiply the Number of Integers whose value is fought by the price of the Integer, and the product is the answer in pounds.

C. l. 42 at 2 per C.	C. I. 13 at 8 per C.
841. facit	104 L. facit
C. 1. 30 at 3 per C.	C. 1: 48 at 12 per C.
90 l. facit	576 L facit

20. If the price of the Integer is pounds and fhillings, then for the pounds work as in the last Rule, and for the shillings as in the 12 and 13 Rules before going; then add the Numbers produced from them both, and the Sum is the Value sought.

Examples. gross . l. a at 4-2/. IOS. 369 L RYOFS gross 1. d. 48 AL 2-7 26 at 3-31. 174 6 5. 17-145. 18. and. 194 l. 6 s. facit 971. 10 s. facit 21. When

4.

24

21. When the given price of an Integer confifts of punds, shillings, and pence, with farthings, then work for the shillings, pence, and farthings, first according to the 12 Rule of this Chapter, and find the total value of the given Number, as if there were no counds, then work with the pounds according to the 19 Rule of this Chapter, and add the Numbers thus ound, and their Sum is the total value required.

i i i i i i i i i i i i i i i i i i i	Examples of this C. L. S. arg at 1—13—.	L. J C l.	r. q	
es e	639	296 d. 18—6	8 s. 6 d.	
135. 34 514	2769 d. 53 3 26 7 ¹ / ₂	$ \begin{array}{c c} 9-3 \\ 4-7\frac{1}{2} \\ \hline 32 8-4\frac{1}{2} \end{array} $	3 d. 1 ½ d.	
14.	284 8101	16 1. 8		
	142 l. 08 s. 10 ½ 213	d. 127 L 85	111 34. 127 6. 8 s. 4 1 d. fac.	
	3551. 8s. 101d. fat	ie i	162	
95. 3 d.	erofs 1. s. d. 4 16 at 2-9-34	grofs 1. 48 at 3-	s. A	
	3744 104 26	240 48 720 24	155.	
	38714	16	1 de	
24	193 L 14 s. 0	38-5	31.	
	1025 l. 14 s. Jacit.	1821.65	facit	

yds.

1161 at

Chap 26 C 22. When there is given the value of an Integer and it is required to know the value of many and Integers together, with or or of an integer then first (by the former rules) find out the Value of the given number of Integers, and then for a an lareger take 1 of the given value of the Integer

d.

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th

or for 1 take 1 of the given value of the integer, and fi first take the i of the given value, and then i of the , fetting each part under the precedent, then adding them together, their Sum will be the required val of the Integers and their parts. Example; what is value of 116 yds. at 4 s. 6 d per yard? To give

Answer, first I work for the value of 116 yds. by the 15th. Rule foregoing, and then for the 1 yd. I take 1 of 4 s. 6 d. which is 2 s. 3 d. and add to the reft found as before then is that Sum the total value of 116 yds. at 4 s. 6 d. per yard, which I find to a-

14. 125 728 14-10d. 1 yes

26-4- 3 facit

mount to 261. 4 s. 3d. as by the work in the Marge Other Examples follow.

3244 yds. at 4 s. rod.	7201 yds. at 6 s. 8 d.	
1296 - 45.	240 1. 3 s. 4 d. facit	
162 6 d.		
108 4 d.	C-+2-2 3 (31)	
1 56 17 5. 21 d.		
781. 7 s 21 d. facit		
2283 ells at 125. 11 d.	C. grs. L. L.	
2736	1 28-3-14 at 1-10	
76 4d.	28 /.	
37-134	14 l. 10s,	
37 3 d. 3 d.	75.6d. 30	
3 - 24 d. 1 4 ell.	35. 94. 144	
295 4 8 4 d.	43 1. 6 s. 3 d. facit	

195

eger Many more queffions may be flated, and feveral other Rules of Practice may be shewn according to the eger method of divers Authors, but what have been derician in all Cases whatsoever.

The Rule of Barter.

1. D'Arter is a Rule amongst Merchants, which (in the Exchanging of one Commdity for another) informs them to to proportion their Races as that neither may fustain loss.

2. To resolve Questions in Barter, it will not be difficult to him that is acquainted with the Golden Aule, or Rule of 3, it being altogether used in resol-

ving fuch Questions.

Queft, 1. Two Merchants, (viz. A and B) Barter, A hath 13, C. 3 grs. 14 l. of Pepper at 2 l. 16 s. per C. and B hath Cotton at o d. per l. I demand how much Cotton B must give A for his Pepper ?

Anfwer, 9 C. 1 gr.

First, find by the Rule of 3, or the Rules of Prafrying,

If 1 C. coft 2 1. 16 s. what will 13 C. 3 grs. 14 to

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ACI 44 Aufwer 28 1. 173.

Secondly, By the Rule of a fay, if o d. buy 1 % of Cotron, how much will 38 4 175 buy?

Asfer, 9. C. and to much Cotron must B give to A for 13 C. 3 grs. rath of Pepper at 24, 16 1. per Cont. when the Cotton is writh 9 d. per li

Quel

Quest. 2. Two Merchants (A. and B) barter, A hath Ginger worth 1 l. 17 s. 4 d. per C. but in barter he will have 2 l. 16 s. per C. B hath Nutmegs worth 5 l. 12 l. per C. now-I demand how B must rate his Nutmeg at per C. to make his gain in barter equal to that of A?

Answer, 8 l. 8 s.
Say, By the Rule of 3, If 1 l. 17 s. 4 d. require the

barter ?

Facit 81. 8 s.

Quest. 3. A and B barter, A hath 120 yards of Broadcloth worth 6 s. per rd, but in barter he will have 84 per yd. B hath Shalloon worth 4 s. per rd. New I do mand how many yds of Shalloon. B must give A for his Broad-cloth, making his gain in barter equal n that of A?

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Answer, 180 yds of Shalloon.

First (as in the last question) find our how B ought to sell his Shalloon in barter, viz. By if 6 s. require 8 s. what will 4 s. require?

Anfwer, 5 s. 4 d.

Thus you see that B must sell his shalloon in bank ar 5 s. 4 d. if A sell his Broad-cloth at 8 s. per yd.

It remaineth now to find out how much Shallow B must give for 120 yards of broad-cloth, which after the same method used to resolve the first Question of this Chapter is found to be 180, and so many the of Shalloon must B give A for the 120 th of broad-cloth.

Quest 4. A and B bartered, A had 14 C. of Sugar worth 6 d. per 1. for which B gave him 1 C. 3 que of Cinnamon, I demand how B rated his Cinnamon per la

Anfwer, 43 per pound.

Quef. 5. A and B barrer, A hath 4 Tun of Brandy worth 37 l. 163, ready money, but in barrer he hath 50 l. 8 s. per Tun, and Agiveth B 21 c. 2 qrs. 11-14 of Ginger for his 4 Tun of Brandy, I defire to know how B fold his Ginger in barrer per C. and how much it was worth in ready money?

Anjury.

27. Chap. 28. Queftions in Lofs, &c. hath Anfwer, For 9 ! 6 s. and 8 d. in Barter, and it was

worth . l. per Cent. in ready money.

121 Queft. 6. A and B barter, A hath 320 dozen of Can-30 1. in money, and the rest in Cotten at 8 d. per l. I demand how much Cotten be must give him more quite than the 30 1. ?

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Queft. 7. A and B barter, A hath 608 yards of broad cloth worth 14 3. per yd. for which B giveth him 125 1: 125. ready money, and 85 C 2 grs. 24 1. of Bees Wax, now I defire to know how he reckoned eis Wax per C.

Animer 3. 10 s. per C.

CHAP. XXVIII.

Questions in Loss and Gain.

Merchant bought 436 yards of broad-Queff. I. cloth for 8 s. 6 d. per yard, and felleth It again at 10 s. 4 d. per yd. now I defire to know how much he gained in the Sale of the 462 yards?

Answer, 39 1. 19 s. 4 d.

First and out by the Rule of Three, or by Practice how much the Cloth coft him at 8 s. 6 d. per pd. which bfind to be 185 t. 6 s, then by the fame Rule find then substract 185 % 6 s. which it cost him, from 2251. 5 s. 4 d. which he fold irfor, and there remaineth 39 6 19 s. 4 d. for his gain in the fale thereof.

Otherwife it may fooner be refolved thus, first find out how much he gained per yd. vie. fubrract 8 3. 6 4. which he gave per yd. from 10 s. 4 d. which he fold ir for per ya. the remainder is 1 s. 10 d. for his gains

mr vd. Then fay,

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If I yd. gain I s. 10. d. what will 436 yds. gain? the Anfin. by Practice, or the Rule of Three is 39% 104

a.d. as was found before.

Quell. 2. A Draper bought 124 yds. of Holland eloth, for which he gave 31 L. I defire to know how he must sell it per yd. to gain 10 L 63. 8d. in the whole Sale of the 124 yas? Answer, at 6 s. 8.4 lay per yd.

Add the price which it coff him, (viz. 311.) to his intended gain, (viz. 101. 6 s. 8 d.) the fum is 41

6 s. 8. d. then fay,

If 124 yds. require 41 L 6s. 8d what will 1 16 require ? by the Rule of Three I find the Answer 6 s. 8 d.

Queft. A Grocer bought 3 C. 1 gr. 141. of Cloves which cost him 2 s. 4 d. per l. and fold them for 42 h 14 s. I defire to know how much he gained in the whole? Answer 84 125.

Queft. 4. A Drawr bought 86 Kerseys for 1204 I demand how he must fell them per piece to gain 144. in laying out 100 L at the rate? Answer 1 L 14 5. 6 L per piece ; fur,

As 100 % is to 11 4 % fo is 129 % to 148 % 7 3, -

So that by the proportion above, I have found how much he must receive for the 86 Kerseys to gain after the rate of 1,5 1. per C. then to find how he must fell them per piece. I fay,

As 86 pieces are to 148 4 7, st fo is I piece to 1 L

14 5. 6 d. which is the number lought.

Queft. 6. A Grecer bought 41 C. of Pepper for 1 st. 17 5. 4 d. and (it proving to be damnified) is willing to lole 12 1 10 5 per Cent. I demand how he must fell it per l. Answer 7 d. per l.

Subaract 121 101. the loss of 1001 from 100 4

and there remains 87 L. 10 s. then fay,

As 1001 is to 87 1. 10 s. to is 154 17 1. 4d. to 191, 175, 8 d. fo much as he must fell it all for to lose after the rate propounded, then to know how he must fell it per l. I fay,

As 131, 17 5. 6 d. is to 41 C. fo is 1 1. to 7 d.

Quella.

1) the Quell. 6. A Plummer fold 10 Fodder of Lead (the 191 felder containing 191 C.) for 204 l. 155, and gained after the rate of 12L 105, per 100 l. I demand how

hos To resolve this Question add 12 1. 10 5; (the Gain n the per Cent.) to 100% and it makes 112% 10% then

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As 112 1. 10 s. is to 100 1. fo is 204%. 15 5. to 1824

Which 1281, is the Sum it cost him in all, then reduce your 10 fodders to half hundreds and it makes

200, then lay,

As 200 half hundreds is to 1821. fo is 2 half hundreds to 18 s. 8 d. the price of 2 half hundreds, or one C. weight, and so much it stood him in per C.

weight.

7. A Merchant bought 8 Tuns of Wine . Queft. which being sophisticated, he selleth for 400%, and lofeth after the race of 12t. in receiving a 100 l. now I demand how much it cost him ger Tun? and how he felleth it per gallon to lofe after the faid rate ? Anfw. it coft 46 1. per tun, and he must fell it at 25. 11 d. 219 ques per gallon to lose 12 1. in receiving 1001.

To refolve this queftion I confider in the first place. that in receiving 100% he loseth 12% therefore 100% comes in for 1121. laid out, wherefore to find how

much he laid out for the whole, I fay,

As 100% is to 112% fo is 400% to 448% and to much the 8 Tun cost him, then to find how much ic coff per tun, I fay,

As 8 is to 448 l. fo is T to 56 l. the price it cast

ber Tun.

Now to find how he must sell it per gall, reduce the 8 Tuns into Gallons, they make 2016, then fay,

As 2016 Gallons is to 400 l. fo is I Gall. to 26. 11d. 230 grs. the price he must sell it at per Gall. to lose . as aforefaid.

Quest. 8. A Merchant bought 8 Tuns of Wine, which being sophisticated, he is willing to sell for 400 l. and by loseth at that rate 12l. in laying out 100 l. upon the same, now I demand how much it cost him per Tun?

Here I confider that for 100 l. laid out, he receiveth but 88 l. therefore to find what the 8 Tuns con

him, I fay,

As 88 l. is to 100 l. fo.is 400 l. to 4547 the price it all cost him, then to find how much per Tun, I say, As 8 is to 4547 t. so is 1 to 5677, or 56 l. 164 d. 1 15 gr. per Tun.

CHAP. XXIX.

Equation of Payments.

Chants whereby we reduce the times for payment of feveral Sums of Money, to an equated time for the payment of the whole Debt, without Damage to Debtor or Creditor, and

The Rule is,

2: Multiply the Sums of each particular payment by its respective Time, then add the several products together, and their Sum divide by the total debt, and the Quotient thence arising is the equated Time sorthe

payment of the whole debt. Example,

Quell. 1. A is indebted to B in the Sum of 1301. whereof 501 is to be paid at 2 months, and 501 at 4 months, and the rest at 6 months, now they agree to make one payment of the total Sum; the question is what is the equated time for payment without Damage to Debtor or Creditor?

f

Chap. 29. Equation of Payments. 201

To resolve this Question I multiply each payments by its time, viz.

50 l. multiplyed by 4 mon. producetb 200 l.

. The Sum of the Product is 480

Then I divide 480 (the Sum of the Products) by

for the time of paying the whole Debr. at 25 the 154 mount

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Quell. 2. A Merchant hash owing him 1000 l. to be paid as followeth, viz. 600 l. at 4 months, 200 l. at 6 months, and the rest (which is 200 l.) at 12 months, and he agreeth with his Debtor to make one payment of the whole, I demand the time of Payment without Damage to Debtor or Creditor?

600 l. multiplyed by 4 months is 2400
200 l. multiplyed by 6 months is 1200
200 l. multiplyed by 12 months is 2400

The Sum of the Product is---- 6000

and the Sum of the Products (6000) being dividedby the whole Debt (10001.) quotes 6 months for the time of payment of the whole Debt.

3. The truth of this Bule is thus manifest, if the interest of that Money which is paid (by the equated time) after it is due, The Proof of that be equal to the interest of that mo-Rule of Equation ney which (by the equated time) of Payments, is paid so much sooner than it is

due at any rate par 6 shentha Operation is true, other-

In the last Quest. 600 l. should have been paid at 4 months, but it is not discharged till 6 months (that is 2 months after it is due) wherefore its interest for 2 months at 6 per C. per Annum is 6 l. and then

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2001. was to be paid at 6 months, which is the equated time for its payment, therefore no interest is reckoned for it, but 200 l. should have been paid at 12 months, but it is to be paid at 6 months, which is 6 months sooner than it ought, wherefore the interest of 200 l. for 6 months is 6 l. (accompting 6 l. per Cent. per Annual) which is equal to the interest of 600 l. for 2 months, wherefore the work is right.

Quelt. 3. A Marchant hath owing him a certain fum to be discharged at 3 equal payments, viz. 1 ar two months, 1 at four months and 1 at 8 months, the question is, what is the equated time for the payment of

the whole Debt And called the trade

In questions of this nature, (viq. where the Debt is divided into equal or unequal parts) each of the parts is to be multiplyed by its time, and the sum of the product is the Answer,

multiplyed by 2 mon. produceth 1 multiplyed by 4 mon. produceth 1 multiplyed by 8 mon. produceth 22

The Sum of the Product in 43

which is 42 months for the equated time of pay-

If instead of the fractions (representing the parts) you had wrought by the numbers themselves (represented by those parts) according to the first and second Examples, it would have been the same Answer, as suppose the Debt had been 90 h, then 1 of it is 30 h for each payment, viz. at 2, 4, and 8 months, then

30 l. multipized by a mon. produceth 60 mg l. multipized by a mon, produceth 120 gol. multipized by 8 mon. produceth 240

Dissiby sell vel

which divided by 90 (the whole debr) quoteth 4 50 or 42 months as before.

203

Quell. 4. A Merchant oweth a Sum of Money to be paid 1 at 5 Months, and 1 at 8 Months, and 1 at 10 Months, and he agreeth with his Creditor to make one total payment; I demand the time, without dammage to Debtor or Creditor? Work as in the last Queffion, and you will find the Answer to be 7 Months.

Quest. 5. A is indebted to B 640%. Whereof he is to pay 40% present Money, and 350% at 3 Months, and the rest (viz. 250%) at 8 Months, and they agree-to make an Equated time for the whole Payment;

now I demand the time?

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In questions of this Nature, (viz where there is ready money paid) you are (in Multiplying) to neglect the Money that is to be paid present, and work with the rest as is before directed, and divide the Sum of the products by the whole Debt, and the Quote is the Answer: For here 40 l, is to be paid present, and hath no time allowed, and according to the Rule is should be multiplied by its time, which is (0) therefore 40 times 0 is 0, which neither augmenteth nor diminisher the Dividend; wherefore (to proceed according to direction) Hay,

350 by 8 Months producetb 1050

The Sum of the product is ____ 3050

which divided by 640, the whole Debt, the Quore is s

442 Months, the time of Payment.

Quel. 6, A is indebted to B in a certain Sum, 3 whereof is to be paid present Money, 3 at 6 Months, and the rest at 8 Months; now I demand the Equated 3 time for the payment of it all?

Answer, 3' Months is the time of payment.

Quest. 7. As indepted to B 120 L whereof & le to > be paid at 3 months, 1 at 6 months, and the rest at 9 : months; what is the Equated sime for the payment of the whole Sum?

Answer, At 6 1 months.

Quest. 8. A is indebted to B 420 l. which is due at the end of 6 months, but A is willing to pay him 1 40 l. prefent, provided he can have the remainder forborn fo much the longer to make latisfaction for his kindness, which is agreed upon, I define to know what time ought to be allotted for the payment of the

280 / remaining ?

To resolve this Question, first, find out what is the interest of 1401. for the time it was paid before it was due, at 6 per Cat. (or any other rate) (viz. 6 months) and you will find it to be 44 43. Then it is evident that the remaining 280% must be detained so much longer than 6 mon. as the while it may eat out that interest, viz. 41. 43. which is thus found out, viz. First, fee what is the Interest of 280 1. for a month, or any other time; but here we will take one month, and its Interest, for one month is 28 %.

Then by the Rule of Three, fay,

As 28 s. is to 1 month'; fo is \$4 s. to 3 months; fo that the 280 L remaining mult be kept 3 months, beyond its first time of payment, (viz 6 months) which added thereto, makes 9 months, at the end of which time A ought to make payment of the remainder.

CHAP. XXX.

EXCHANGE.

THE Rule of Exchange informeth Merchants how to exchange Moneys, Weights, or Measures of one Country into (or for) the Moneys, Weights, or Measures of another Country, and when the Rate, Reason, or Proportion betwire the Money, Weights, or Measures of different Countreys is known, it will not be difficult for the Practitioner that is well acquainted with the Rule of Proportion (or Rule of Three) to folve any Question wherein it is required

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to Exchange a given quantity of the one kind, into the same value of another kind.

2. In Questions of Exchange there is always a comparison made between the Coyns, &c. of two Coun-

tries (or kinds) or of more.

2. In Queftions where there is a comparison made between two things, (whether they be Moneys, Weights, &c.) of different kinds or (Countries) there may be a folution found by a fingle Rule of Three.

as may appear by the following Example.

Queff. 1. A Merchant at London delivered 270 1. Storline to receive the same at Paris in French Crowns. the Exchange 31 Brench Crowns per pound Sterling. I demand how many French Crowns ought he to received In placing the numbers observe the 6 Rule of the

to Chapter, which being done, the given numbers

will fland thus.

and being reduced according to the Rules of the 34 Chapter, will fland thus ; haring a his assill

L. Crowns 1. Crowns As 4 isto 10 is 37 to 1233 }

So that I conclude he ought to receive 1233 1 French Crowns at Paris for his 370 1. delivered at London.

Queft. 2. A Merchant delivered at Amfterdam 587 1. Flenish to receive the value thereof at Naples in Ducats the Exchange 44 Ducats per L. Flemifb. I demand how many Ducars he ought to receive?

The proportion is as followeth:

Ducats As 1 is to 2 1 to is 1 17 to 2817 1

So I find he ought to receive 2817 3 Ducats at Naples for the 587 L. Flemil delivered at Amfterdam.

Quest. 3. A Merchant at Florence delivereth 3478 Ducaroons, to receive the value at London in Pence, the Exchange 52 pence Sterling per Ducaroon; I demand how much Sterling he ought to receive?

The.

The Proportion for Resolution s,

As 1 is to 107 to is 347 to 186073

which is equal to 7751, 6-1 for the Answer.

I might here (according to the Custom of Arithmetical Writers) lay down Tables for the Reduction of Foreign Coyns to English; but by Reason of their Instability (for they continue not at a constant standard, as our Sterling Money doth, but are sometimes raised, and sometimes depressed) I shall forbear.

4. When there is a Comparison made between more than two different Coyns, Weights, or Measures, there ariseth ordinarily two different cases from such a Com-

parison.

1. When it is required to know how many pieces of the first Coyn, Weight, or Measure are equal in value to a known number of Pieces of the last Coyn,

Weight, or Measure.

2. When it is required to find out how many Pieces of the last Coyn; Weight, or Measure are equal in Value to a given Number of the first fort of Coyn, Weight, or Measure.

An Example of the first Cafe may be this, VIZ.

Quefl. 4. If 150 pence at Lindon are equal to 3 Docats at Naples, and 42 Ducats at Naples make 34 Shillings at Bruffels, then how many pence at London are equal to 138 Shillings at Bruffels? Facil 960 d.

This Question may be resolved at two single Rules

of Three; for first Ifay,

If 1 Ducars at Naples make 150 Pence London, how many Pence will 42 Ducars make?

Answer, 240 Pence.

By the foregoing Proportion, we have discovered that 43 Ducats at Naples make 240 Pence at London

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Lindon: And by the Tenour of the Question we see that 42 Ducats at Venice make 342 shillings at Brussels, therefore 240 d. at Lond. are equal to 342 sat Brussels, (for the things that are equal to one and the same thing are also equal to one another) wherefore we have a way laid open to give a solution to this Question by another Single Rule of Three, whose Proportion is,

As 34 fhillings at Bruffels is to 240 pence at London, to is 138 shill. at Bruffels to 960 pence at London,

which is the Answer to the Queffion.

As Example of the Second Cafe mar be thus, VIZ.

Bast. 5. If 40 L. Averdupois weight at London is equal to 26 l. weight at Amsterdam, and 90 l. at Amsterdam makes 116 l. at Dantziek, then how many pounds at Dantziek are equal to 112 L of Averdupies weight at London?

Answer, 12923 pounds at Dantzick.

This Question is likewise answered at two single Rules of Three, viz. First, I say,

As 36 l at Amsterdam is to 40 l. at Lond. . So is 90 l. at Amsterdam to 100 l. at Lond.

And by the Question you find that 90 L at Austerdam is 116 L at Daniziek, and therefore 100 L at London is likewise equal thereunto, wherefore again, I say,

As 100 l. at London is to 116 l. at Dantrick, So is 112 l. at Londo to 129. 321. at Dantrick.

By which I find that 11231 at Dantgiot are equal

to 1121 Averdapois weight at Lord.

g. There is a more speedy way to resolve such Questions as are contained under the two Cases beforementioned, laid down by Mr. Kersy in the third Chapter of his Appendix to Mr. Wingati's Arichmetick, where he hash given two Rules for the Resolution of the Questions pertinent to the two said Cases.

6 But I shall lay down a general Rule for the solution of both Cales; and first, let the Learner observe the sollowing Directions in placing of the given terms,

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7. Let these be made two Columns, and in these Columns so place the given terms one over the other, as that in the same Column there may not be found two terms of the same kind one with the other.

Having thus placed the Terms, the General Rule

IS.

Offerve which of the said Columns bath the most Terms placed in it, and multiply all the Terms there in continually, and place the last product for a Dividend; then multiply the Terms in the other Column continually, and let the last Product be a Divisor, then divide the said Dividend by the said Divisor, and the Quotient thence arising is the Answer to the Question.

So the Example of the first of the said Cases being again repeated, viz. if 150 pence at London make 3 Ducars at Naples, and 4 Ducars at Naples make 34 thill, at Brussels, then how many Pence at London are

equal to 138 shillings at Bruffels ?

The terms being placed according to the 7th Rule will fland as followeth.

Pence at Lond. 150 3 Ducats at Na.
Ducats at Na. 45 343 Shill, at Bruff. 128

having thus placed the Terms that in either Column there is two Terms of one kind, then observe that the Column under A hath most terms in it, therefore they must be multiplyed together for a Dividend; viz. 150 mult. by 4‡ produceth 360\$ which multiplyed by 128 produceth 49510\$ for a Dividend, then in the Column under B there are 2 and 34½ which multiplyed together; produce 200 for a Divident; when having divided 496100 by 200 the Quotient is 560 pence for the answer as before,

Again, let the Example of the second case be again repeated, viz. If 40 l. Averdupois weight at London make 36 l. weight at Amstrdam, and 90 l. at Amstrdam make 116 l. at Danezick, then how many pounds at Danezick are equal to 112 l. Averdupois weight at London.

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The terms being disposed according to the 7th.

L. at Lond. | 40 | 96 | L. at Amsterdam

whereby I find that the terms under B multiplyed together produce 467712 for a dividend, and the terms under A, viz. 40 and 90 produce 3600 for a Divisor, and Division being finished, the quotient aivern 1293312 pounds at Dantzick for the Answer.

CHAP. XXXI.

Single Position.

I. Egative Arithmetick, called the Rule of Falle, is that by which we find out a truth, by numbers invented or supposed, and this is either single or double.

2. The Rule of Single Position is when at once, viz. by one Palie position, or seigned number, we.

find out the true Number fought.

3. In the fingle Rule of Falle, when you have made choice of your position, work it according to the senour of the question, as if it were the true number sought, and if by the ordering of your position you find the result either too much or too little you may then find out the number sought by this proportion following, Viz.

As the result of your position is to the position, to

is the given number to the number fought.

Example.

Quell. 1. A Person having about him a certain number of Crowns, said if the fourth and third and sixth of them were added together, they would make just 45, now I demand the number of Crowns he had about him? Answer, 60 Crowns.

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To resolve this question I suppose he had 24 Growns (or any other number that will admit of the like division) now the fourth of 24 is 6, and the third is 8, and the fixth is 4, all which parts (viz. 6, 8, and 4,) being added together make but 18, but it should be 45, wherefore I say by the Rule of Three,

As 18, the fum of the parts is to the position 24, fo is 45 the given number to 60 the true number

fought.

For the fourth of 60 is 14, and the third of 60 is 20, and the fixth of 60 is 10, which added together

make 45.

Quell. 2. Three Persons, vig. A. B, C, thus difcourse together concerning their Age, quoth B to A, I am as old, and half as old again as you, then quoth C to B I am twice as old as you, then quoth A to them and I am sure the Sum of all our Ages is 165, now I demand each mans Age? Answer, A 30, B 45, C 90 years of Age, which added together, make 165.

CHAP. XXXII.

Double Position.

THE Rule of Double Position is when 2 falle positions are assumed to give a Resolution to the question propounded.

2. When any Question is stated in double position make such a Cross as followeth.

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3. Then make choice of any number you think may be convenient for your working, which call your first Position, and place it at that end of the Cross at a, then work with this position (as if it were the true number

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number fought) according to the nature of your queflion, then having found out your errour, either too much or too little, place it on that fide the Crofs d, then make choice of another number of the same denomination with the field position (which call-your fecond polition) and place it on that fide of the Cross at & then work with this polition as with the former, and having found our your error, either too much or too little, place it on that fide of the Crofs at e, and then the positions will stand at the top of the cross, and the errors at the bottom, cach under his correspondent position, and then multiply the errors into the positions cross-wife, that is to say, multiply the first posicion by the second error, and the second polition by the first error, and put each product over its polition.

A Having proceeded so far, then consider whether the errors were both alike, that is, whether they were both too much, or both too little, and if they are alike, then subtract the lesser product from the greater, and set the remainder for a dividend, then subtract the lesser Error from the greater, and let the remainder be a divisor, then the quotient arising by

this Division is the answer to the question.

g. But if the errors are unlike, that is one too much and the other too little, then add the products of the positions and errors together, and their Sum shall be a dividend; then add the errors together, and their Sum shall be a Divisor, and the Quotient arising hence is the Answer; which two last Rules may be kept in memory by this Verse following, vie.

When Errors are of unlike kinds Addition doth erfut, But if a like, Subtraction finds Dividing work for you.

Queft. 1. A. B. and C build a Honfe which coft 76 t. of which A paid a certain Sum unknown .

B paid

Chap, 32

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B paid as much as A, and rot over, and C paid a much as A and B, now I defire to know each man

Share in that Charge?

Having made a Cross according to the 2 Rule, I come according to the third Rule to make choice of any first position, and here I suppose A paid 64, which I put upon the Cross as you see, then B paid 164. (for it is said he paid 104. more than A) and C paid 224. for 'tis said he paid as much as A and B, when I add their parts.

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and they amount to 44, but it is faid they paid 764, wherefore it is 32 too little, which I note down at the bottom of the Cross under its position for the first

Secondly, Fluppote A paid 9 l. then B paid 19 l. and C 28 l. all which added together, make 56, but they should make 76, wherefore the error of this position is 20, which I put at the bottom of the Crosunder his position for the second Error, then I multiply the Errors and the Positions Cross-wise, viz. 32 (the Error of the stress Position) by 9 (the second Position,) and the product is 288. Then I multiply 20 (the Error of the second Position) by 6 (the first position), and the Product is 120.

Then (according to the 4th. Rule) I subtract the lesser Product from the greater, (via 120. from 288, because the Errors are both alike, viz. too little)

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and there remaineth 168 for a Dividend, then I substract 20, (the lesser Error) from 32 (the greater Error) and the Remainder is 12 for a Divisor, then divide 168 by 12, and the Quotient is 14 for the Answer, which is the share of A in the Payment.

6. Again Secondly, If the errors had been both too big it had had the same effect, as appeareth by the following work; for first I suppose A paid 201. then B paid 301. and C. 50.1. which in all is 100, but it should have been no more than 76, wherefore the first Error is 24 too much. Again, I suppose A paid 181. then B must pay 281. and C must pay 46.1 which in all

90 B : 10 11 12 12 13 13 13 13 13 13 13 13 13 13 13 13 13		B 28
40 C 20 I	12 432	C 46
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is 921: but it should have been but 764 wherefore the second Error is 16 too much; then I multiply 20 (the second Error) and the Product is 320, again I multiply 18, (the second Position) by 24 (the second Error) and the product is 422: Then because the Errors are both too much, I substract 320 (the second from 432 (the greater product,) and there remained 112 for a Dividend, likewise I substract (16 the second Error) from 24 (the greater Error,) and the difference is 8 for a Division, then perform Division, and the Quotient is 14, (as before) for the answer.

Again Thirdly, If the Errors had been the one too big' and the other too little, Respect being had to the 3th. Rule foregoing, the Answer would have been the same; a sthus, I take for my first Postion 6, and then the Error is 32 too little, then I

take for my fecond Policion 18, and then the error is 16 too much, then I multiply the Politions and en rors Cross-wife, and the products are 96 and \$76, at because the errors are unlike,

96 672 576 130ml 3 6 718 ears you have all G14 32 6 316 the state of the state of the state of the

(viz.) one too big, and another too little, I add the products 96 and 576 together, and their Sum is 674 for a Dividend, I likewife add the errors 32 and 16 together, and their Sum is 48 for a Divilor, then he ving finished Division, I find the Quotient to be 1 which is the answer as was found out at the 2 several Tryals before.

For proof of the Work I fay,

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Then:	C	paid	14	and	24	(that	u)-	
Hill:	B	3 17	7/1	all	001	30	of Arriva	

which is the total value of the building and equal to

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the given Numbered didding agents in Those who defire to see the demonstration of this Rule, let them read the 7th Chap. of Mr. Kafin Appendix to Wingates Arithmeticks Patifeus in the 5th Book of his Trigonometria. Or Mr. Ongbired in his Clavit

Quell. 2. Three Persons, A, B, C, thus discoursed together concerning their Age ; quoth A I am 18 years of Age, quoth B I am as old as A and 1C; and quoth Clam as old as you both, if your years were added together. Now I defire to know the Age of each Perfoo ? Anfwer A is 18, B is 54, and C is 72 years of Age. Queft. 2

Quiff. 3. A Father lying at the point of Death, left to his 3 Sons, viz. A, B, Q, all his Effate in Money, and divideth it as followeth, viz. to A he gave \(\frac{1}{2}\) wanting 44 \(\lloar{1}\). to B he gave \(\frac{1}{2}\) and 14 \(\lloar{1}\). over, and to C he gave the Remainder, which was \$2 \(\lloar{1}\) left thus the thare of B, now I demand what was the Sum left, and each mans part ? Answer, The Sum bequeathed was \$88 \(\lloar{1}\). and whereof A had \$252 \(\lloar{1}\). B had \$210 \(\lloar{1}\), and C had \$128 \(\lloar{1}\).

Quell. 4. Two persons, viz. A and B had each in their hands a certain number of Crowns, and A said to B, if you give me I of your Crowns I shall have 5 times as many as you, and said B to him again, if you give me one of yours, then we shall each of us have an equal number; now I demand how many Crowns had each Person? Answer, A had 4, and B had 2 Crowns.

Crowns

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Quell. 9, What number is that unto which if I add of it fell, and from the Sum subtract of it fell, the Remainder will be 210? Answer, 192.

Many more questions may be added, but these well understood, will be sufficient, (even for the meanest Capacity) for the Resolution of any other question

pertinent to this Rule.

There may be an objection made because we have not treated particularly upon interest and Rebate, but the operation of such Questions being more applicable to Decimals, are omitted; till we come to acquaint the Learner therewith.

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